



**Tutorial T1**  
**Fundamentals of Music Processing:**  
**An Introduction using Python and Jupyter Notebooks**

### Audio Structure Analysis

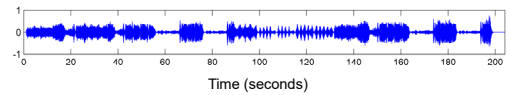
**Meinard Müller, Frank Zalkow**

International Audio Laboratories Erlangen  
 meinard.mueller@audiolabs-erlangen.de, frank.zalkow@audiolabs-erlangen.de



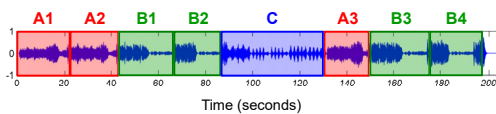
### Music Structure Analysis

**Example:** Brahms Hungarian Dance No. 5 (Ormandy)



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### Music Structure Analysis

**General goal:** Divide an audio recording into temporal segments corresponding to musical parts and group these segments into musically meaningful categories.

**Examples:**

- Stanzas of a folk song
- Intro, verse, chorus, bridge, outro sections of a pop song
- Exposition, development, recapitulation, coda of a sonata
- Musical form ABACADA ... of a rondo

### Music Structure Analysis

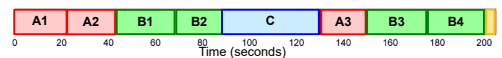
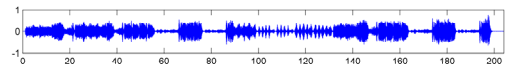
**General goal:** Divide an audio recording into temporal segments corresponding to musical parts and group these segments into musically meaningful categories.

**Challenge:** There are many different principles for creating relationships that form the basis for the musical structure.

- **Homogeneity:** Consistency in tempo, instrumentation, key, ...
- **Novelty:** Sudden changes, surprising elements ...
- **Repetition:** Repeating themes, motives, rhythmic patterns,...

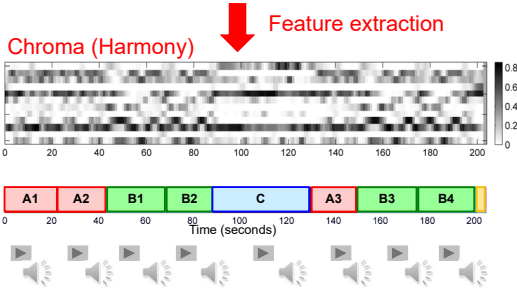
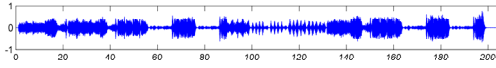
### Feature Representation

**Example:** Brahms Hungarian Dance No. 5 (Ormandy)



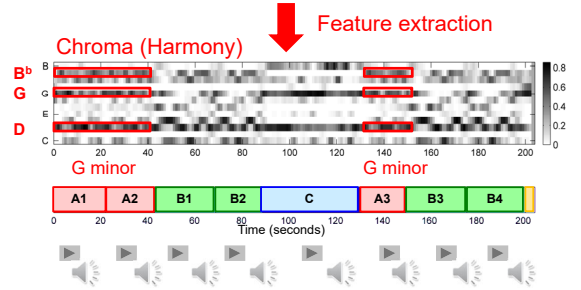
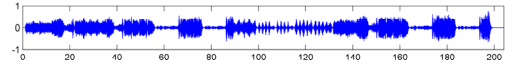
## Feature Representation

Example: Brahms Hungarian Dance No. 5 (Ormandy)



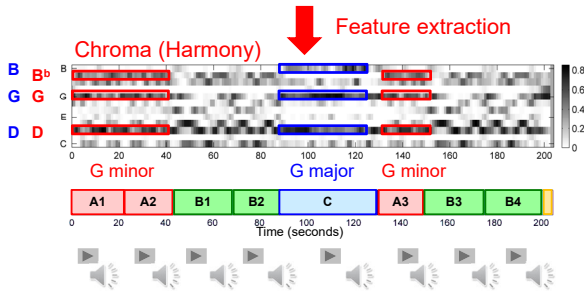
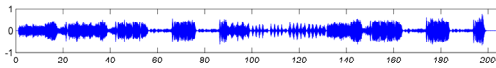
## Feature Representation

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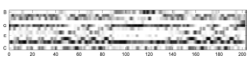
## Self-Similarity Matrix (SSM)

**General idea:** Compare each element of the feature sequence with each other element of the feature sequence based on a suitable similarity measure.

→ Quadratic self-similarity matrix

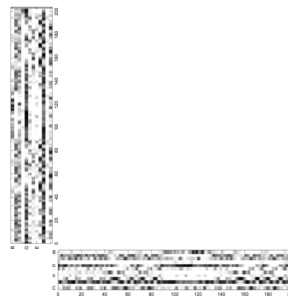
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Example: Brahms Hungarian Dance No. 5 (Ormandy)



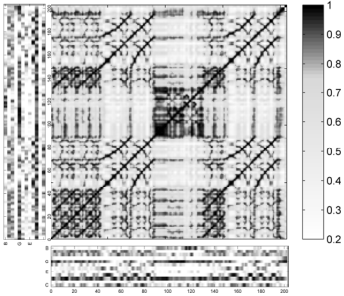
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Example: Brahms Hungarian Dance No. 5 (Ormandy)



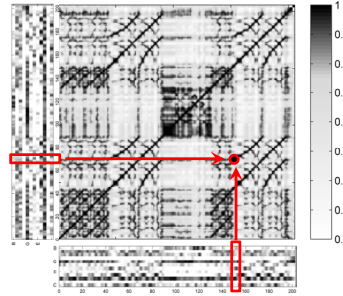
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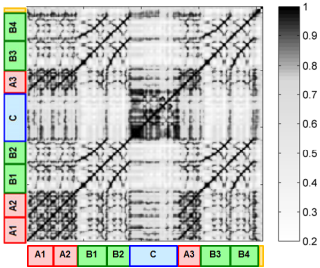
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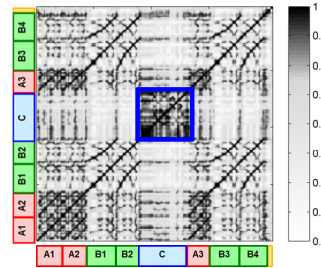
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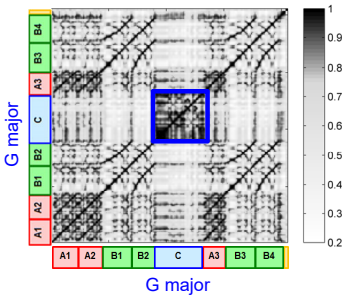
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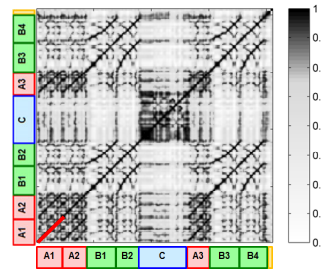
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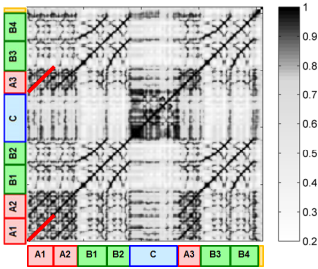
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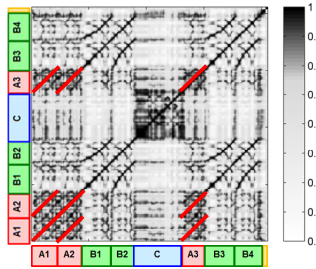
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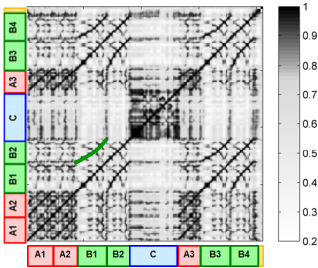
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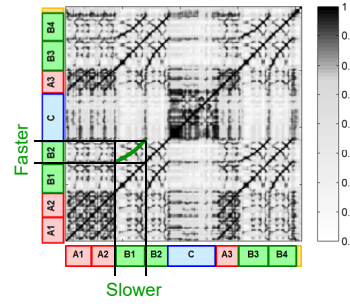
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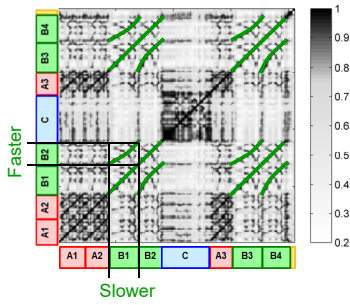
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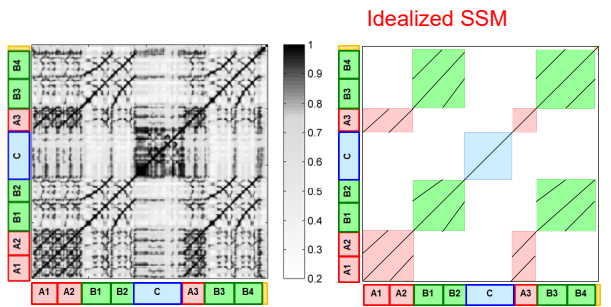
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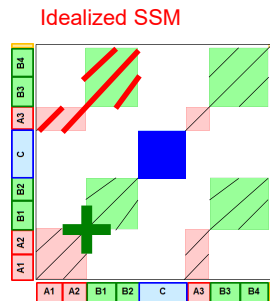
## Self-Similarity Matrix (SSM)

**Example:** Brahms Hungarian Dance No. 5 (Ormandy)

**Blocks:** Homogeneity

**Paths:** Repetition

**Corners:** Novelty



## SSM Enhancement

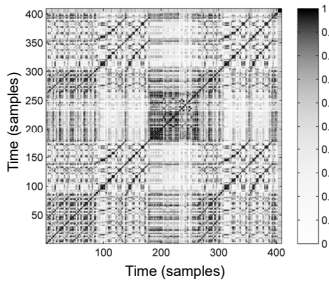
**Challenge:** Presence of musical variations

- Fragmented paths and gaps
- Paths of poor quality
- Regions of constant (low) cost
- Curved paths

**Idea:** Enhancement of path structure

## SSM Enhancement

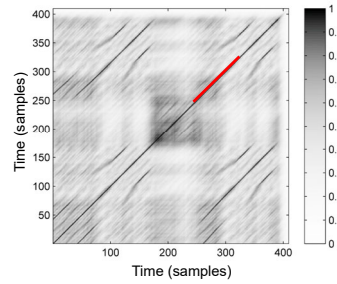
**Path Enhancement**



## SSM Enhancement

**Path Enhancement**

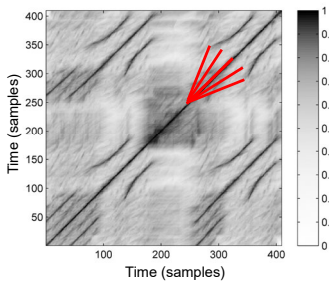
- Diagonal smoothing



## SSM Enhancement

**Path Enhancement**

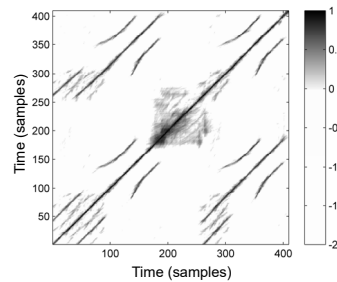
- Diagonal smoothing
- Multiple filtering



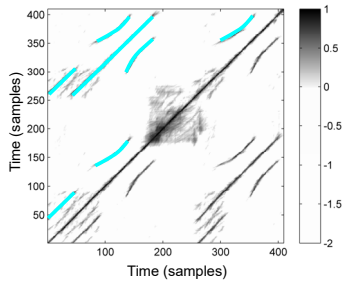
## SSM Enhancement

**Path Enhancement**

- Diagonal smoothing
- Multiple filtering
- Thresholding (relative)
- Scaling & penalty



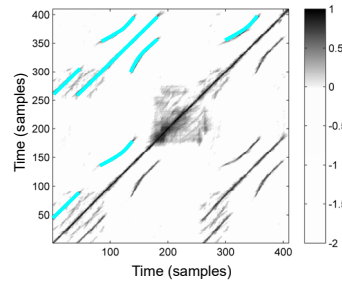
## SSM Enhancement



### Further Processing

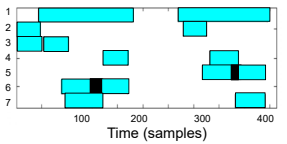
- Path extraction

## SSM Enhancement

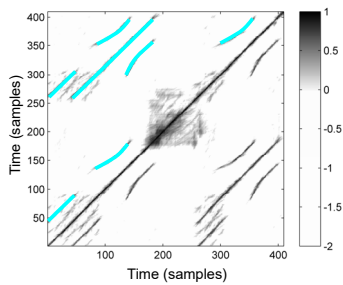


### Further Processing

- Path extraction
- Pairwise relations

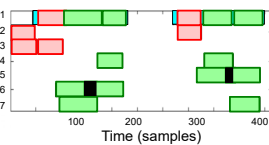


## SSM Enhancement

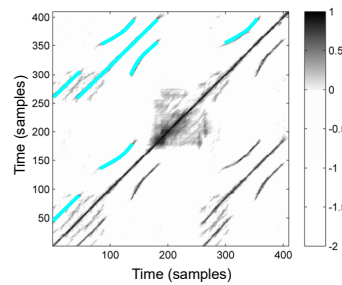


### Further Processing

- Path extraction
- Pairwise relations
- Grouping (transitivity)

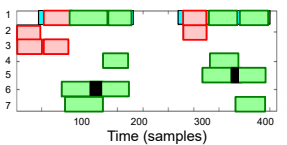


## SSM Enhancement



### Further Processing

- Path extraction
- Pairwise relations
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## Novelty-Based Segmentation

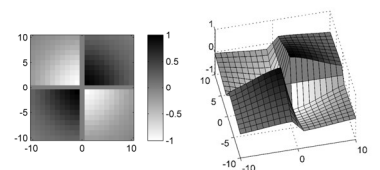
## Novelty-Based Segmentation

### General goals:

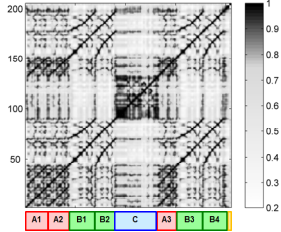
- Find instances where musical changes occur.
- Find transition between subsequent musical parts.

### Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.



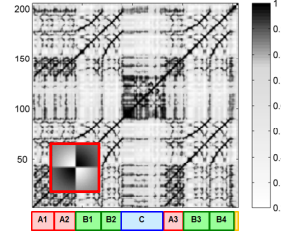
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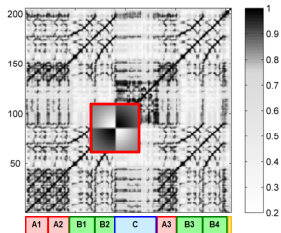
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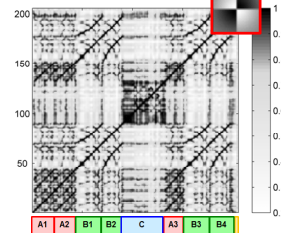
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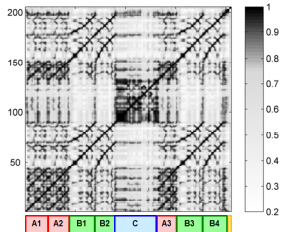
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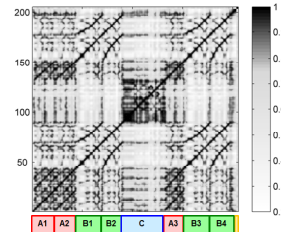
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Novelty function using



## Novelty-Based Segmentation



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Novelty function using

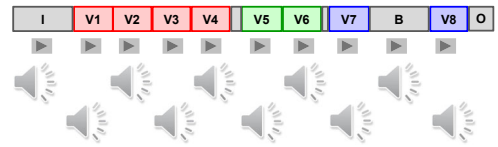


Novelty function using



## SSM Enhancement

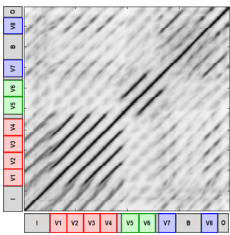
Example: Zager & Evans "In The Year 2525"



## SSM Enhancement

Example: Zager & Evans "In The Year 2525"

Missing relations because of transposed sections

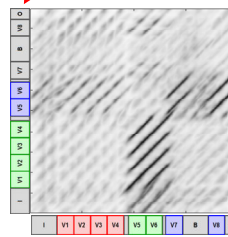


## SSM Enhancement

Example: Zager & Evans "In The Year 2525"

Idea: Cyclic shift of one of the chroma sequences

One semitone up

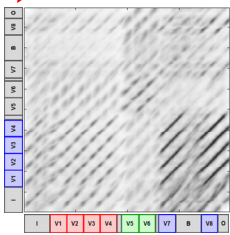


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Example: Zager & Evans "In The Year 2525"

Idea: Cyclic shift of one of the chroma sequences

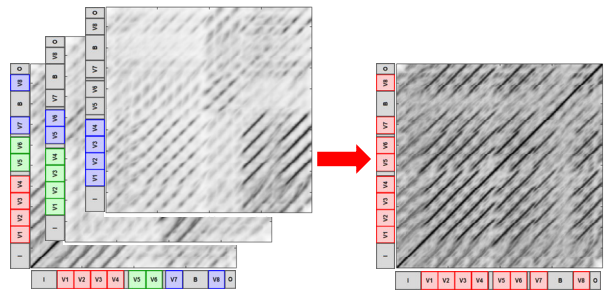
Two semitones up



## SSM Enhancement

Example: Zager & Evans "In The Year 2525"

Idea: Overlay & Maximize → Transposition-invariant SSM





## Audio Thumbnailing

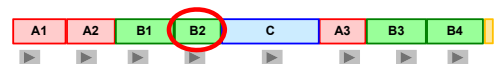
## Audio Thumbnailing

**General goal:** Determine the most representative section ("Thumbnail") of a given music recording.

**Example:** Zager & Evans "In The Year 2525"



**Example:** Brahms Hungarian Dance No. 5 (Ormandy)



Thumbnail is often assumed to be the most repetitive segment

## Audio Thumbnailing

### Two steps

#### 1. Path extraction

### Both steps are problematic!

- Paths of poor quality (fragmented, gaps)
- Block-like structures
- Curved paths

#### 2. Grouping

- Noisy relations (missing, distorted, overlapping)
- Transitivity computation difficult

### Main idea: Do both, path extraction and grouping, jointly

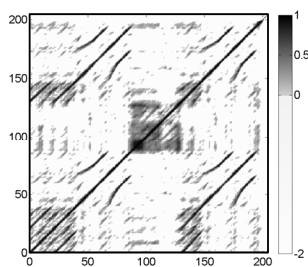
- One optimization scheme for both steps
- Stabilizing effect
- Efficient

## Audio Thumbnailing

Main idea: Do both path extraction and grouping jointly

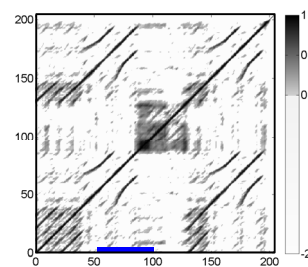
- For each audio **segment** we define a **fitness** value
- This fitness value expresses "how well" the segment explains the entire audio recording
- The segment with the highest fitness value is considered to be the **thumbnail**
- As main technical concept we introduce the notion of a **path family**

## Fitness Measure



Enhanced SSM

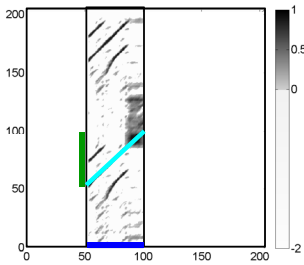
## Fitness Measure



Path over segment

- Consider a fixed **segment**

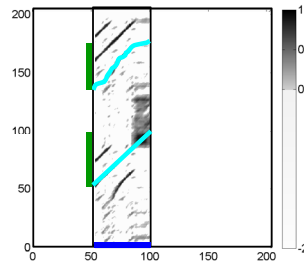
## Fitness Measure



### Path over segment

- Consider a fixed **segment**
- **Path** over **segment**
- **Induced segment**
- Score is high

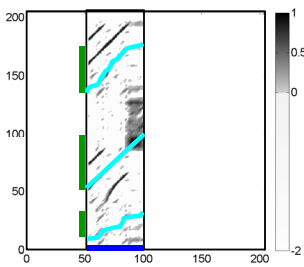
## Fitness Measure



### Path over segment

- Consider a fixed **segment**
- **Path** over **segment**
- **Induced segment**
- Score is high
- A **second path** over **segment**
- **Induced segment**
- Score is not so high

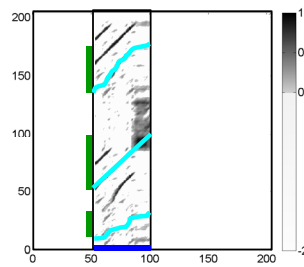
## Fitness Measure



### Path over segment

- Consider a fixed **segment**
- **Path** over **segment**
- **Induced segment**
- Score is high
- A **second path** over **segment**
- **Induced segment**
- Score is not so high
- A **third path** over **segment**
- **Induced segment**
- Score is very low

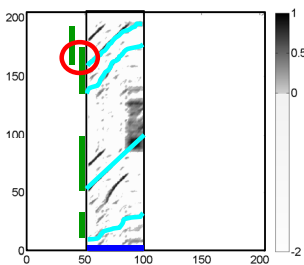
## Fitness Measure



### Path family

- Consider a fixed **segment**
- A path family over a **segment** is a family of paths such that the **induced segments** do **not overlap**.

## Fitness Measure

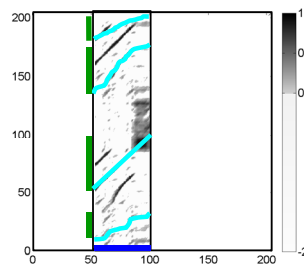


### Path family

- Consider a fixed **segment**
- A path family over a **segment** is a family of paths such that the **induced segments** do **not overlap**.

This is **not** a path family!

## Fitness Measure

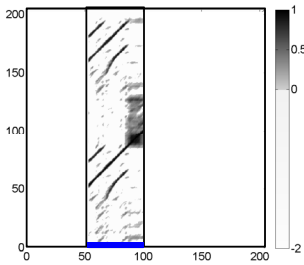


### Path family

- Consider a fixed **segment**
- A path family over a **segment** is a family of paths such that the **induced segments** do **not overlap**.

This is a path family!  
(Even though not a good one)

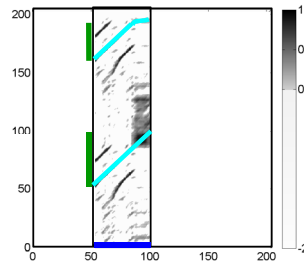
## Fitness Measure



### Optimal path family

- Consider a fixed **segment**

## Fitness Measure

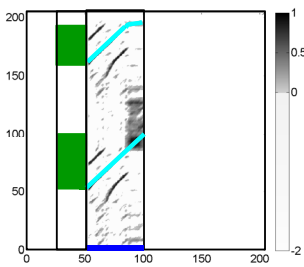


### Optimal path family

- Consider a fixed **segment**
- Consider over the **segment** the **optimal path family**, i.e., the path family having maximal overall score.
- Call this value:  $\text{Score}(\text{segment})$

Note: This optimal path family can be computed using dynamic programming.

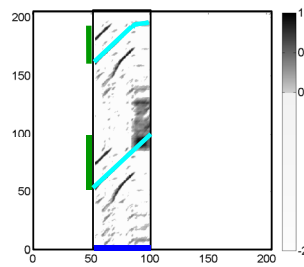
## Fitness Measure



### Optimal path family

- Consider a fixed **segment**
- Consider over the **segment** the **optimal path family**, i.e., the path family having maximal overall score.
- Call this value:  $\text{Score}(\text{segment})$
- Furthermore consider the amount covered by the **induced segments**.
- Call this value:  $\text{Coverage}(\text{segment})$

## Fitness Measure



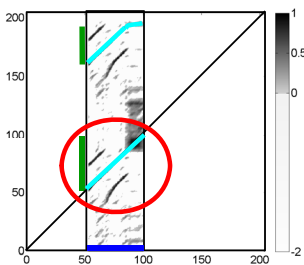
### Fitness

- Consider a fixed **segment**

$$P := \text{Score}(\text{segment})$$

$$R := \text{Coverage}(\text{segment})$$

## Fitness Measure



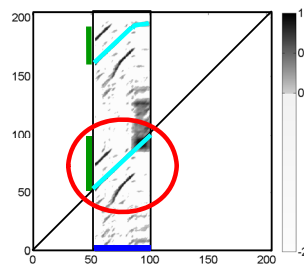
### Fitness

- Consider a fixed **segment**
- Self-explanation are trivial!**

$$P := \text{Score}(\text{segment})$$

$$R := \text{Coverage}(\text{segment})$$

## Fitness Measure



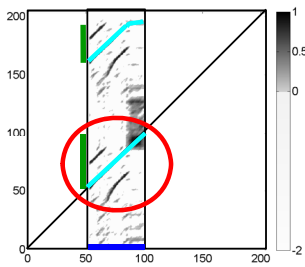
### Fitness

- Consider a fixed **segment**
- Self-explanation are trivial!**
- Subtract length of **segment**

$$P := \text{Score}(\text{segment}) - \text{length}(\text{segment})$$

$$R := \text{Coverage}(\text{segment}) - \text{length}(\text{segment})$$

## Fitness Measure



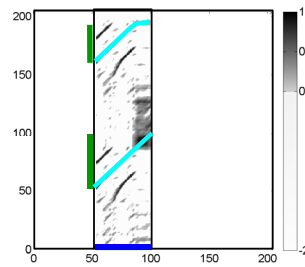
### Fitness

- Consider a fixed **segment**
- Self-explanations are trivial!
- Subtract length of **segment**
- Normalization

$$P := \text{Normalize}(\text{Score}(\text{segment}) - \text{length}(\text{segment})) \in [0,1]$$

$$R := \text{Normalize}(\text{Coverage}(\text{segment}) - \text{length}(\text{segment})) \in [0,1]$$

## Fitness Measure



### Fitness

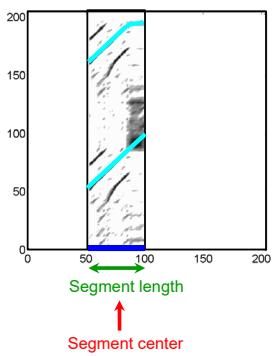
- Consider a fixed **segment**

$$F := \frac{2 \cdot P \cdot R}{P + R}$$

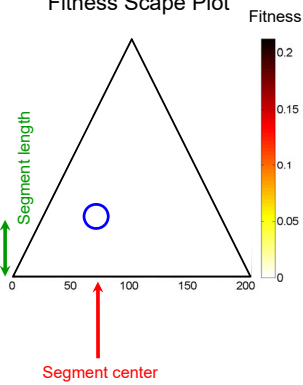
$$P := \text{Normalize}(\text{Score}(\text{segment}) - \text{length}(\text{segment})) \in [0,1]$$

$$R := \text{Normalize}(\text{Coverage}(\text{segment}) - \text{length}(\text{segment})) \in [0,1]$$

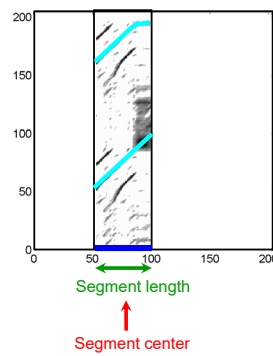
## Thumbnail



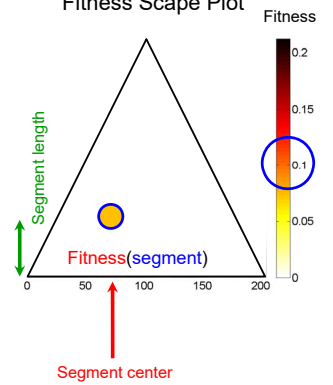
### Fitness Scape Plot



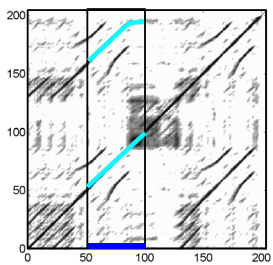
## Thumbnail



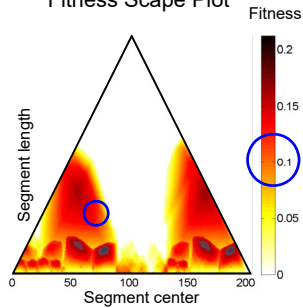
### Fitness Scape Plot



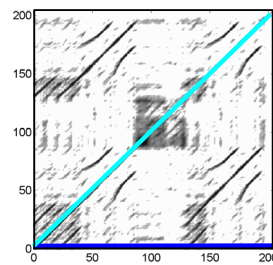
## Thumbnail



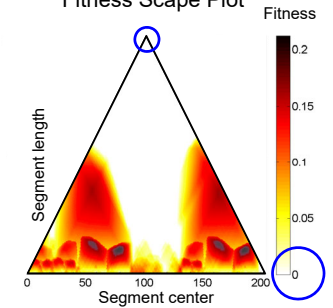
### Fitness Scape Plot



## Thumbnail

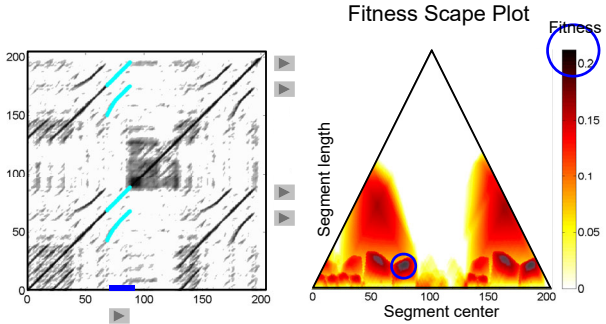


### Fitness Scape Plot



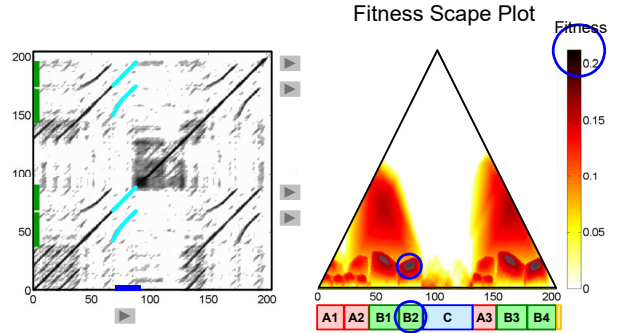
Note: Self-explanations are ignored → fitness is zero

### Thumbnail



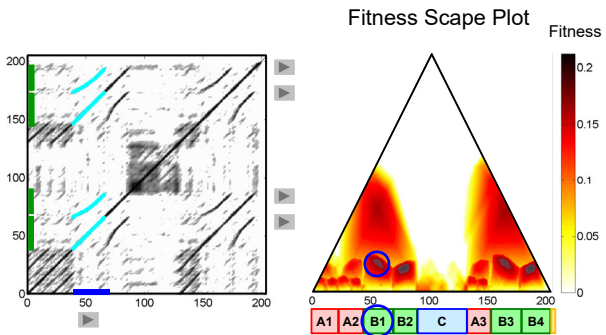
Thumbnail := segment having the highest fitness

### Thumbnail



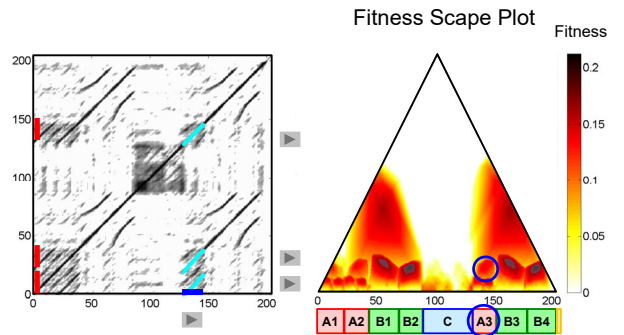
Example: Brahms Hungarian Dance No. 5 (Ormandy)

### Thumbnail



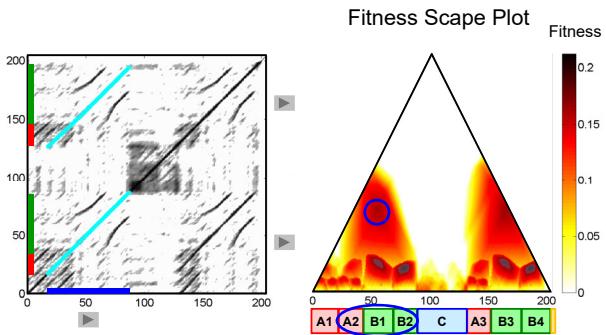
Example: Brahms Hungarian Dance No. 5 (Ormandy)

### Thumbnail



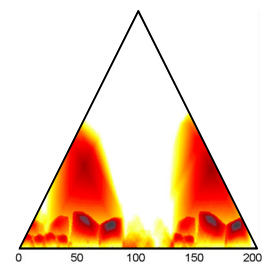
Example: Brahms Hungarian Dance No. 5 (Ormandy)

### Thumbnail



Example: Brahms Hungarian Dance No. 5 (Ormandy)

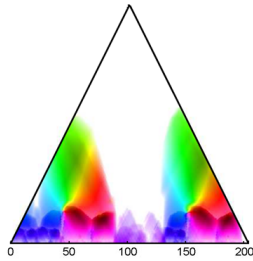
### Scape Plot



Example: Brahms Hungarian Dance No. 5 (Ormandy)

## Scape Plot

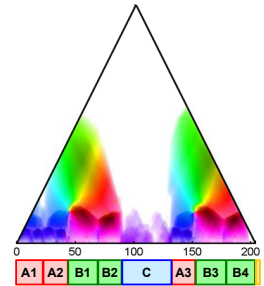
Coloring according to clustering result (grouping)



**Example:** Brahms Hungarian Dance No. 5 (Ormandy)

## Scape Plot

Coloring according to clustering result (grouping)

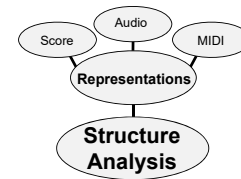


**Example:** Brahms Hungarian Dance No. 5 (Ormandy)

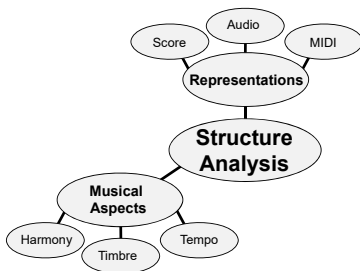
## Conclusions

**Structure Analysis**

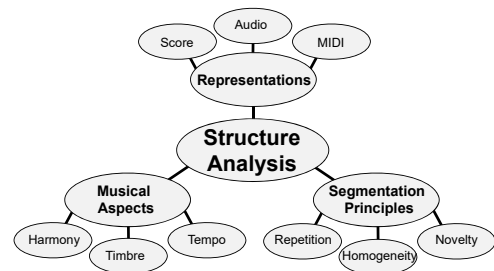
## Conclusions



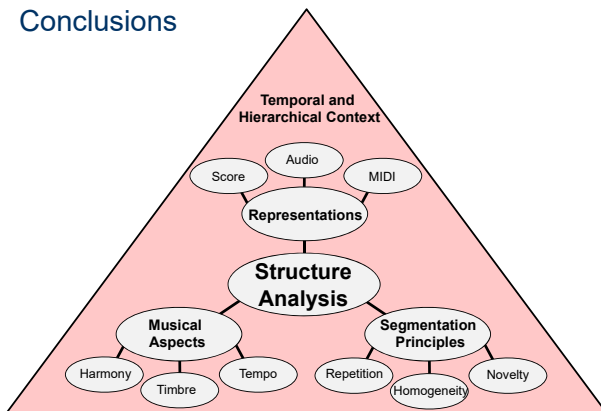
## Conclusions



## Conclusions



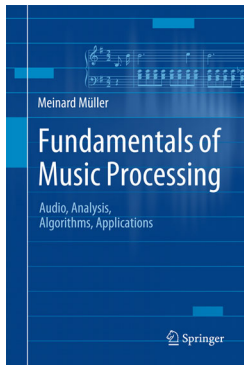
## Conclusions



## Links

- SM Toolbox (MATLAB)  
<http://www.audiolabs-erlangen.de/resources/MIR/SMtoolbox/>
- MSAF: Music Structure Analysis Framework (Python)  
<https://github.com/urinieto/msaf>
- SALAMI Annotation Data  
<http://ddmal.music.mcgill.ca/research/salami/annotations>
- LibROSA (Python)  
<https://librosa.github.io/librosa/>
- Evaluation: mir\_eval (Python)  
[https://craffel.github.io/mir\\_eval/](https://craffel.github.io/mir_eval/)
- Deep Learning: Boundary Detection  
Jan Schlüter (PhD thesis)

## Book: Fundamentals of Music Processing



Meinard Müller  
Fundamentals of Music Processing  
Audio, Analysis, Algorithms, Applications  
483 p., 249 illus., hardcover  
ISBN: 978-3-319-21944-8  
Springer, 2015

Accompanying website:  
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## Book: Fundamentals of Music Processing

Chapter	Music Processing Scenario
1	Music Representations
2	Fourier Analysis of Signals
3	Music Synchronization
4	Music Structure Analysis
5	Chord Recognition
6	Tempo and Beat Tracking
7	Content-Based Audio Retrieval
8	Musically Informed Audio Decomposition

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