



**Tutorial T1**  
**Fundamentals of Music Processing:**  
**An Introduction using Python and Jupyter Notebooks**

# **Audio Structure Analysis**

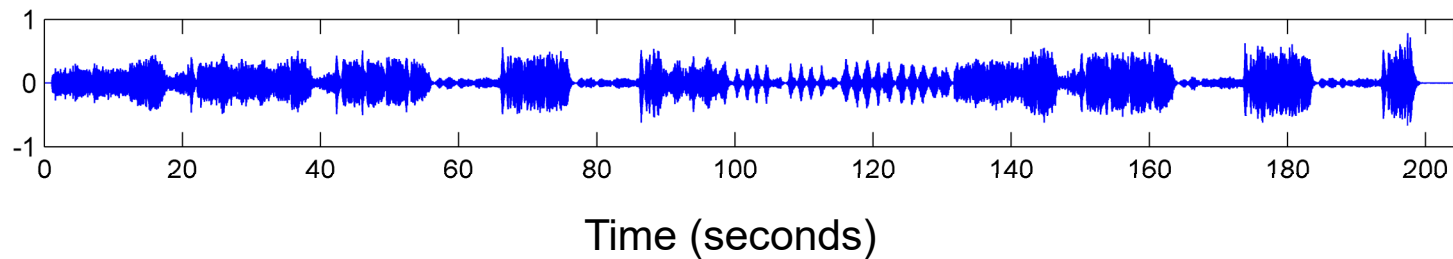
**Meinard Müller, Frank Zalkow**

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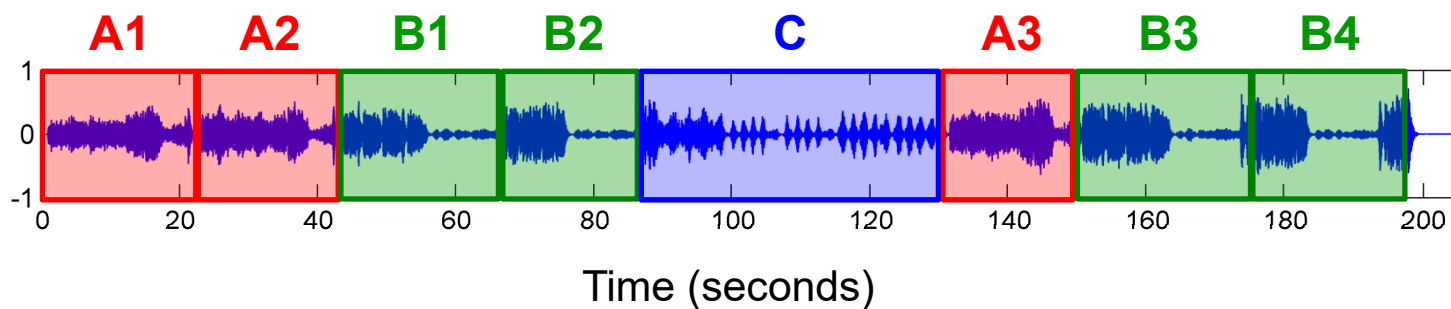
# Music Structure Analysis

**Example:** Brahms Hungarian Dance No. 5 (Ormandy)



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# Music Structure Analysis

**General goal:** Divide an audio recording into temporal segments corresponding to musical parts and group these segments into musically meaningful categories.

## Examples:

- Stanzas of a folk song
- Intro, verse, chorus, bridge, outro sections of a pop song
- Exposition, development, recapitulation, coda of a sonata
- Musical form ABACADA ... of a rondo

# Music Structure Analysis

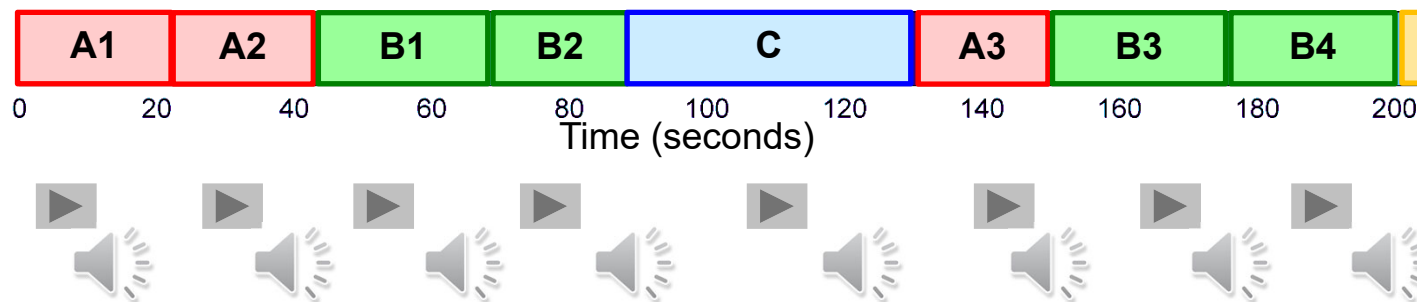
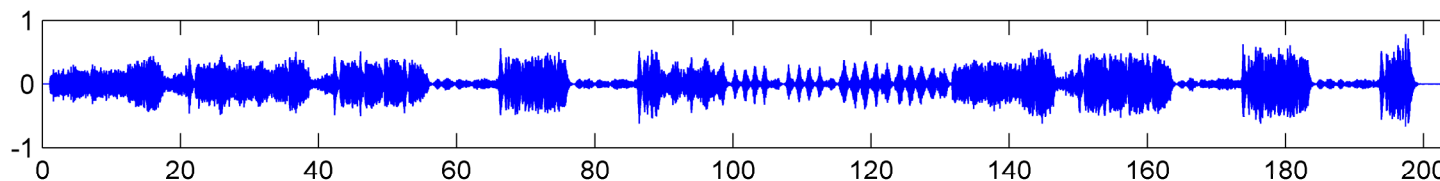
**General goal:** Divide an audio recording into temporal segments corresponding to musical parts and group these segments into musically meaningful categories.

**Challenge:** There are many different principles for creating relationships that form the basis for the musical structure.

- **Homogeneity:** Consistency in tempo, instrumentation, key, ...
- **Novelty:** Sudden changes, surprising elements ...
- **Repetition:** Repeating themes, motives, rhythmic patterns,...

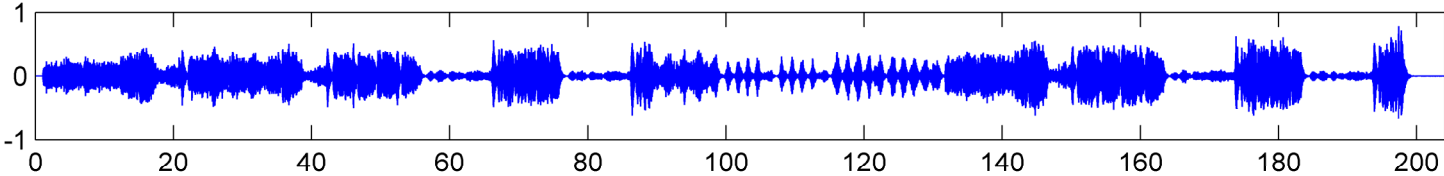
# Feature Representation

**Example:** Brahms Hungarian Dance No. 5 (Ormandy)

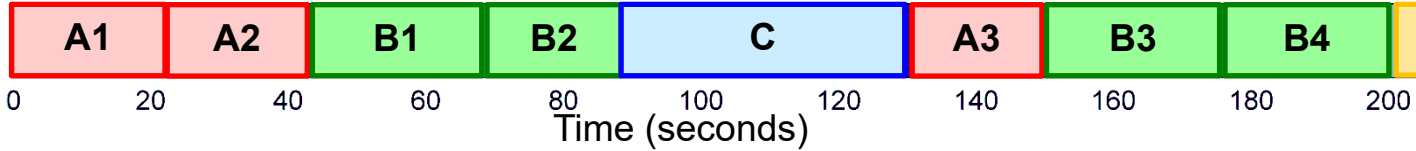
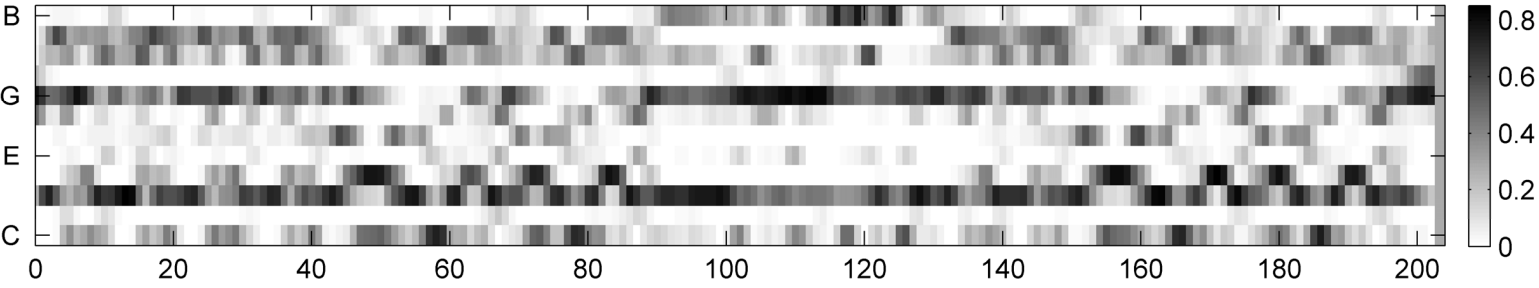


# Feature Representation

**Example:** Brahms Hungarian Dance No. 5 (Ormandy)

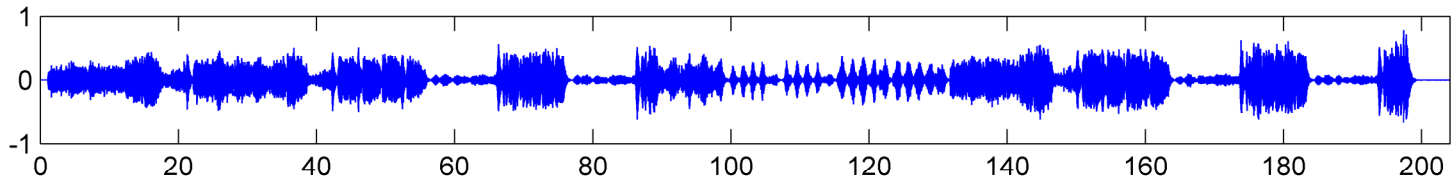


Chroma (Harmony)

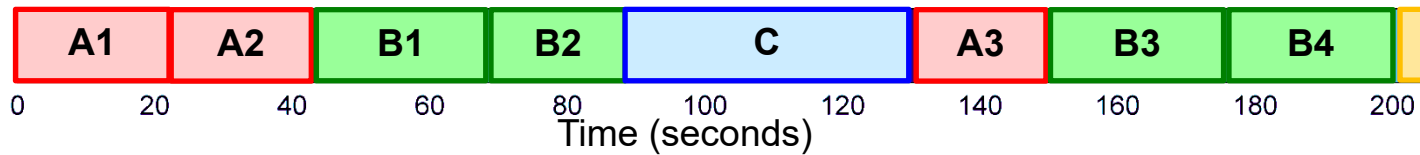
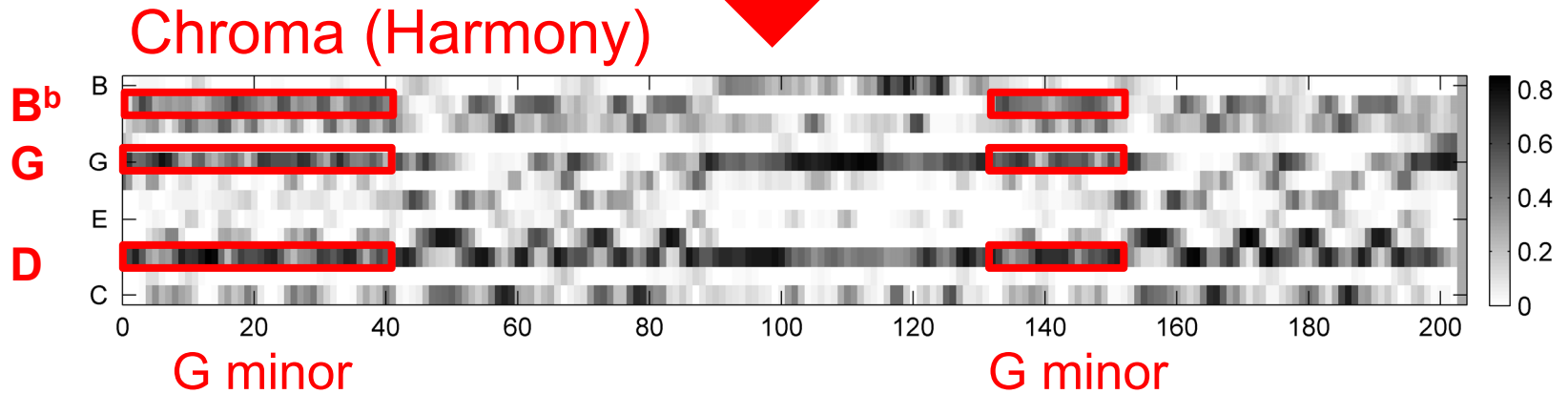


# Feature Representation

**Example:** Brahms Hungarian Dance No. 5 (Ormandy)



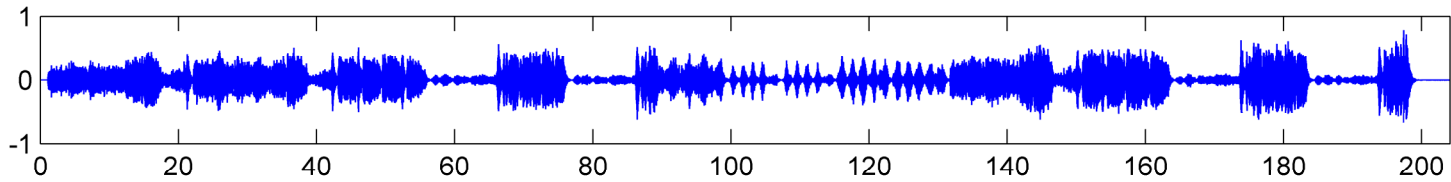
Feature extraction



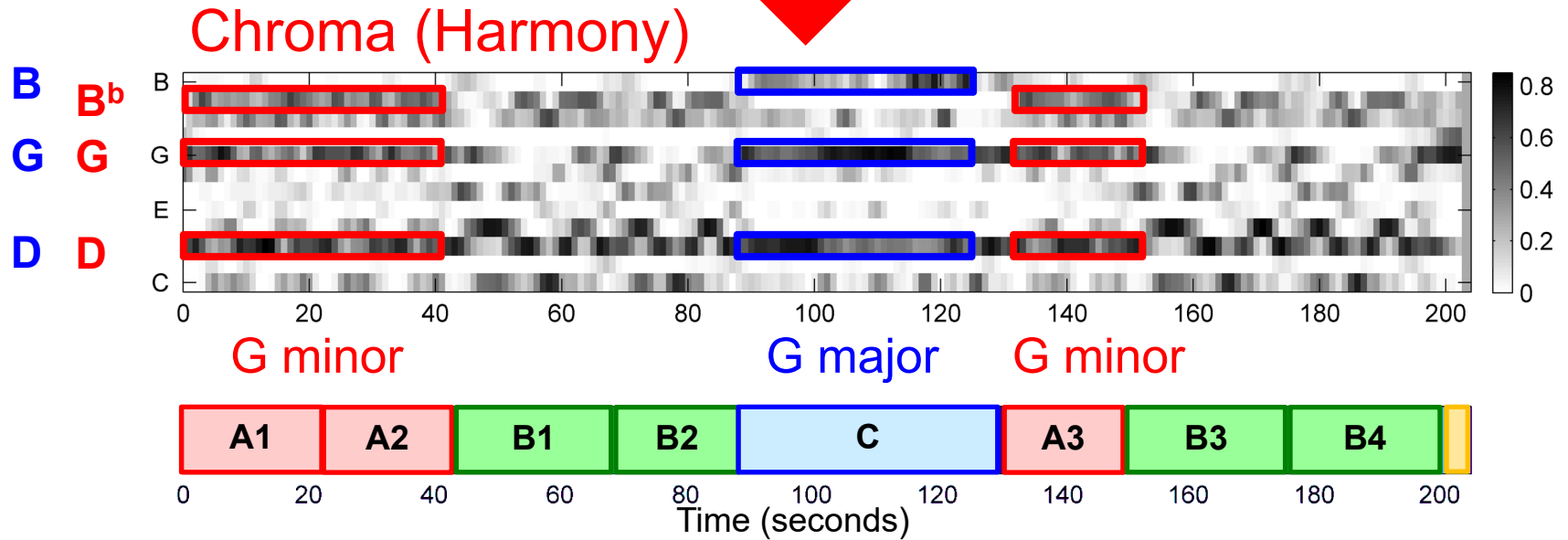


# Feature Representation

**Example:** Brahms Hungarian Dance No. 5 (Ormandy)



Feature extraction



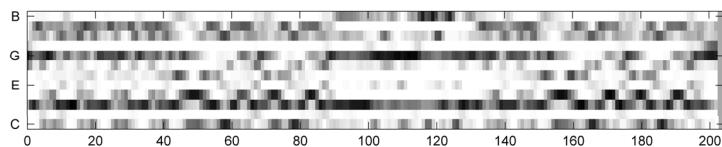
# Self-Similarity Matrix (SSM)

**General idea:** Compare each element of the feature sequence with each other element of the feature sequence based on a suitable similarity measure.

→ Quadratic self-similarity matrix

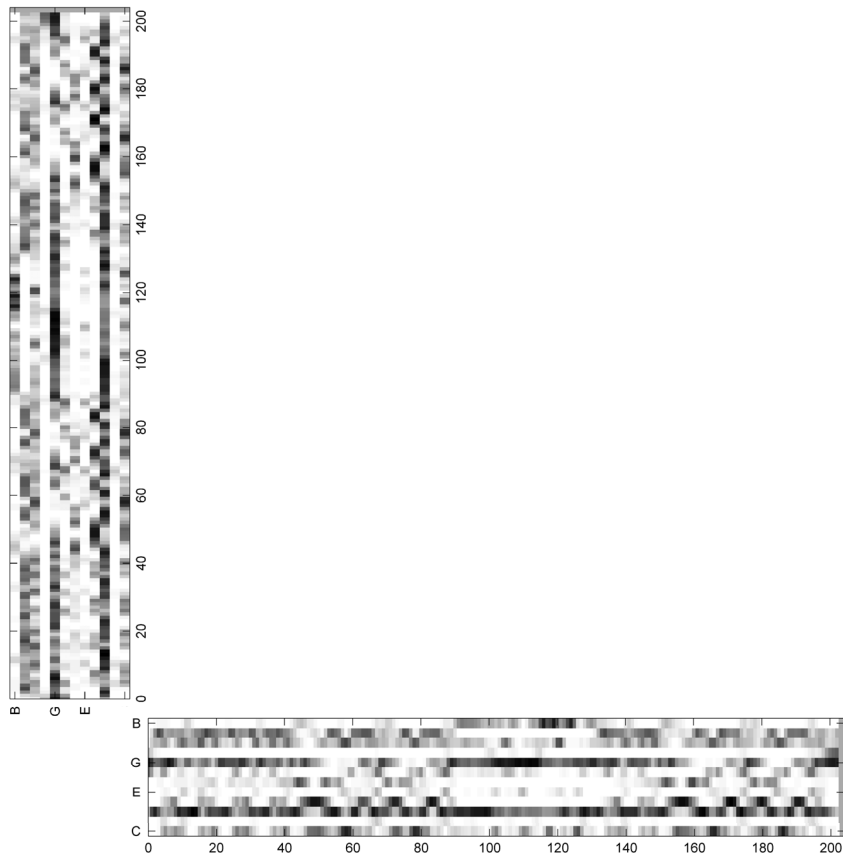
# Self-Similarity Matrix (SSM)

**Example:** Brahms Hungarian Dance No. 5 (Ormandy)



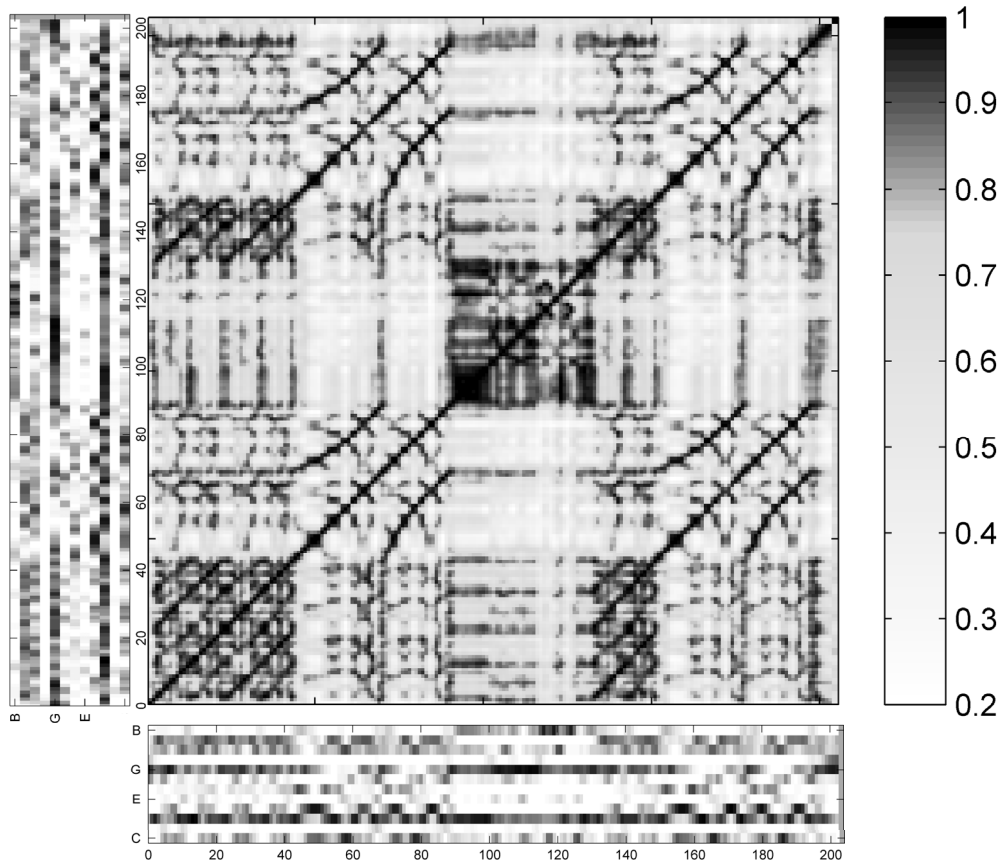
# Self-Similarity Matrix (SSM)

**Example:** Brahms Hungarian Dance No. 5 (Ormandy)



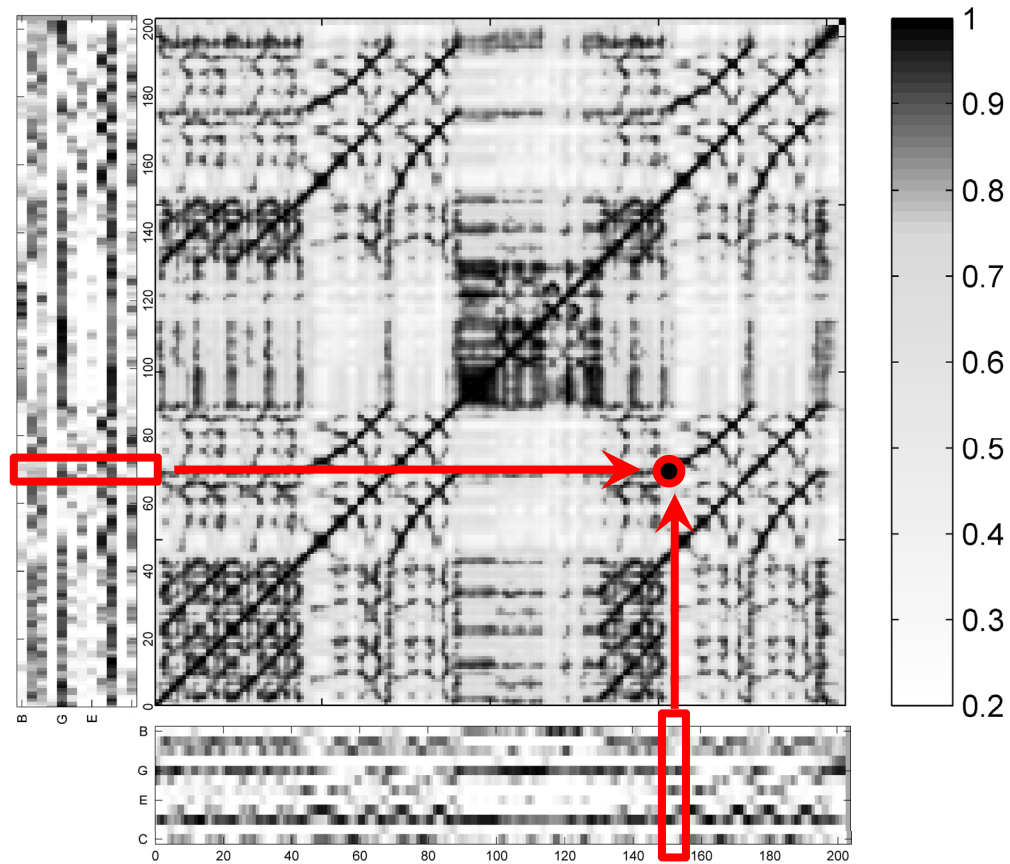
# Self-Similarity Matrix (SSM)

**Example:** Brahms Hungarian Dance No. 5 (Ormandy)



# Self-Similarity Matrix (SSM)

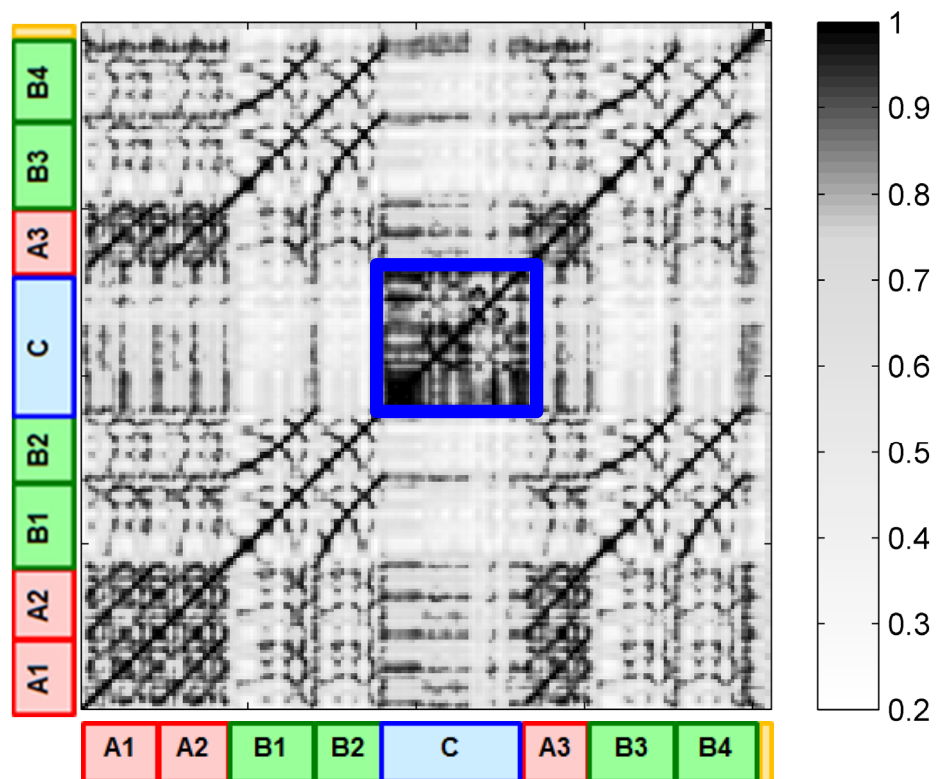
**Example:** Brahms Hungarian Dance No. 5 (Ormandy)





# Self-Similarity Matrix (SSM)

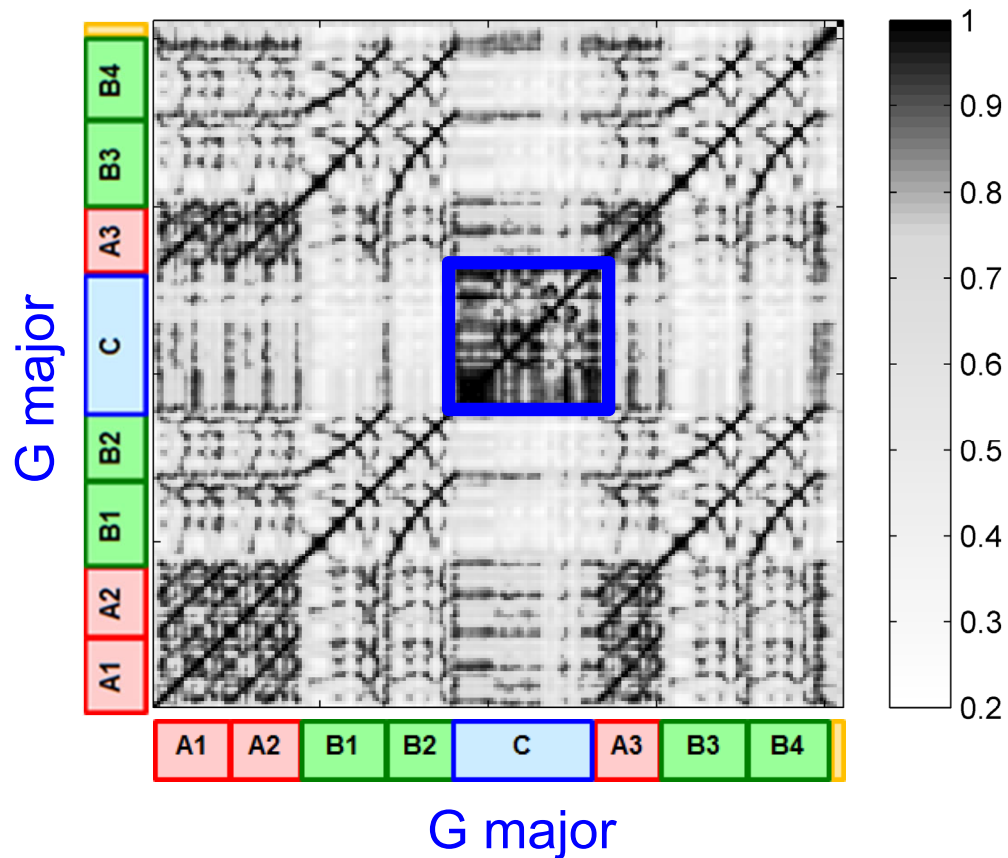
**Example:** Brahms Hungarian Dance No. 5 (Ormandy)





# Self-Similarity Matrix (SSM)

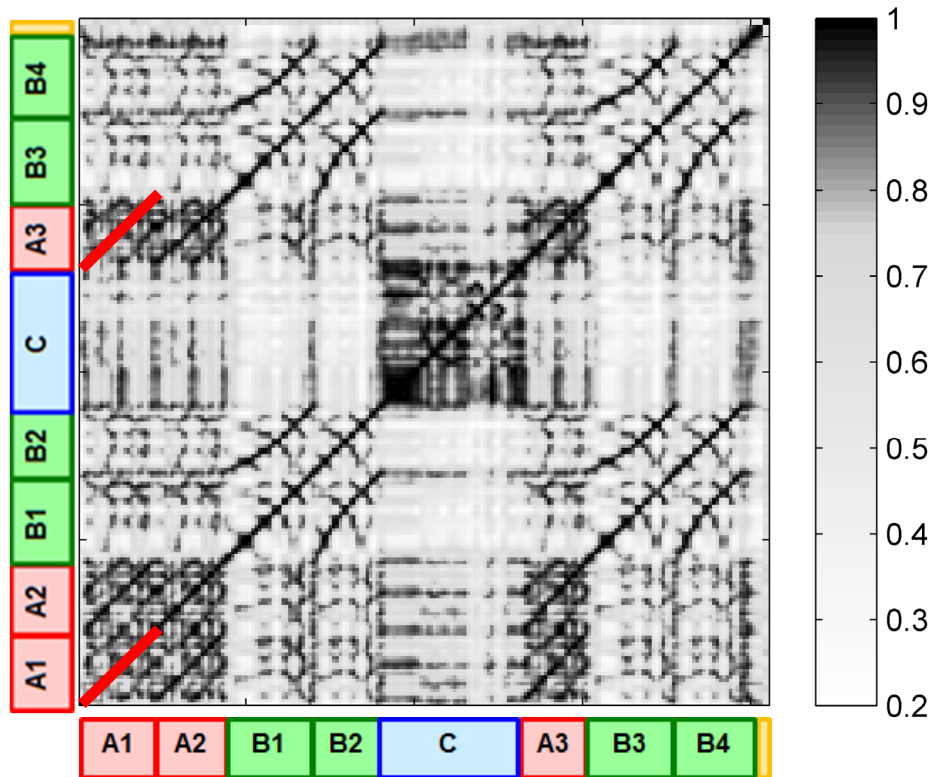
**Example:** Brahms Hungarian Dance No. 5 (Ormandy)





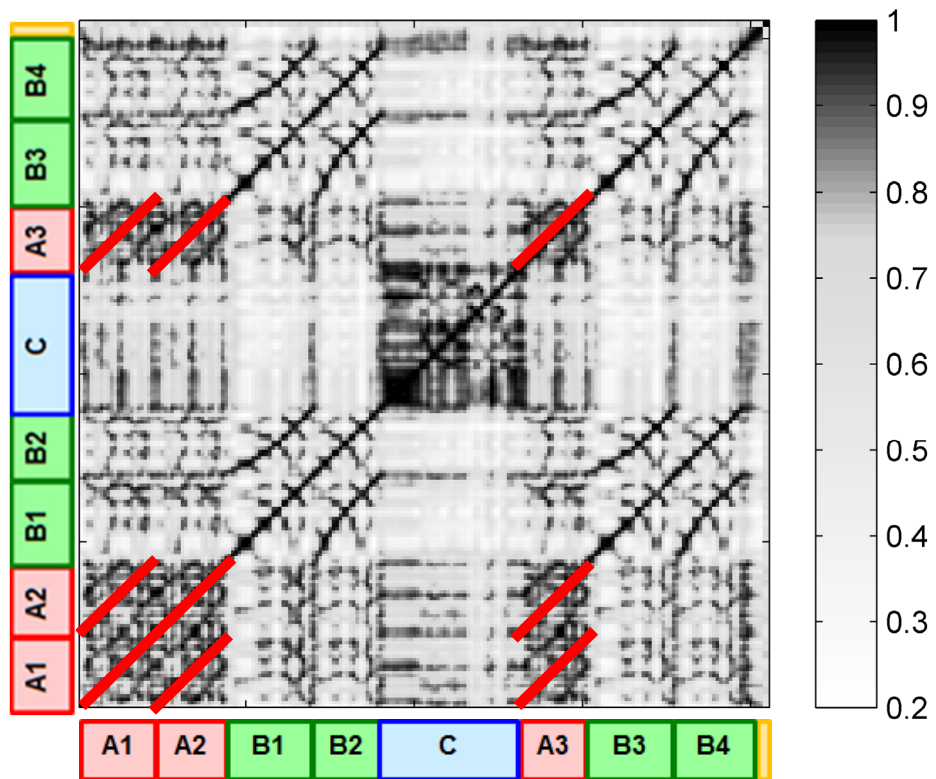
# Self-Similarity Matrix (SSM)

**Example:** Brahms Hungarian Dance No. 5 (Ormandy)



# Self-Similarity Matrix (SSM)

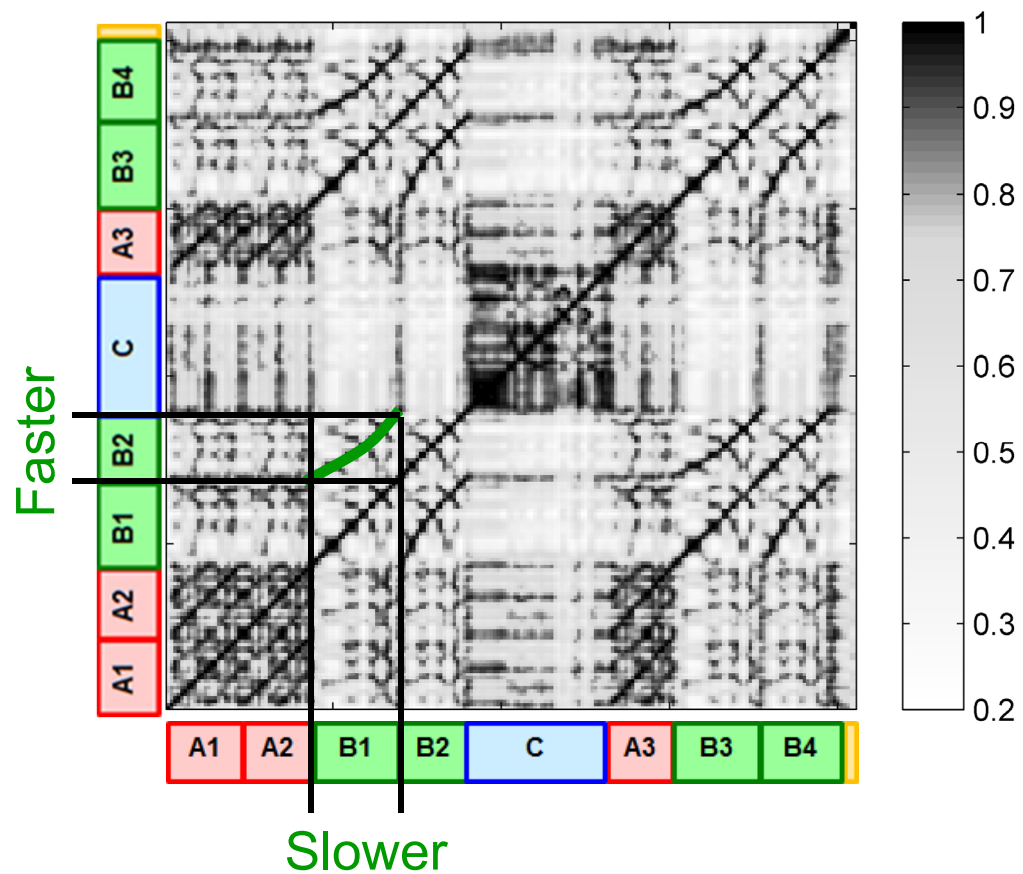
**Example:** Brahms Hungarian Dance No. 5 (Ormandy)





# Self-Similarity Matrix (SSM)

**Example:** Brahms Hungarian Dance No. 5 (Ormandy)









# Self-Similarity Matrix (SSM)

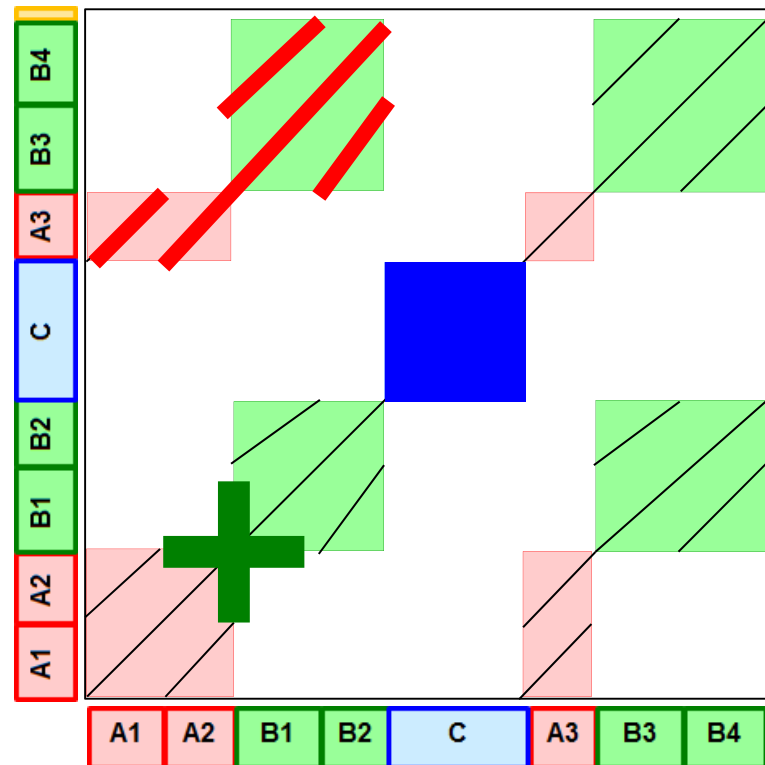
**Example:** Brahms Hungarian Dance No. 5 (Ormandy)

**Blocks:** Homogeneity

**Paths:** Repetition

**Corners:** Novelty

Idealized SSM



# SSM Enhancement

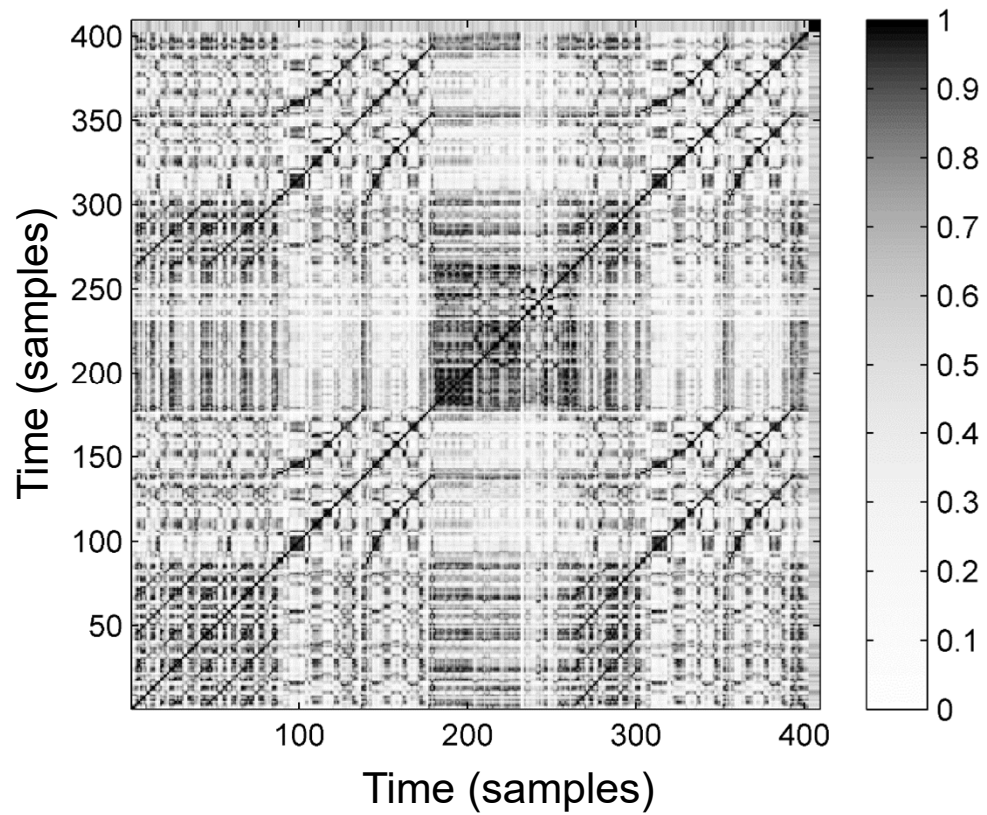
Challenge: Presence of musical variations

- Fragmented paths and gaps
- Paths of poor quality
- Regions of constant (low) cost
- Curved paths

Idea: Enhancement of path structure

# SSM Enhancement

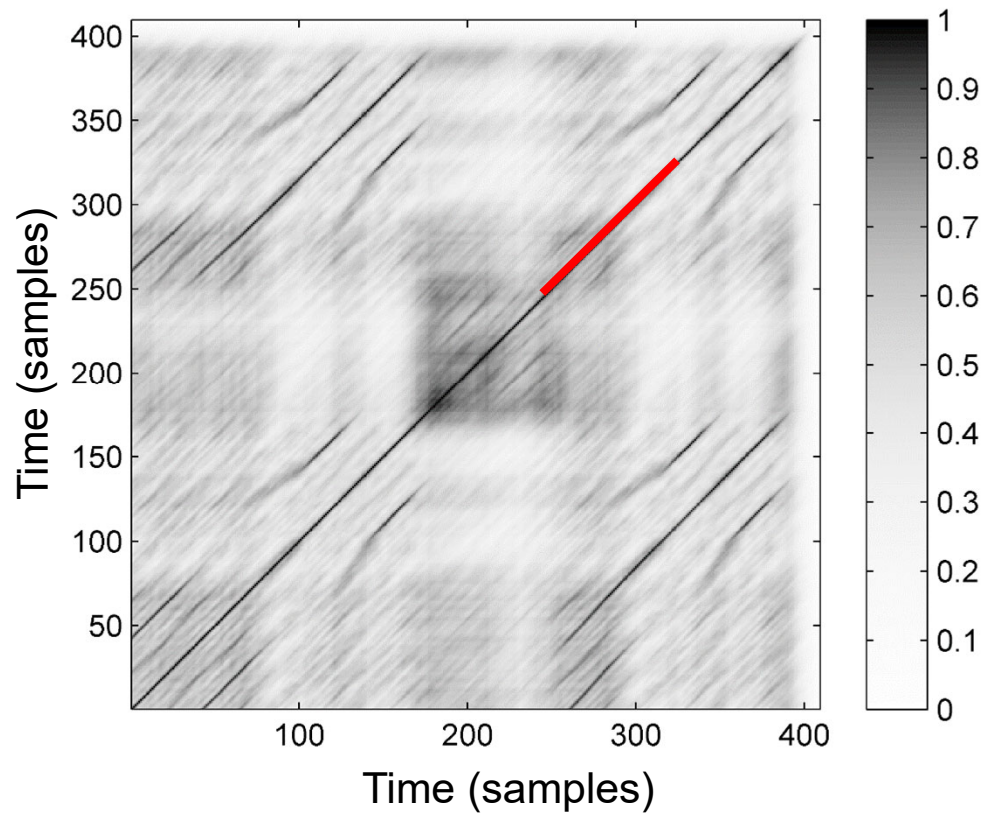
Path Enhancement



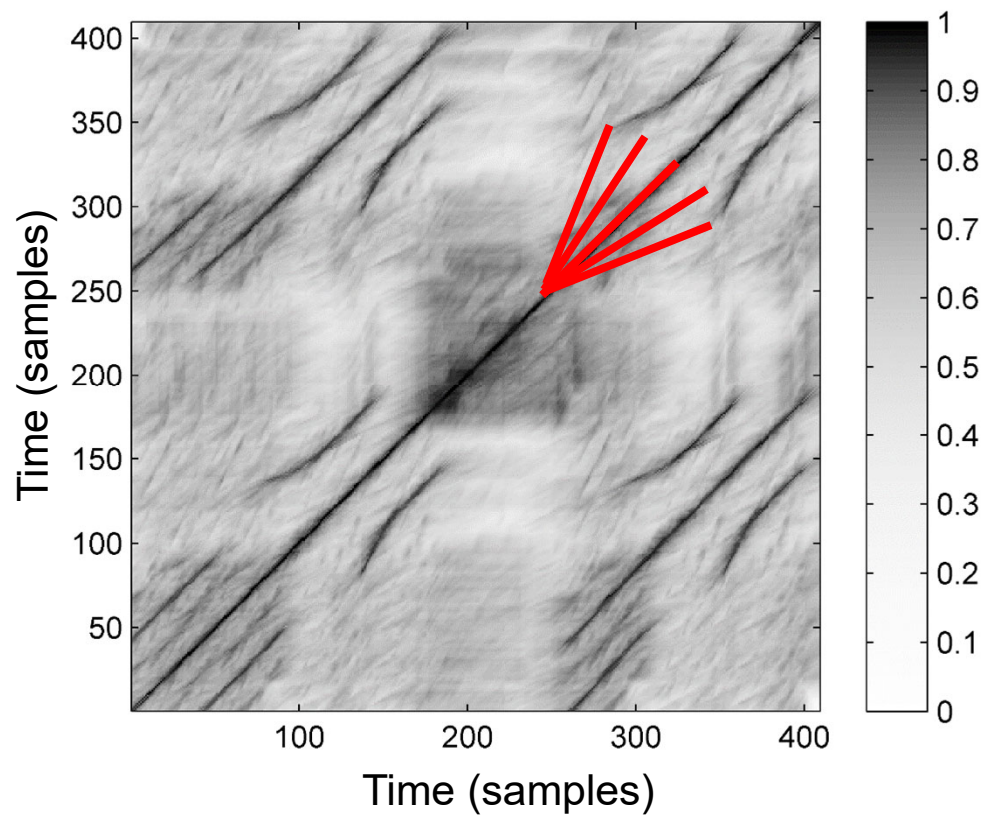
# SSM Enhancement

## Path Enhancement

- Diagonal smoothing



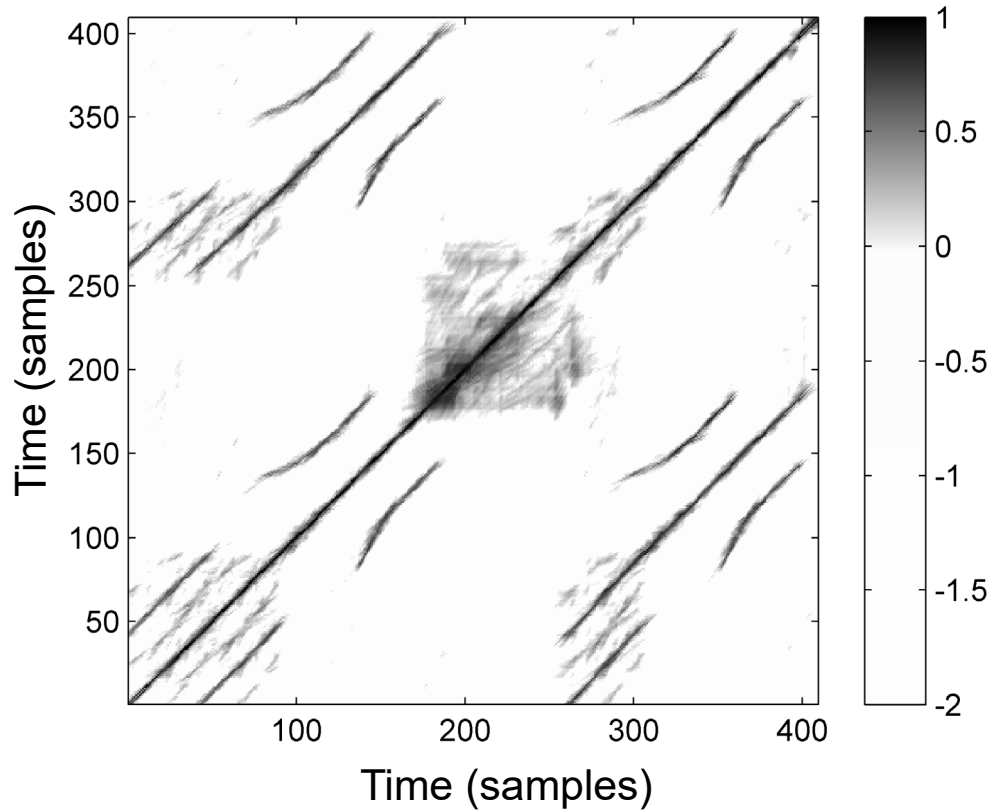
# SSM Enhancement



## Path Enhancement

- Diagonal smoothing
- Multiple filtering

# SSM Enhancement



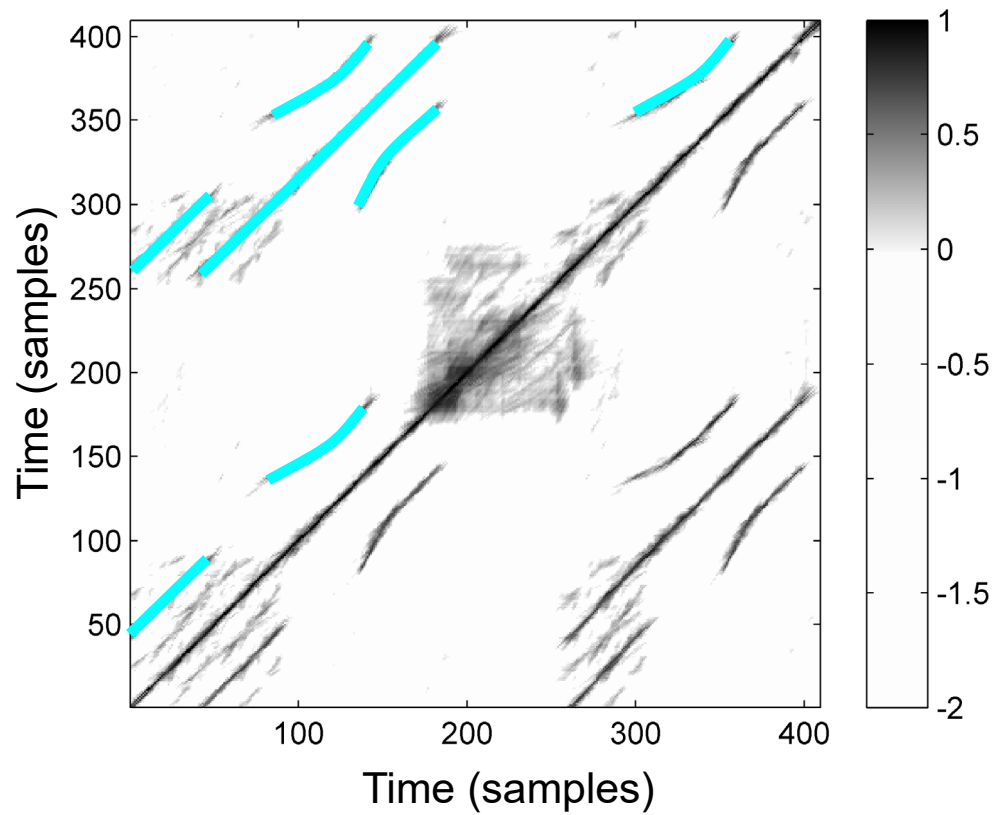
## Path Enhancement

- Diagonal smoothing
- Multiple filtering
- Thresholding (relative)
- Scaling & penalty

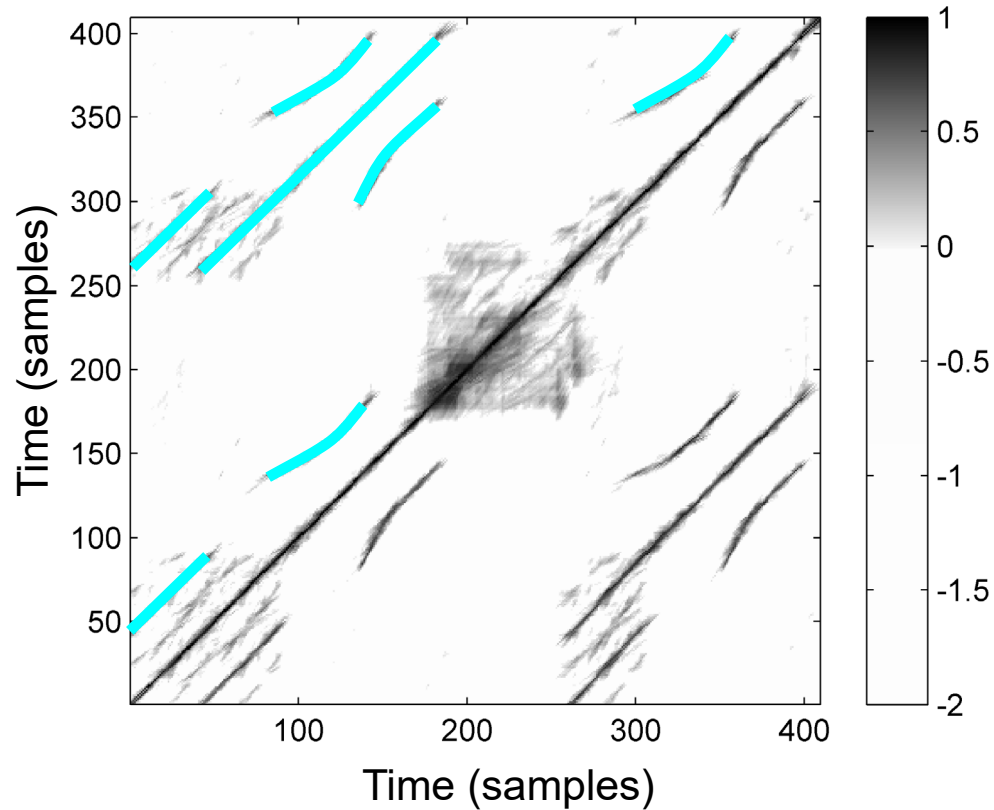
# SSM Enhancement

## Further Processing

- Path extraction

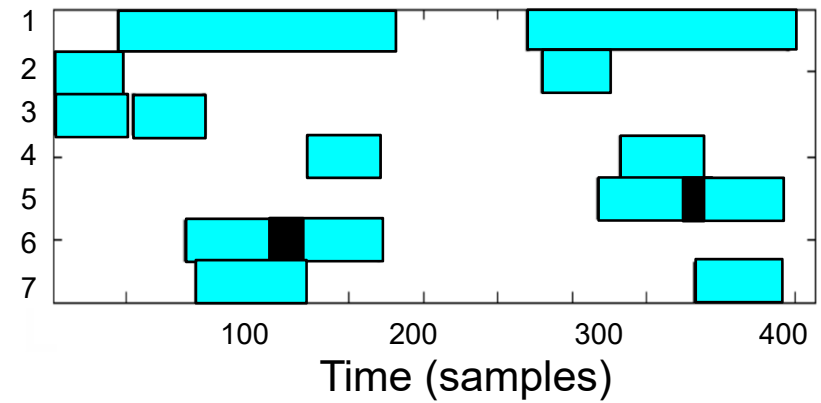


# SSM Enhancement



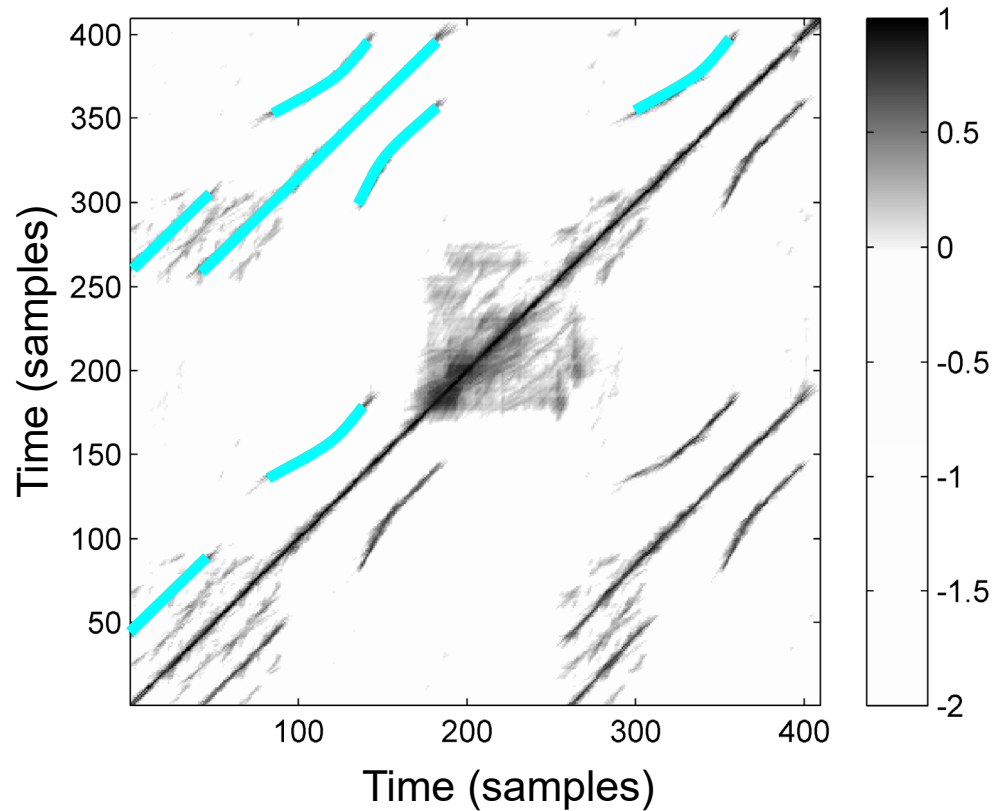
## Further Processing

- Path extraction
- Pairwise relations



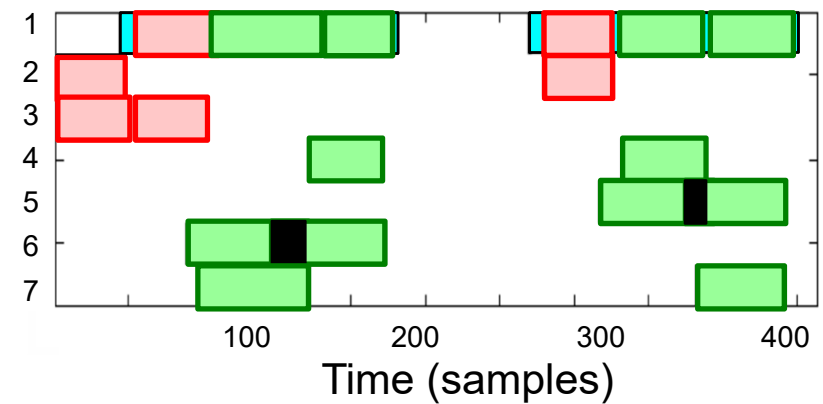


# SSM Enhancement

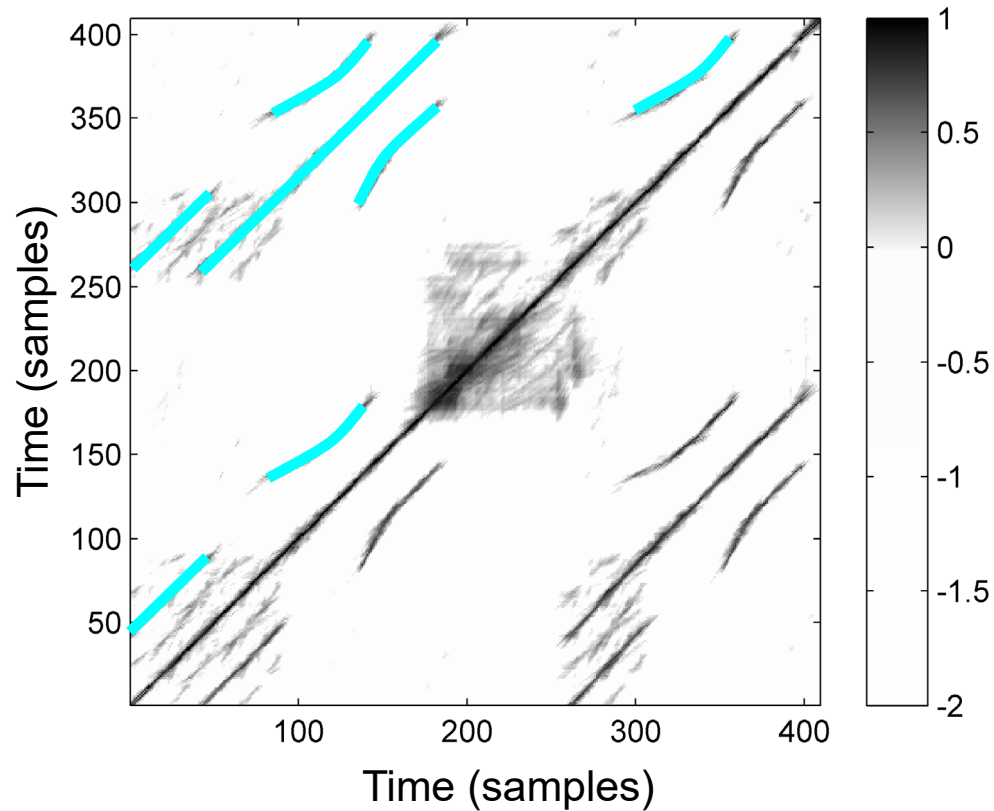


## Further Processing

- Path extraction
- Pairwise relations
- Grouping (transitivity)

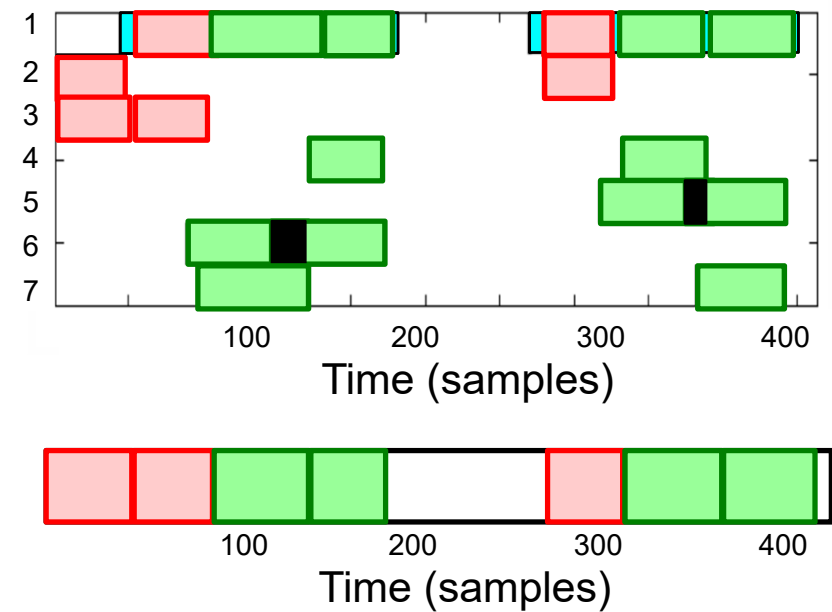


# SSM Enhancement



## Further Processing

- Path extraction
- Pairwise relations
- Grouping (transitivity)



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# Novelty-Based Segmentation

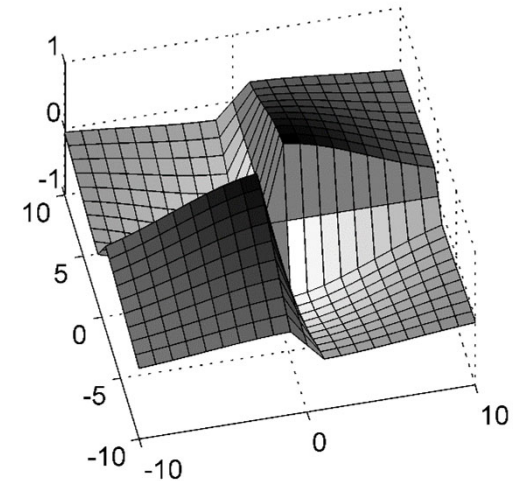
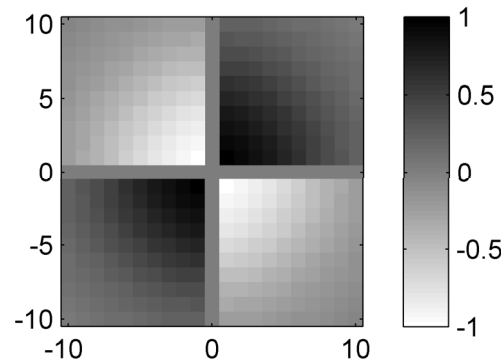
# Novelty-Based Segmentation

## General goals:

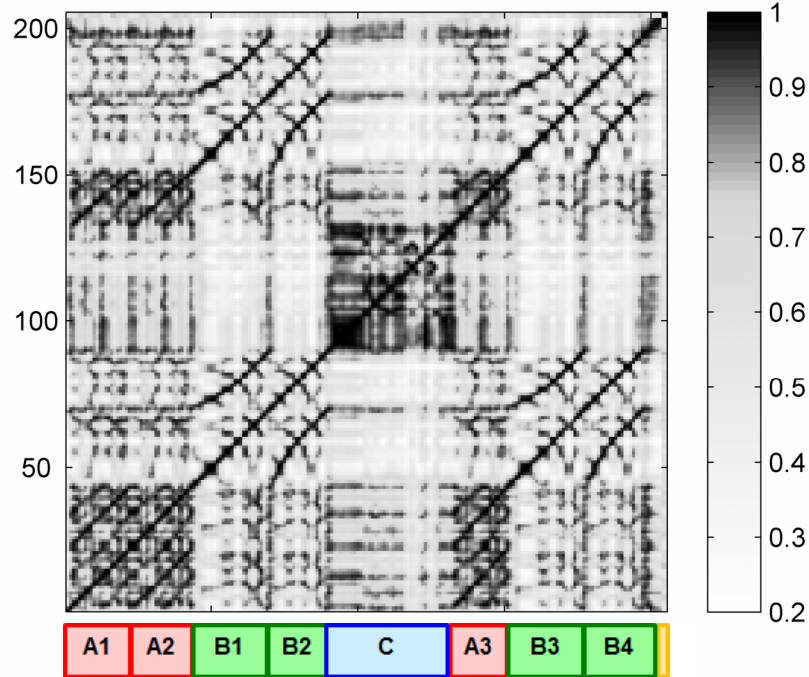
- Find instances where musical changes occur.
- Find transition between subsequent musical parts.

## Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.



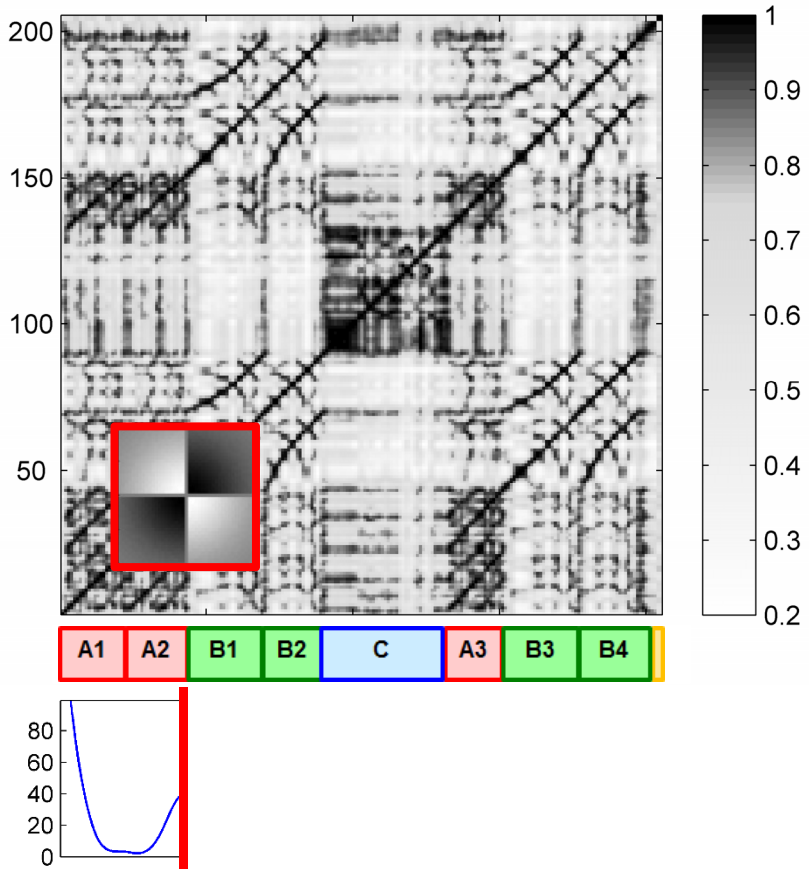
# Novelty-Based Segmentation



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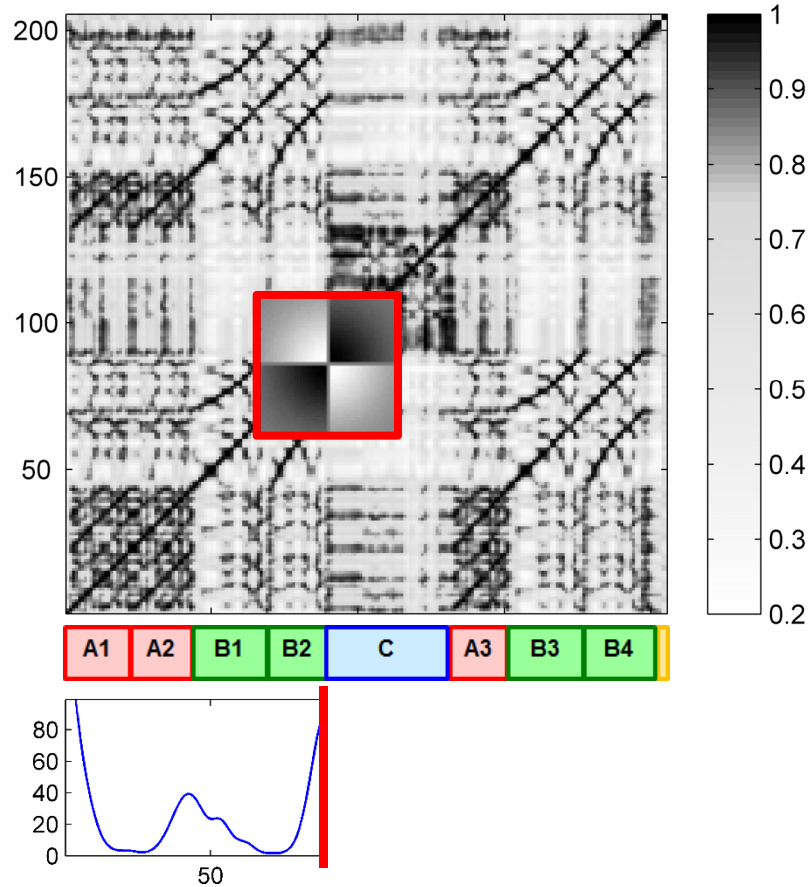
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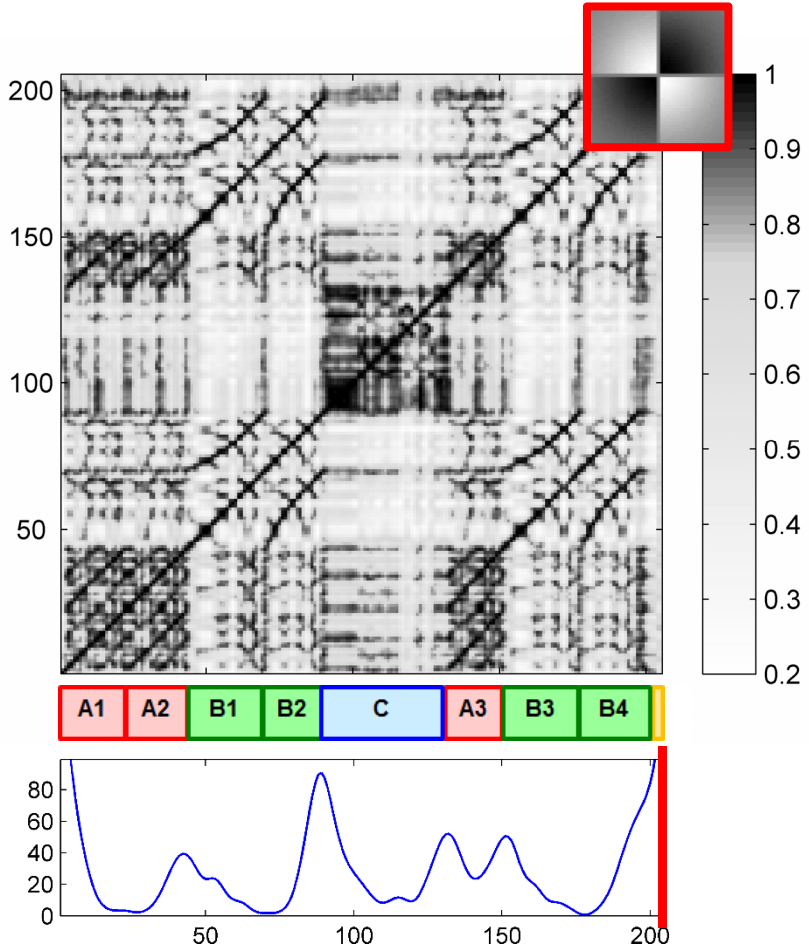
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# Novelty-Based Segmentation

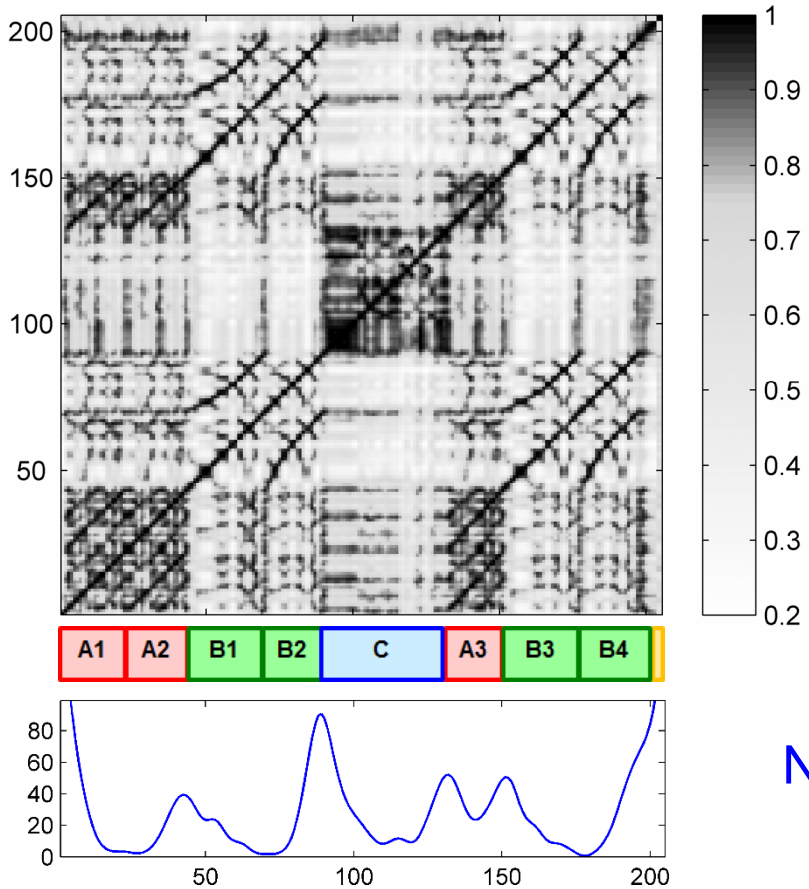


## Idea (Foote):

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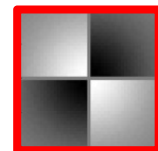
# Novelty-Based Segmentation



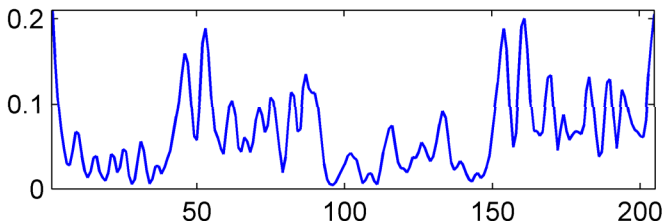
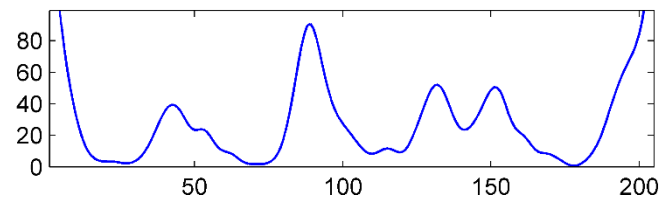
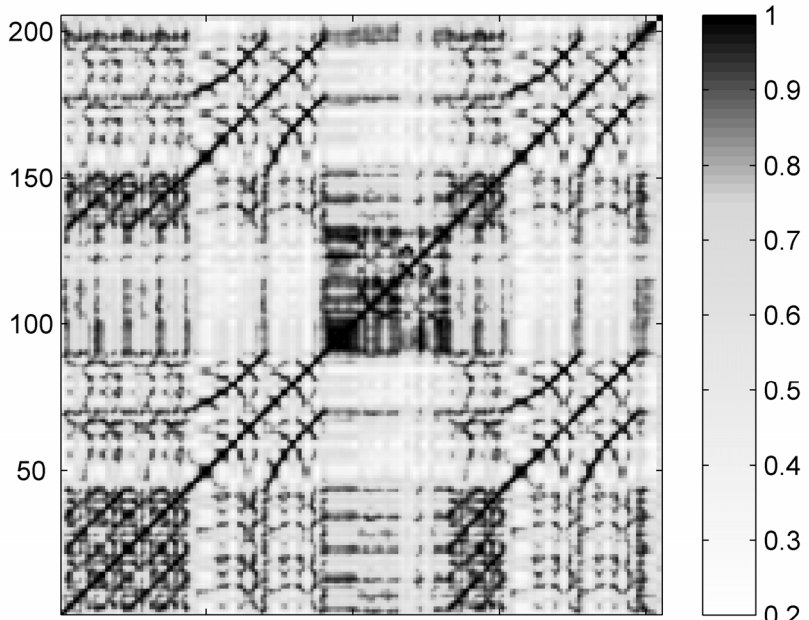
## Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.

Novelty function using



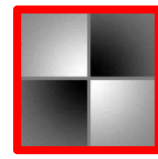
# Novelty-Based Segmentation



## Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.

Novelty function using



Novelty function using



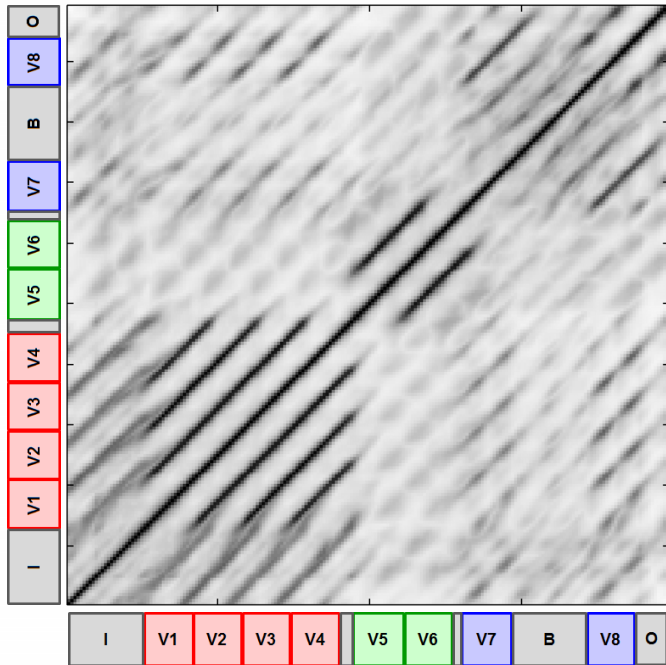




# SSM Enhancement

**Example:** Zager & Evans “In The Year 2525”

Missing relations because of transposed sections

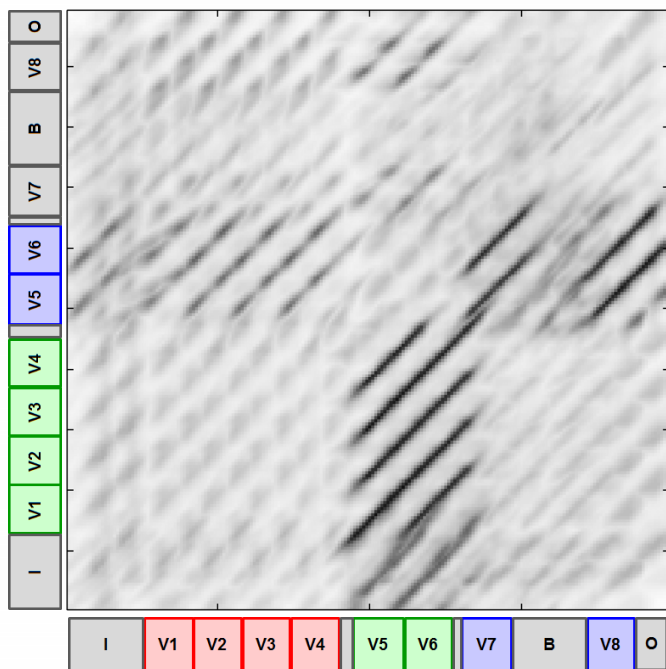


# SSM Enhancement

**Example:** Zager & Evans “In The Year 2525”

**Idea:** Cyclic shift of one of the chroma sequences

**One semitone up**

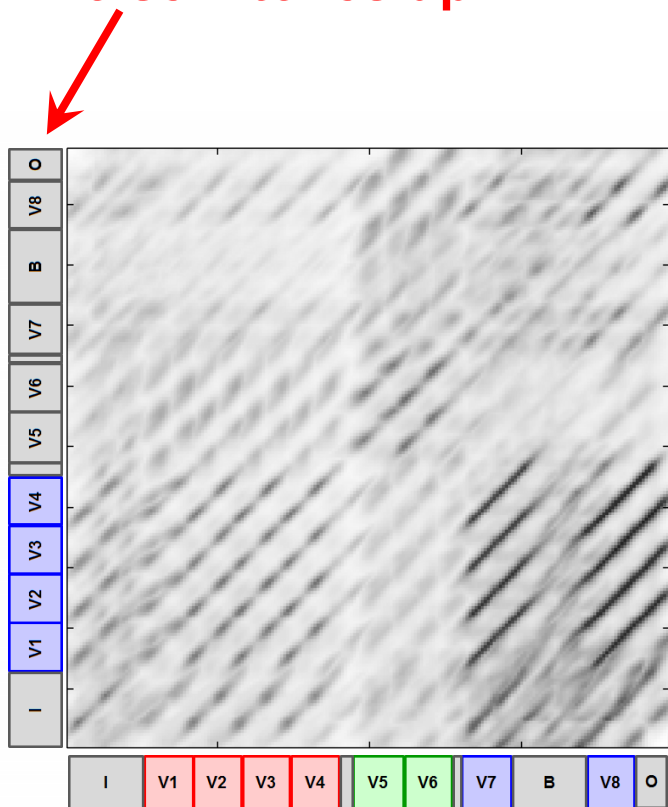


# SSM Enhancement

**Example:** Zager & Evans “In The Year 2525”

Idea: Cyclic shift of one of the chroma sequences

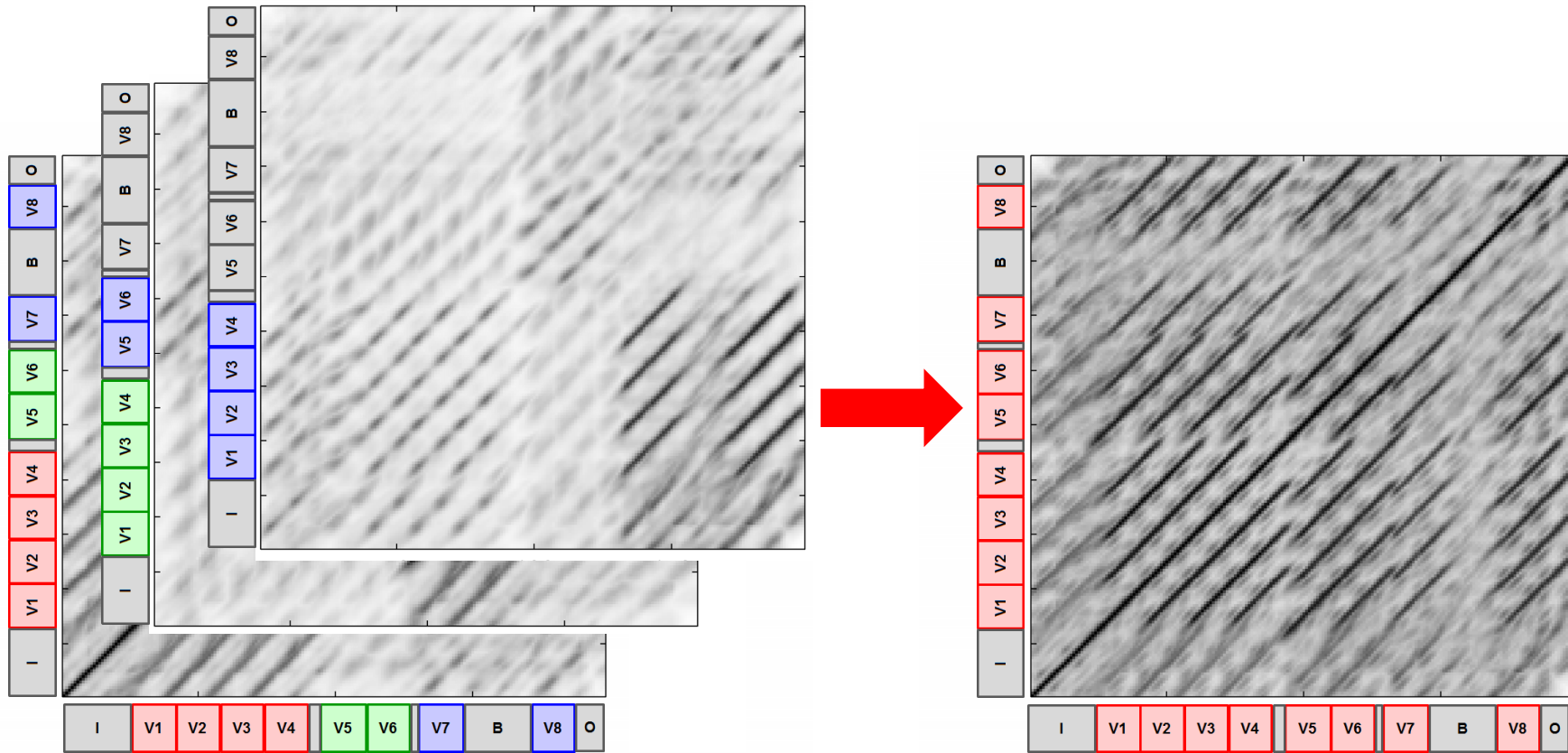
Two semitones up



# SSM Enhancement

**Example:** Zager & Evans “In The Year 2525”

**Idea:** Overlay & Maximize  $\longrightarrow$  Transposition-invariant SSM





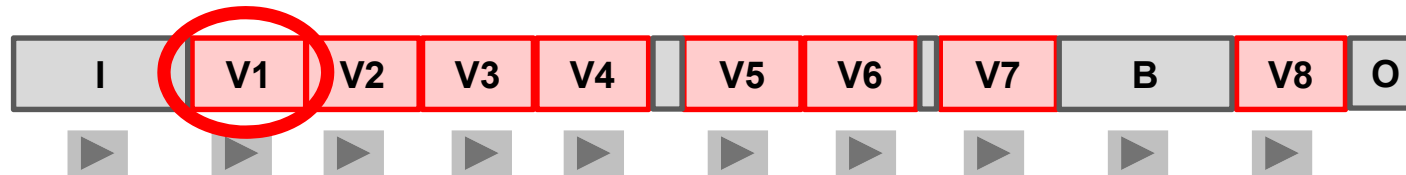
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# Audio Thumbnailing

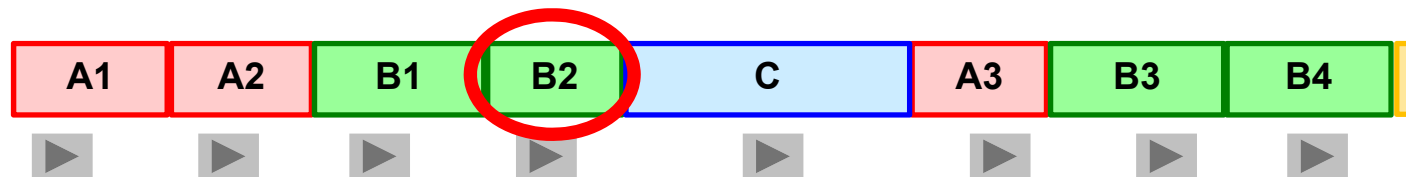
# Audio Thumbnailing

**General goal:** Determine the most representative section (“Thumbnail”) of a given music recording.

**Example:** Zager & Evans “In The Year 2525”



**Example:** Brahms Hungarian Dance No. 5 (Ormandy)



Thumbnail is often assumed to be the most repetitive segment

# Audio Thumbnailing

## Two steps

1. Path extraction

2. Grouping

## Both steps are problematic!

- Paths of poor quality (fragmented, gaps)
- Block-like structures
- Curved paths
- Noisy relations (missing, distorted, overlapping)
- Transitivity computation difficult

## Main idea: Do both, path extraction and grouping, jointly

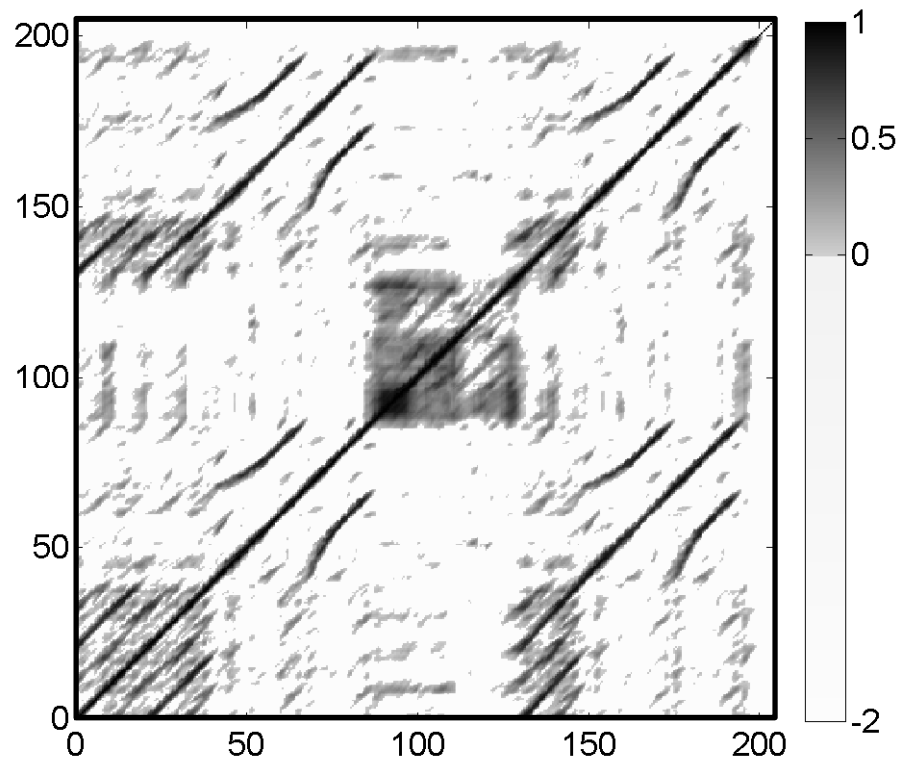
- One optimization scheme for both steps
- Stabilizing effect
- Efficient

# Audio Thumbnailing

Main idea: Do both path extraction and grouping jointly

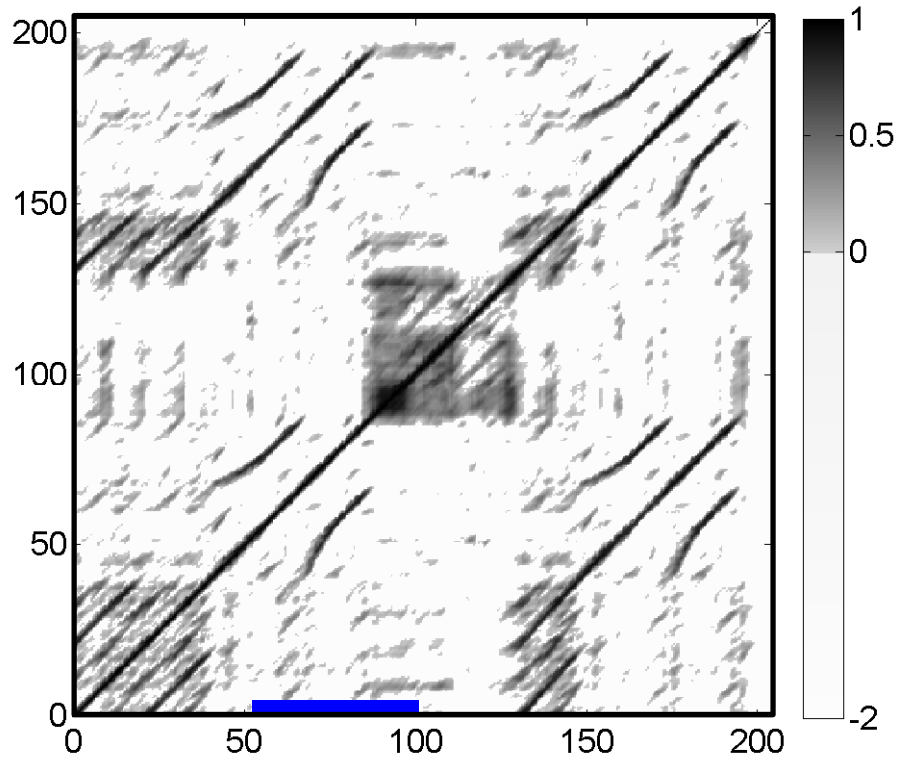
- For each audio **segment** we define a **fitness** value
- This fitness value expresses “how well” the segment explains the entire audio recording
- The segment with the highest fitness value is considered to be the **thumbnail**
- As main technical concept we introduce the notion of a **path family**

# Fitness Measure



Enhanced SSM

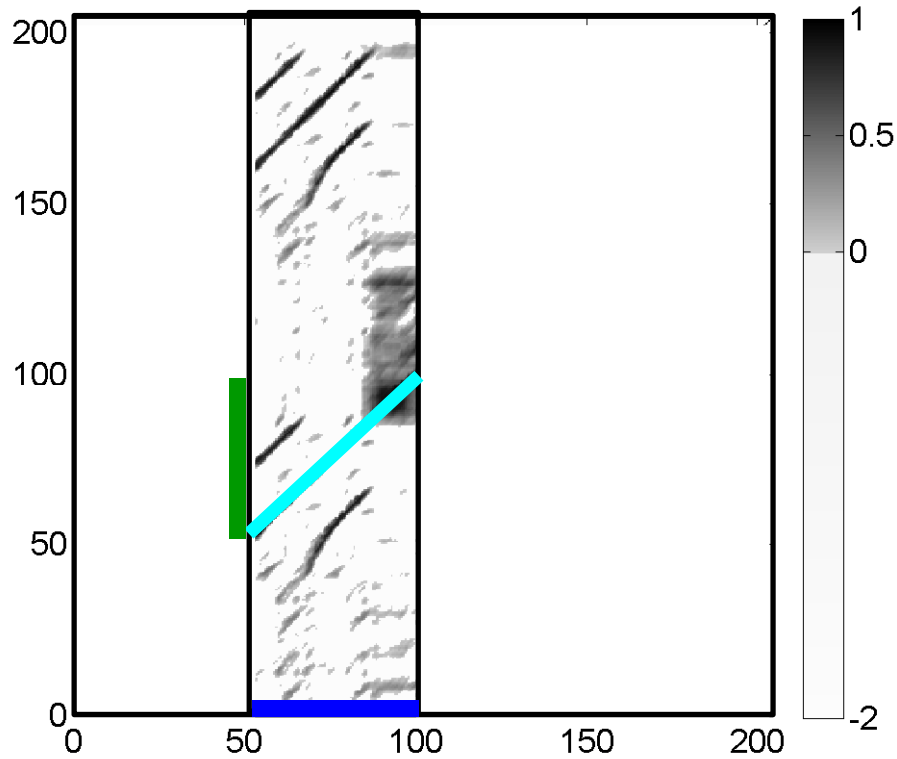
# Fitness Measure



## Path over segment

- Consider a fixed **segment**

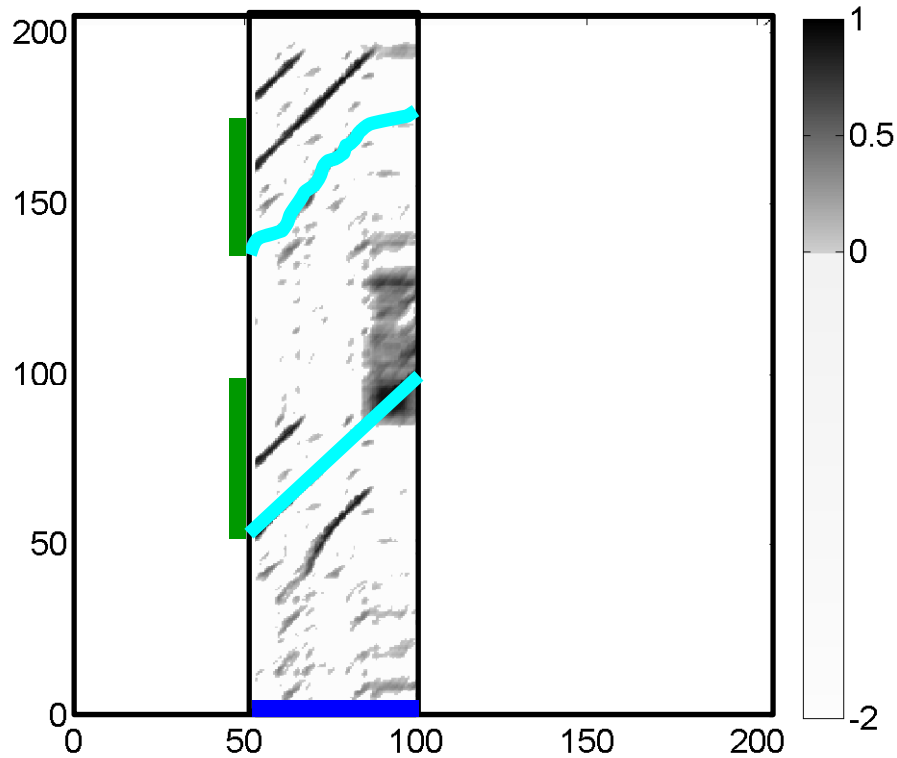
# Fitness Measure



## Path over segment

- Consider a fixed **segment**
- **Path** over **segment**
- **Induced segment**
- Score is high

# Fitness Measure

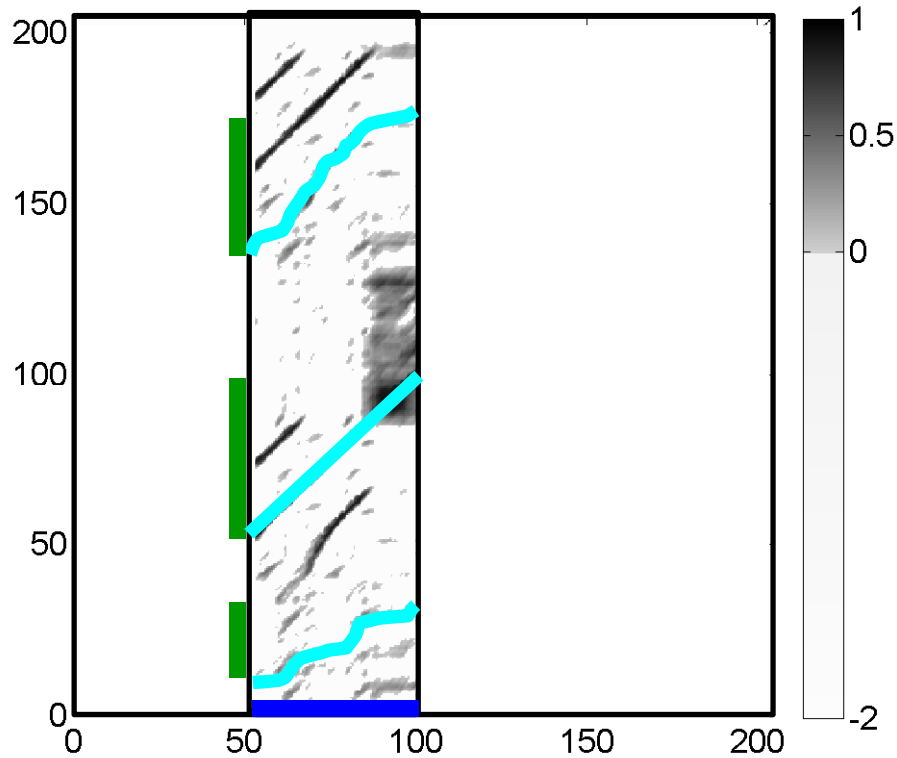


## Path over segment

- Consider a fixed **segment**
- **Path** over **segment**
- **Induced segment**
- Score is high
  
- **A second path** over **segment**
- **Induced segment**
- Score is not so high



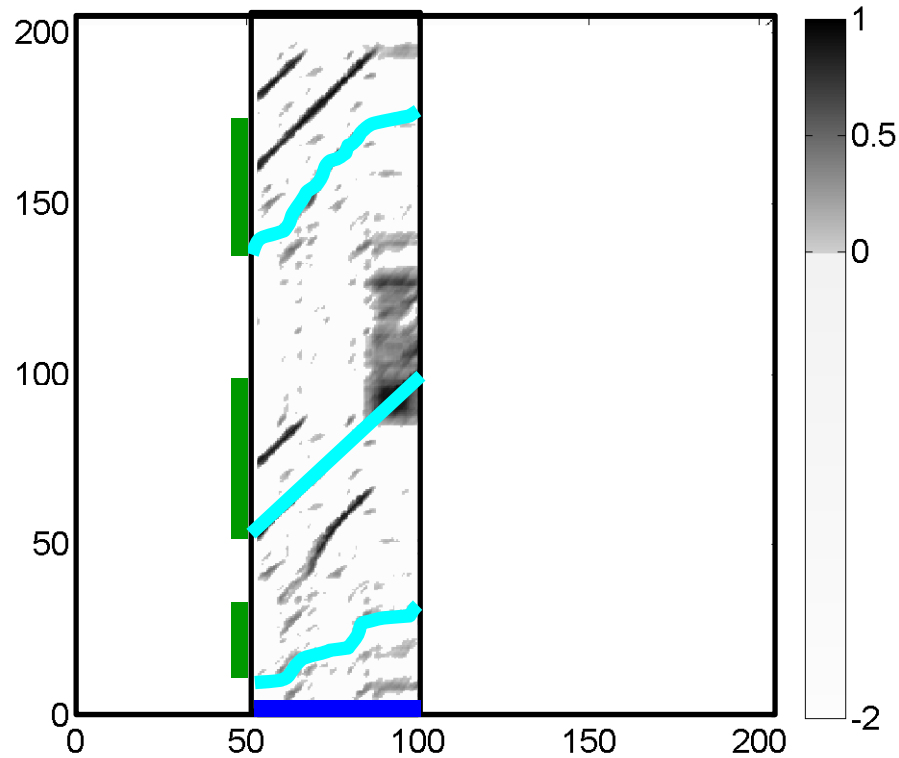
# Fitness Measure



## Path over segment

- Consider a fixed **segment**
- **Path** over **segment**
- **Induced segment**
- Score is high
  
- **A second path** over **segment**
- **Induced segment**
- Score is not so high
  
- **A third path** over **segment**
- **Induced segment**
- Score is very low

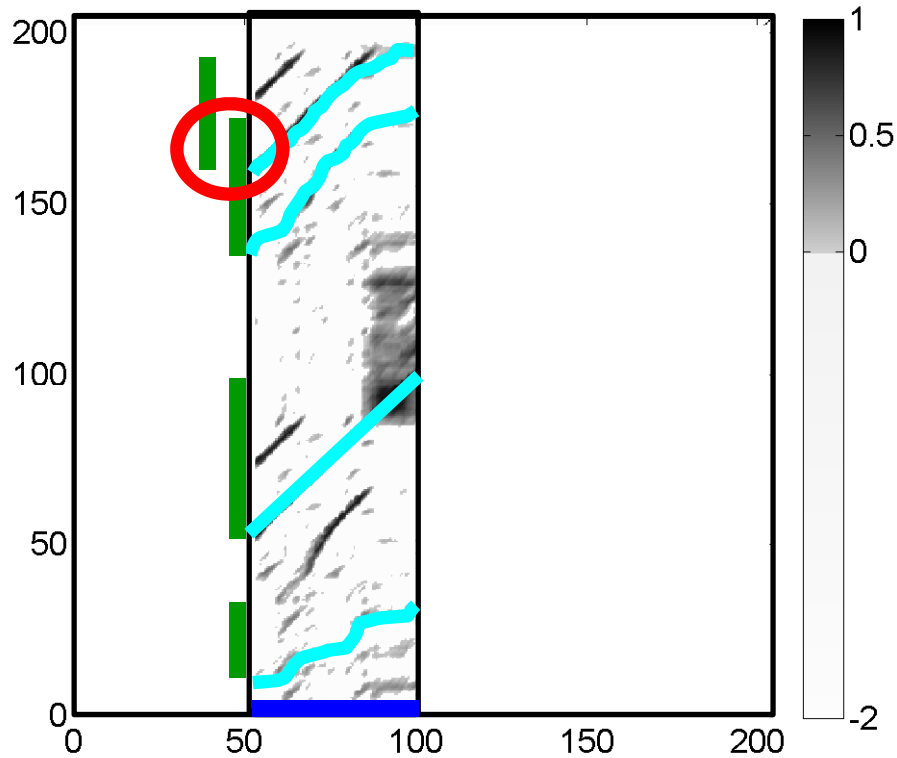
# Fitness Measure



## Path family

- Consider a fixed **segment**
- A path family over a **segment** is a family of paths such that the **induced segments** do **not overlap**.

# Fitness Measure

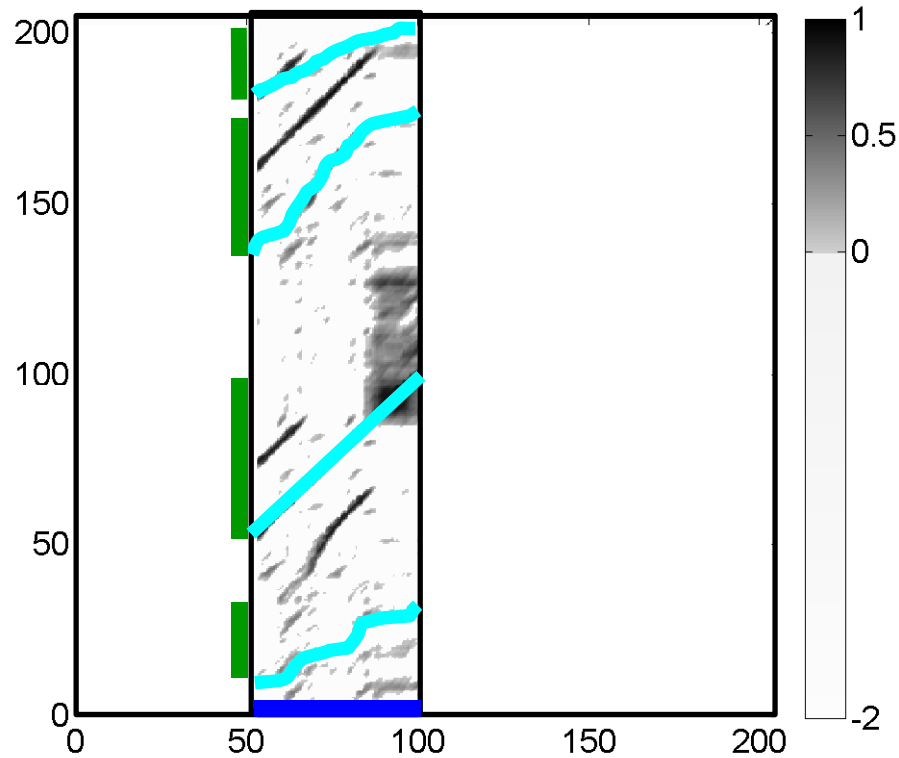


## Path family

- Consider a fixed **segment**
- A path family over a **segment** is a family of paths such that the **induced segments** do **not overlap**.

This is **not** a path family!

# Fitness Measure



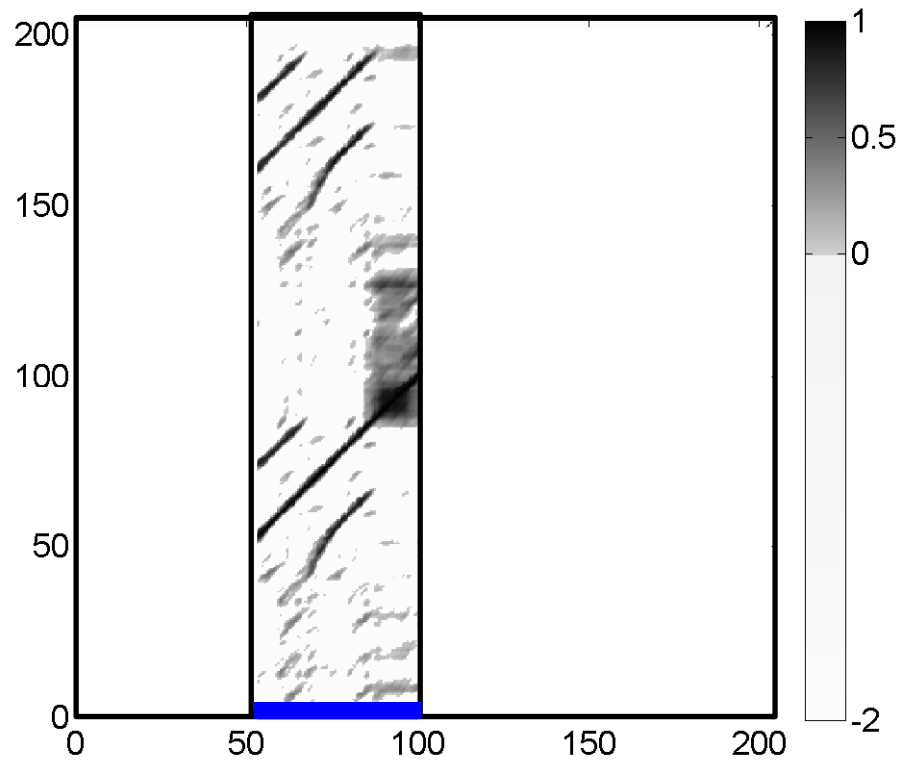
## Path family

- Consider a fixed **segment**
- A path family over a **segment** is a family of paths such that the **induced segments** do **not overlap**.

This is a path family!

(Even though not a good one)

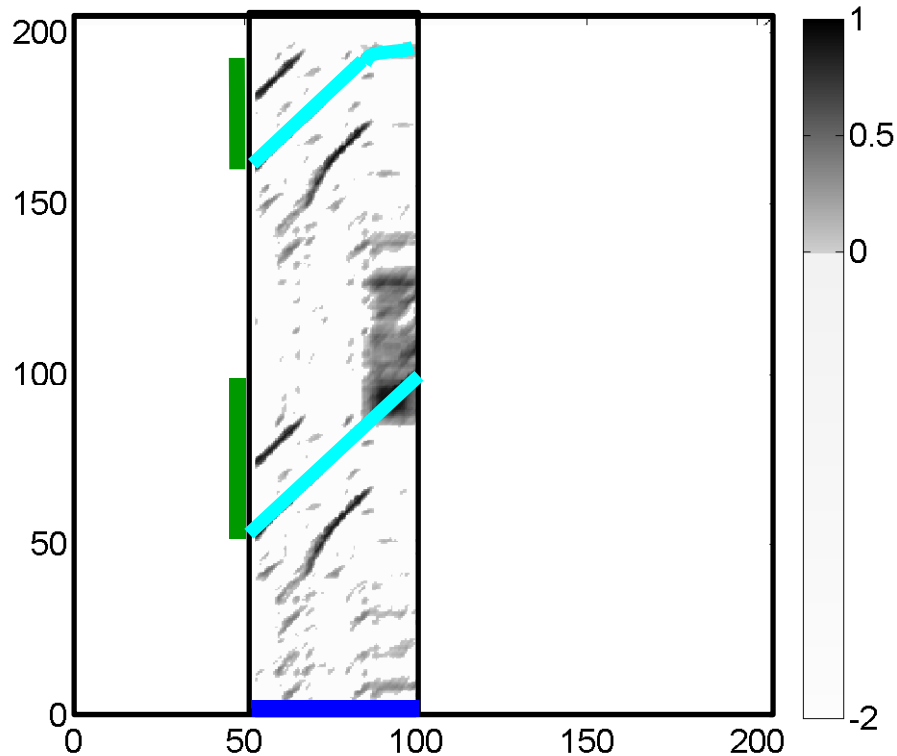
# Fitness Measure



## Optimal path family

- Consider a fixed **segment**

# Fitness Measure

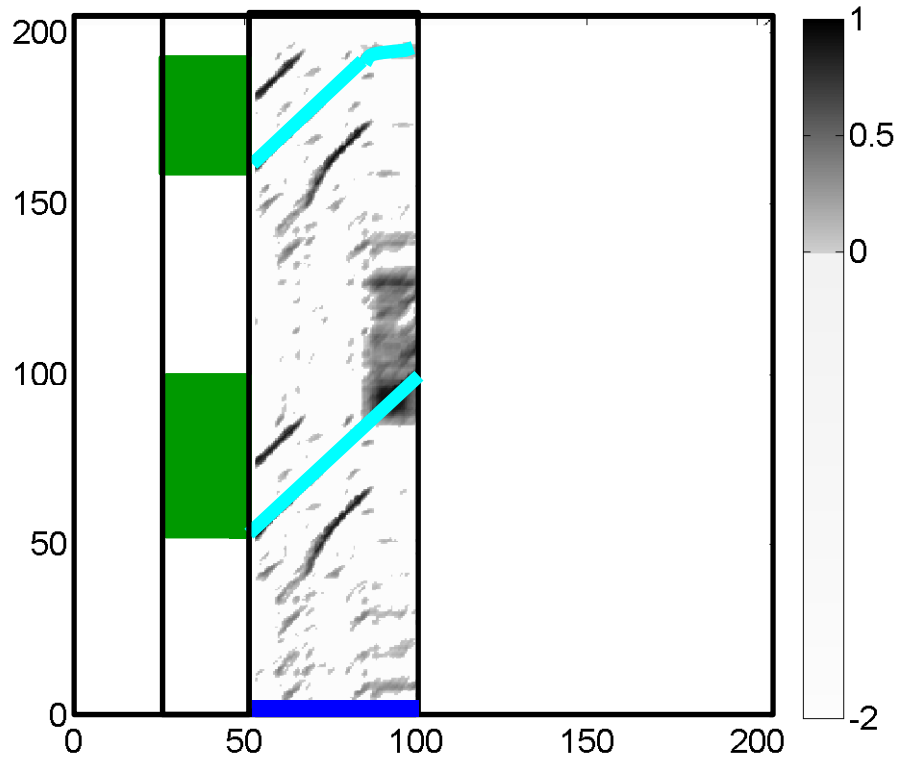


## Optimal path family

- Consider a fixed **segment**
- Consider over the **segment** the **optimal path family**, i.e., the path family having maximal overall score.
- Call this value:  
**Score(segment)**

Note: This optimal path family can be computed using dynamic programming.

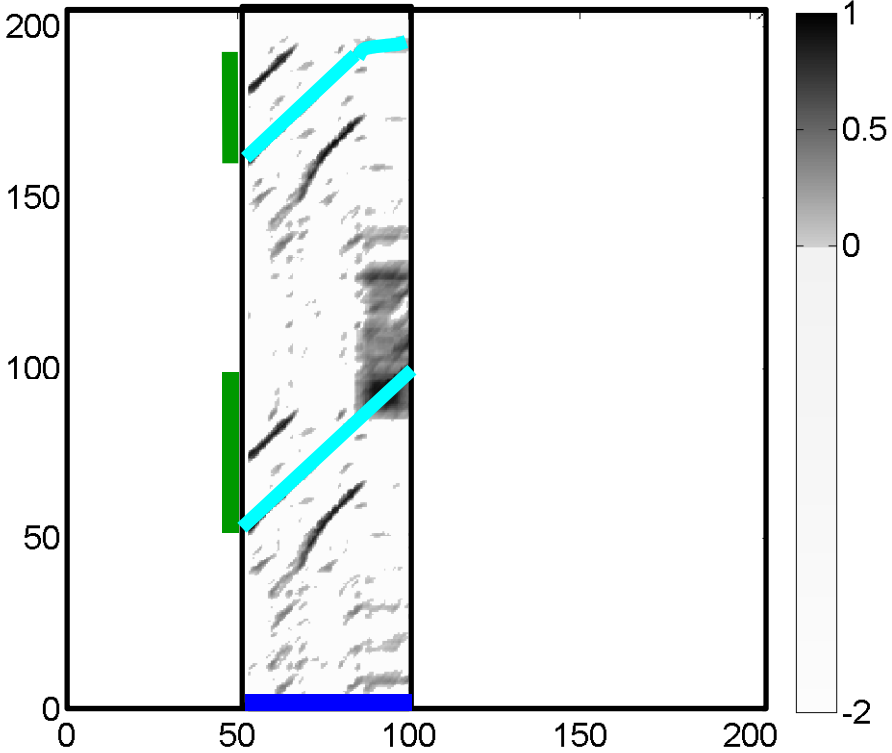
# Fitness Measure



## Optimal path family

- Consider a fixed **segment**
- Consider over the **segment** the **optimal path family**, i.e., the path family having maximal overall score.
- Call this value:  
 $\text{Score}(\text{segment})$
- Furthermore consider the amount covered by the **induced segments**.
- Call this value:  
 $\text{Coverage}(\text{segment})$

# Fitness Measure



## Fitness

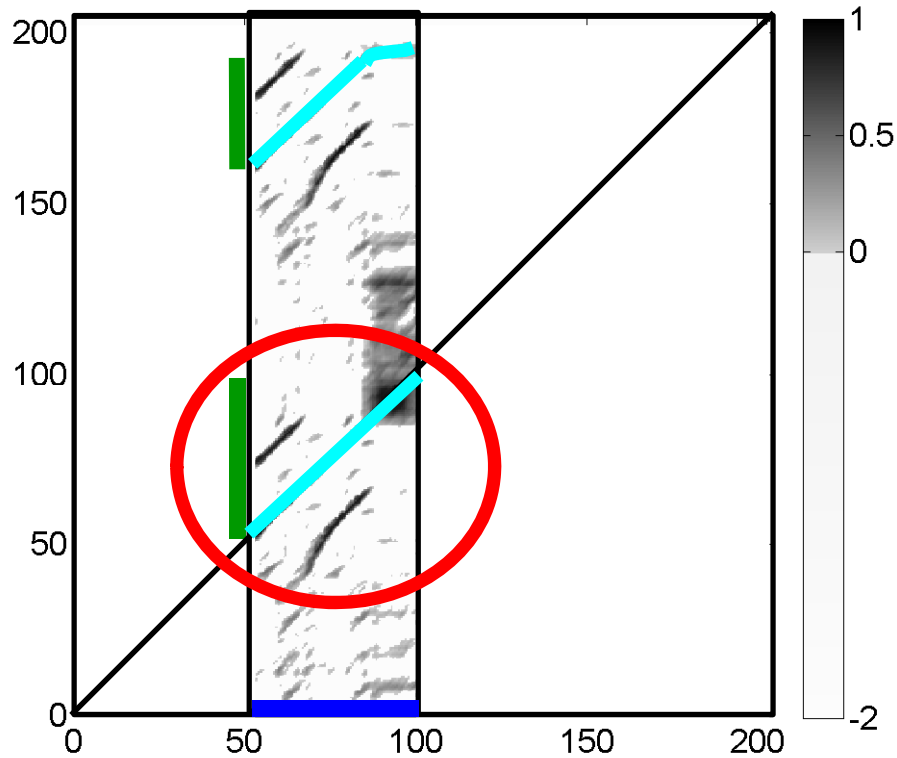
- Consider a fixed **segment**

P := Score(segment)

R := Coverage(segment)



# Fitness Measure



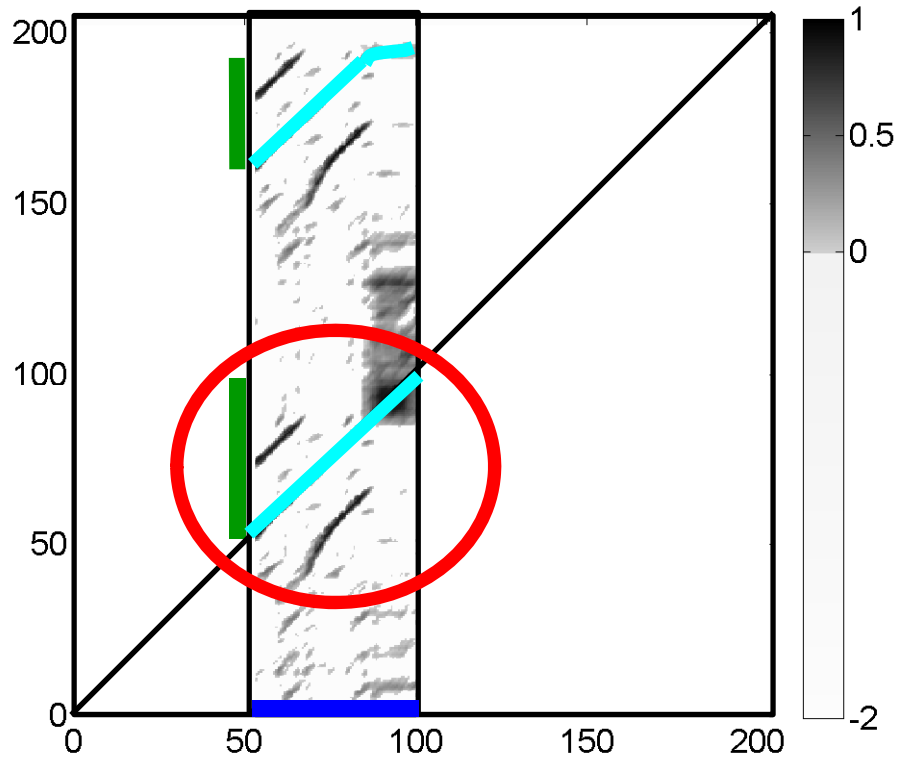
P := Score(segment)

R := Coverage(segment)

## Fitness

- Consider a fixed **segment**
- **Self-explanation are trivial!**

# Fitness Measure



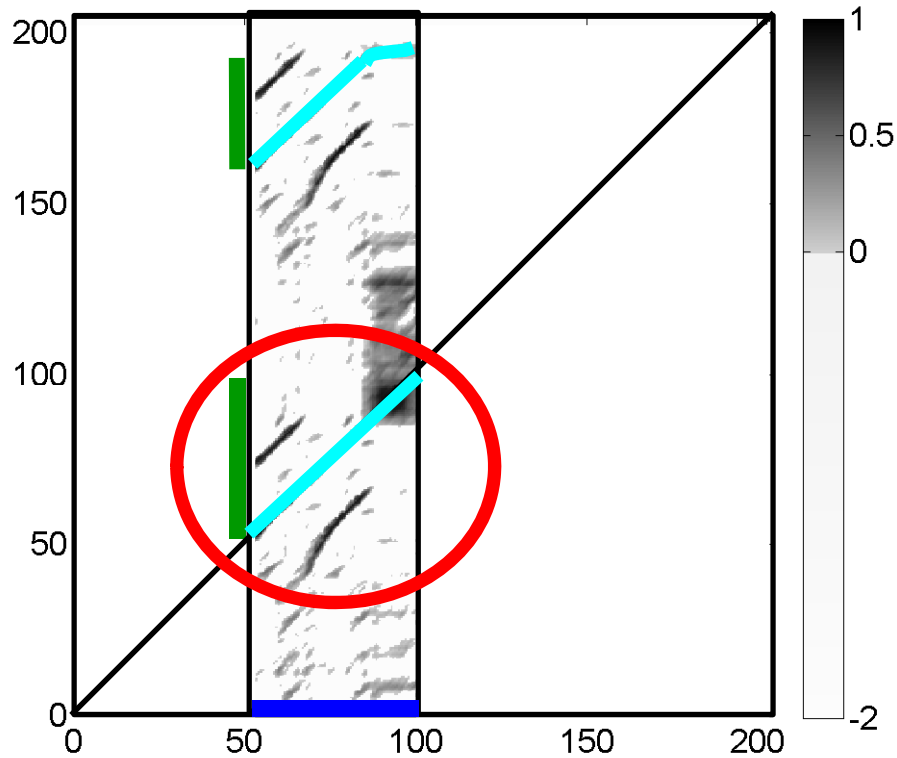
## Fitness

- Consider a fixed **segment**
- **Self-explanation are trivial!**
- Subtract length of **segment**

**P** := **Score(segment)** - length(segment)

**R** := **Coverage(segment)** - length(segment)

# Fitness Measure



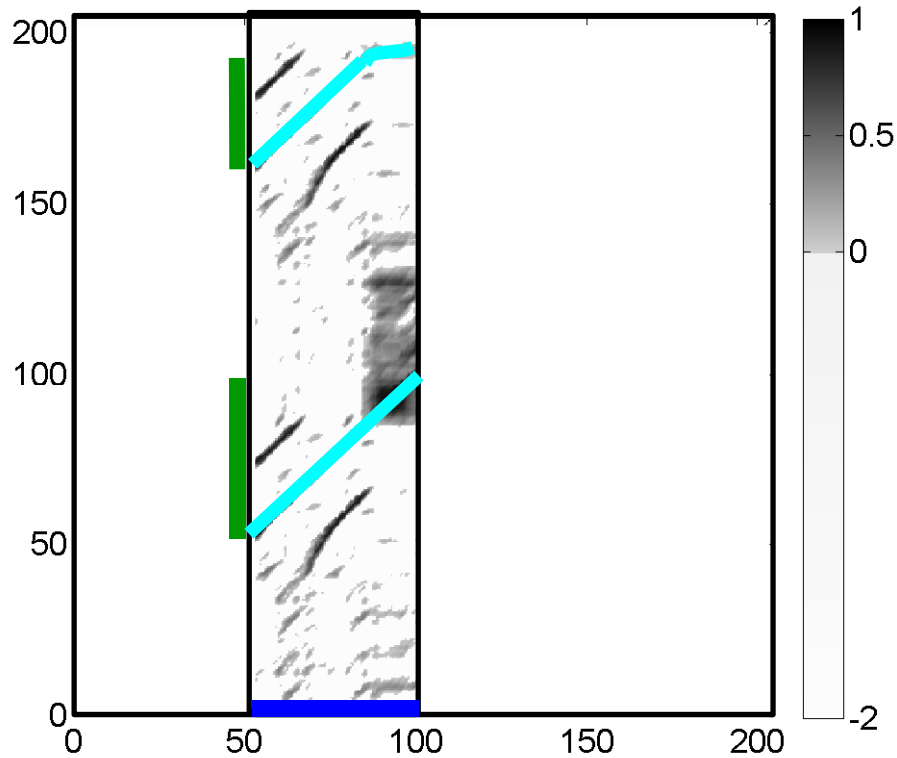
## Fitness

- Consider a fixed **segment**
- **Self-explanation are trivial!**
- Subtract length of **segment**
- Normalization

$$P := \text{Normalize}(\text{Score}(\text{segment}) - \text{length}(\text{segment})) \in [0,1]$$

$$R := \text{Normalize}(\text{Coverage}(\text{segment}) - \text{length}(\text{segment})) \in [0,1]$$

# Fitness Measure



## Fitness

- Consider a fixed **segment**

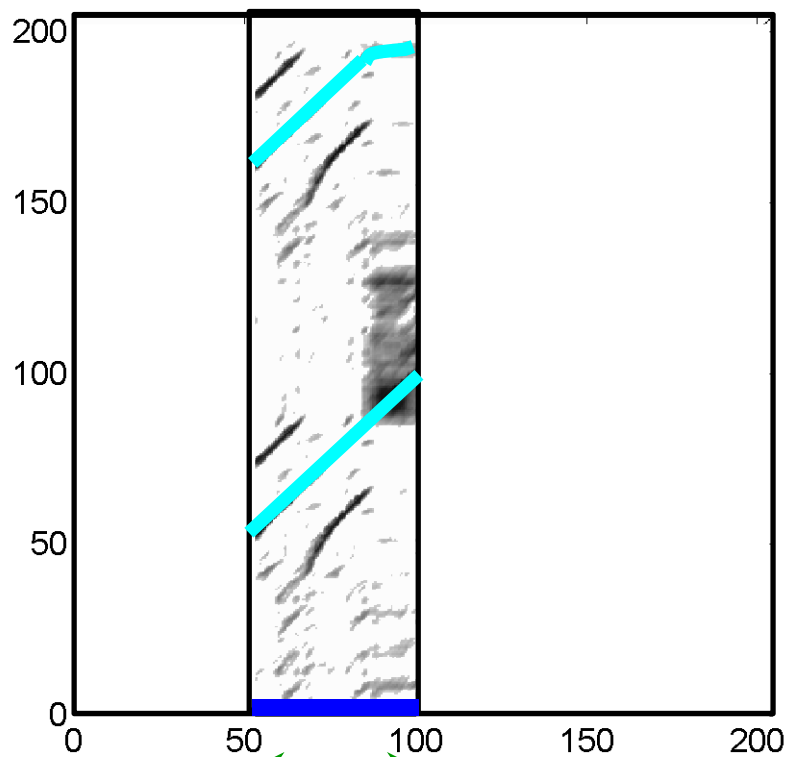
**Fitness**(**segment**)

$$F := 2 \cdot P \cdot R / (P + R)$$

$P := \text{Normalize}(\text{Score}(\text{segment}) - \text{length}(\text{segment})) \in [0,1]$

$R := \text{Normalize}(\text{Coverage}(\text{segment}) - \text{length}(\text{segment})) \in [0,1]$

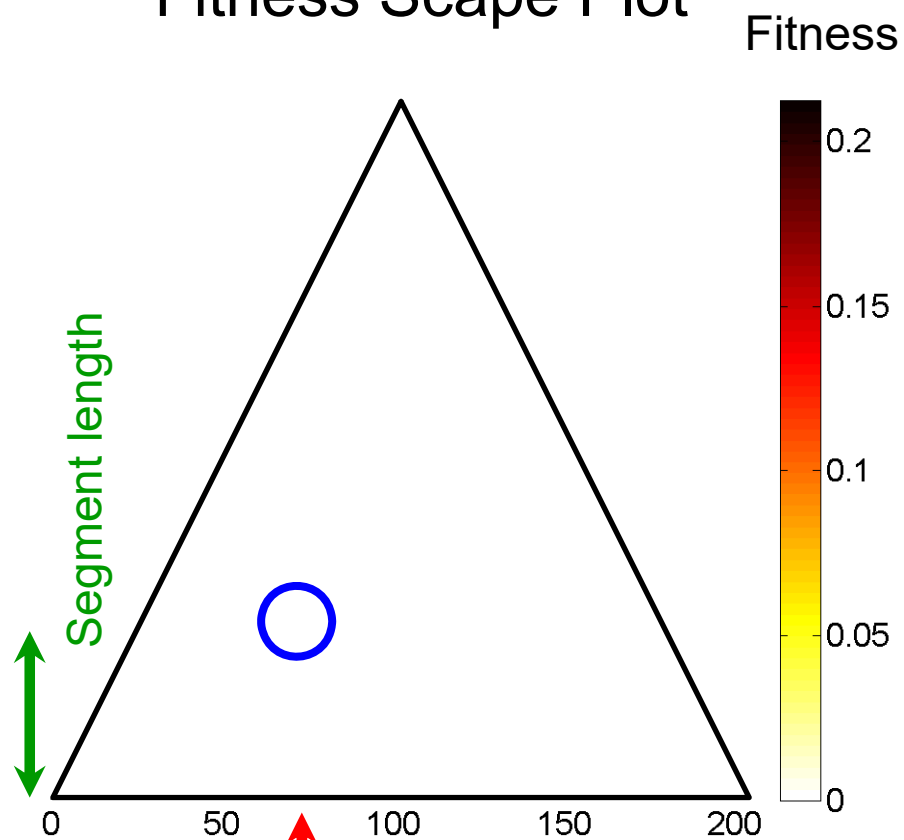
# Thumbnail



Segment length

Segment center

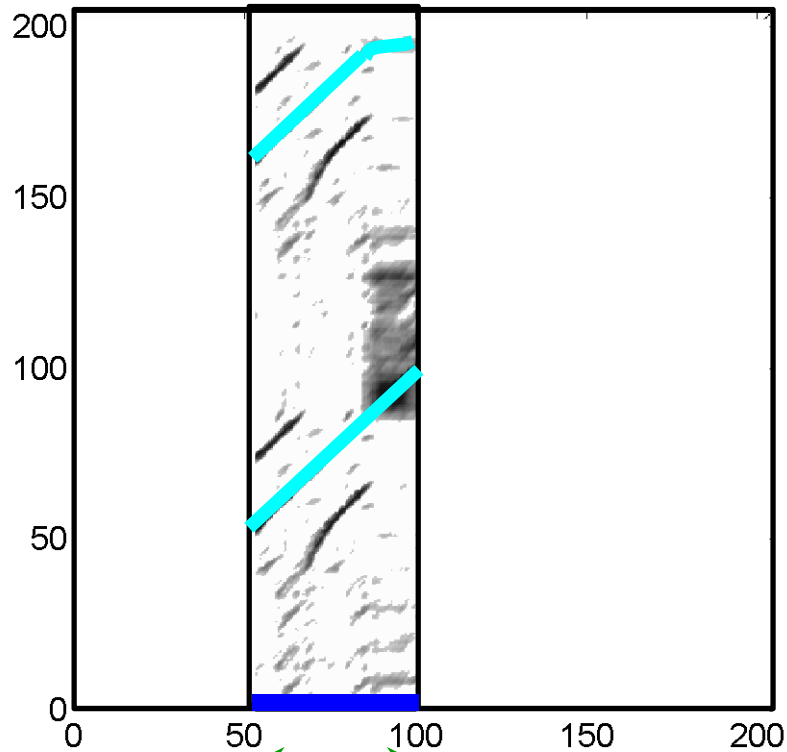
# Fitness Scape Plot



Segment length

Segment center

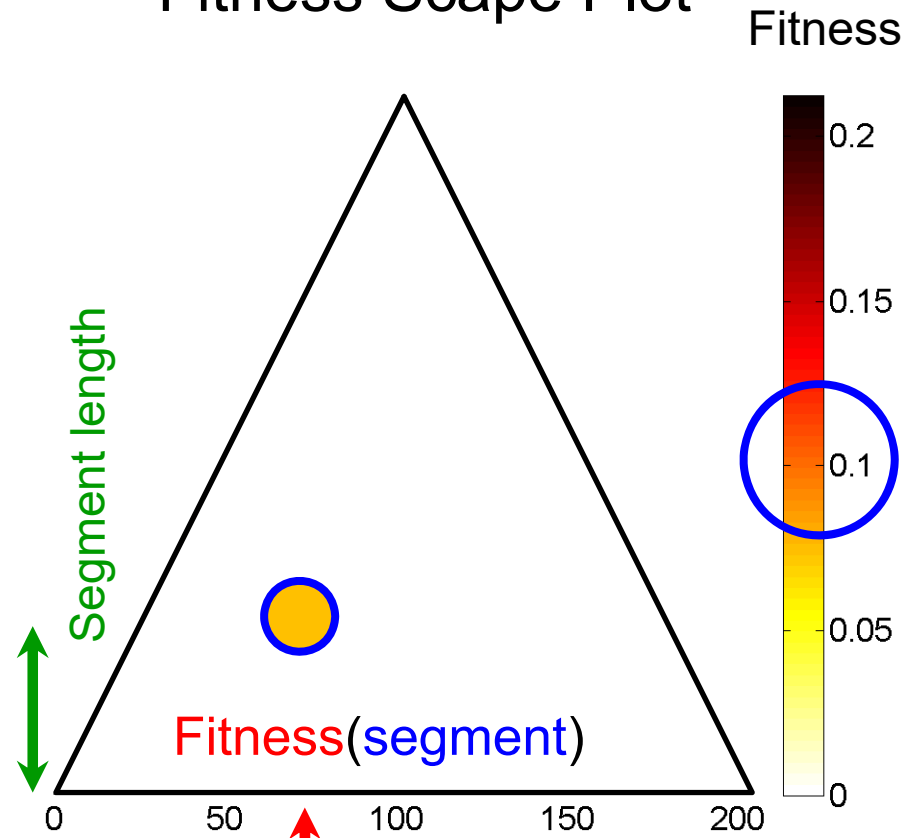
# Thumbnail



Segment length

Segment center

# Fitness Scape Plot

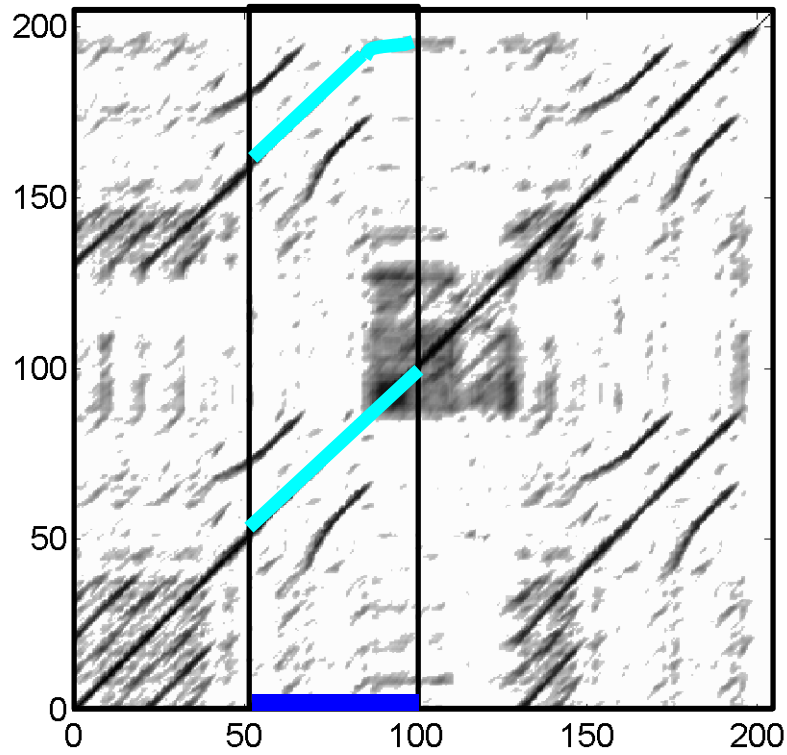


Segment length

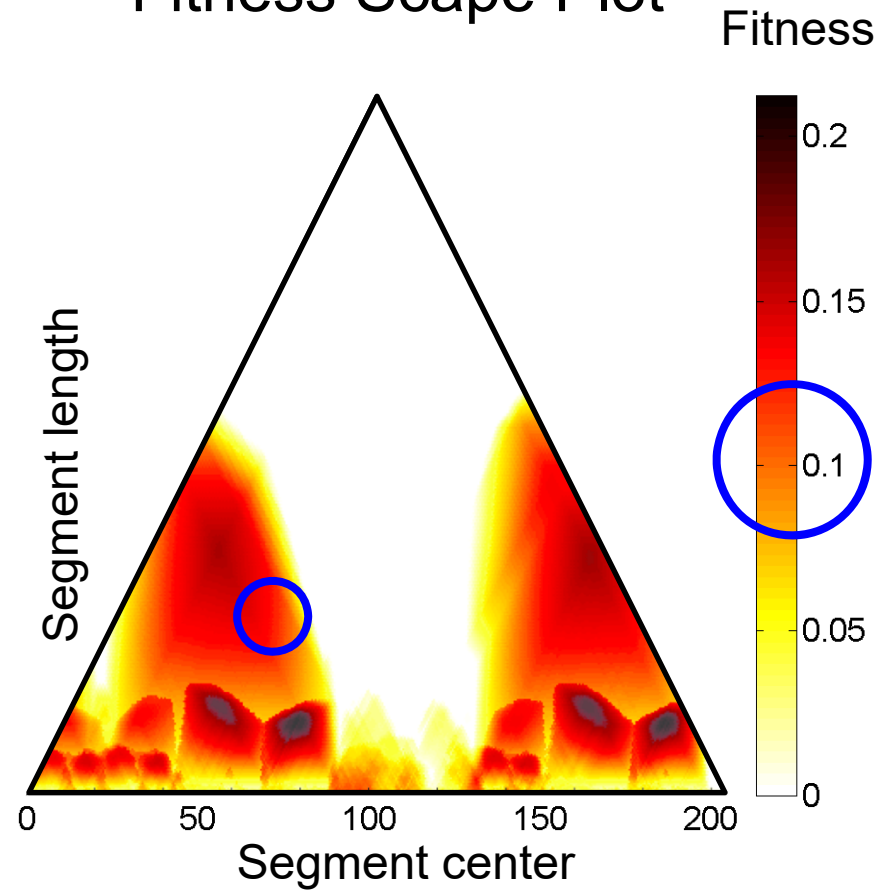
Fitness(segment)

Segment center

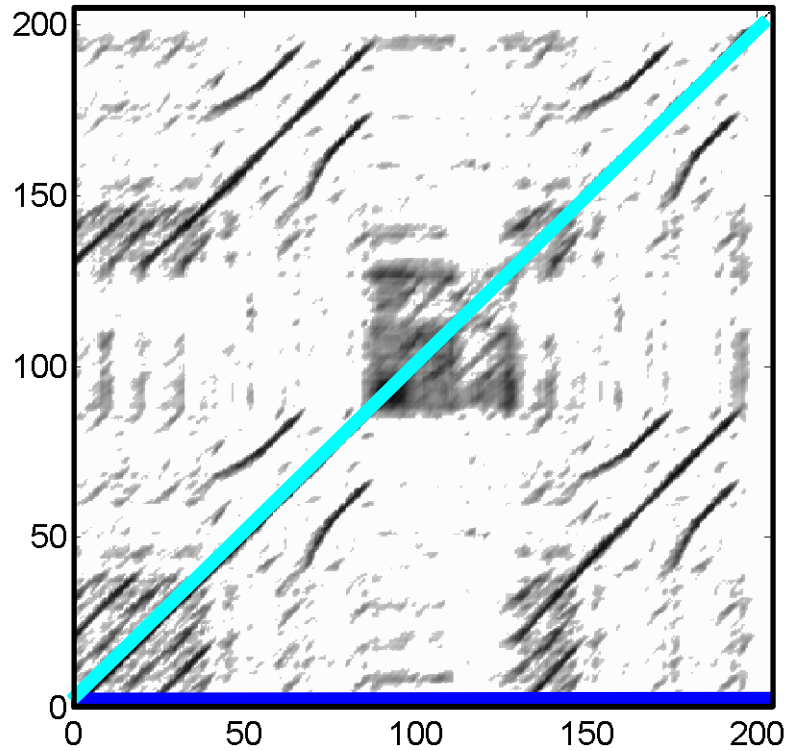
# Thumbnail



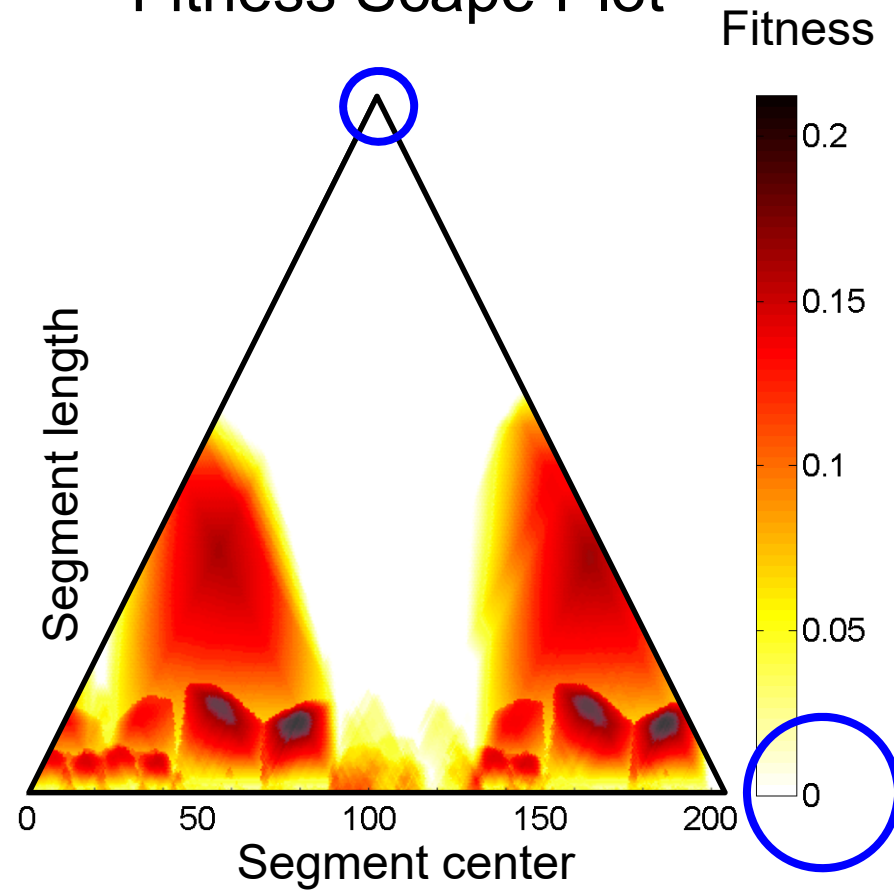
## Fitness Scape Plot



# Thumbnail



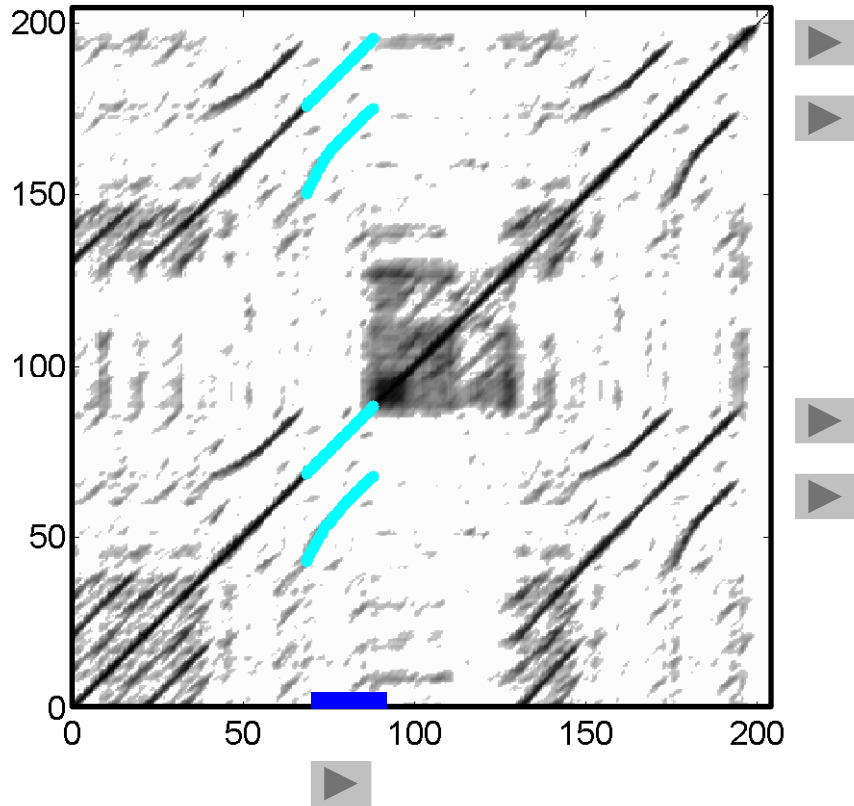
## Fitness Scape Plot



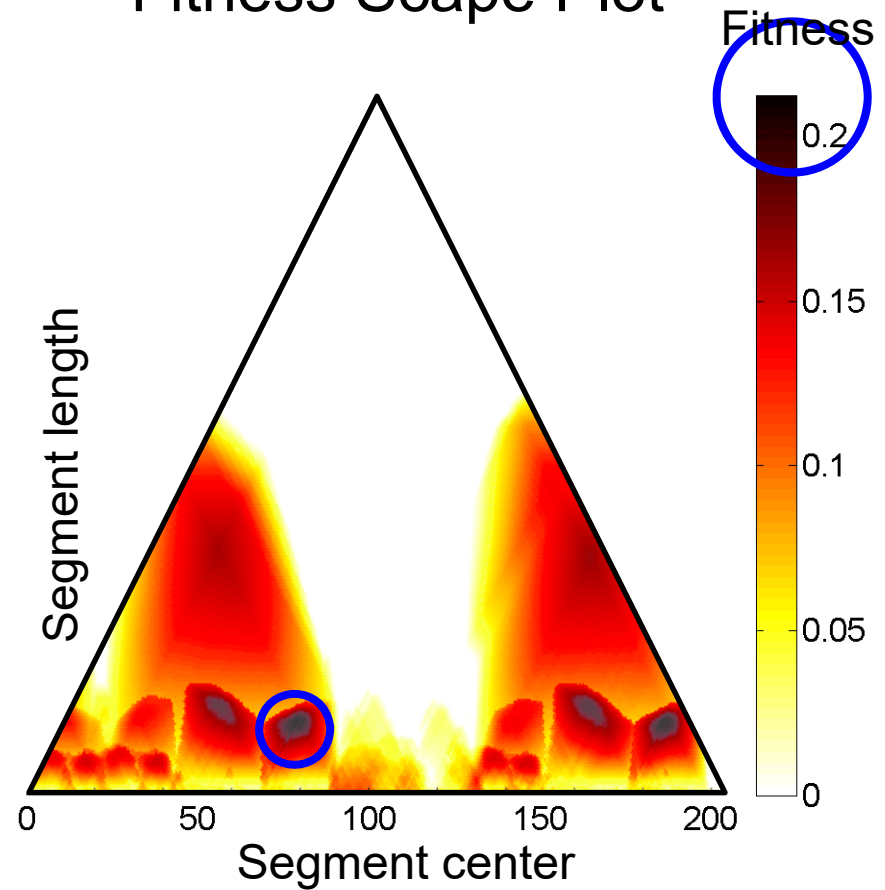
Note: Self-explanations are ignored → fitness is zero



# Thumbnail

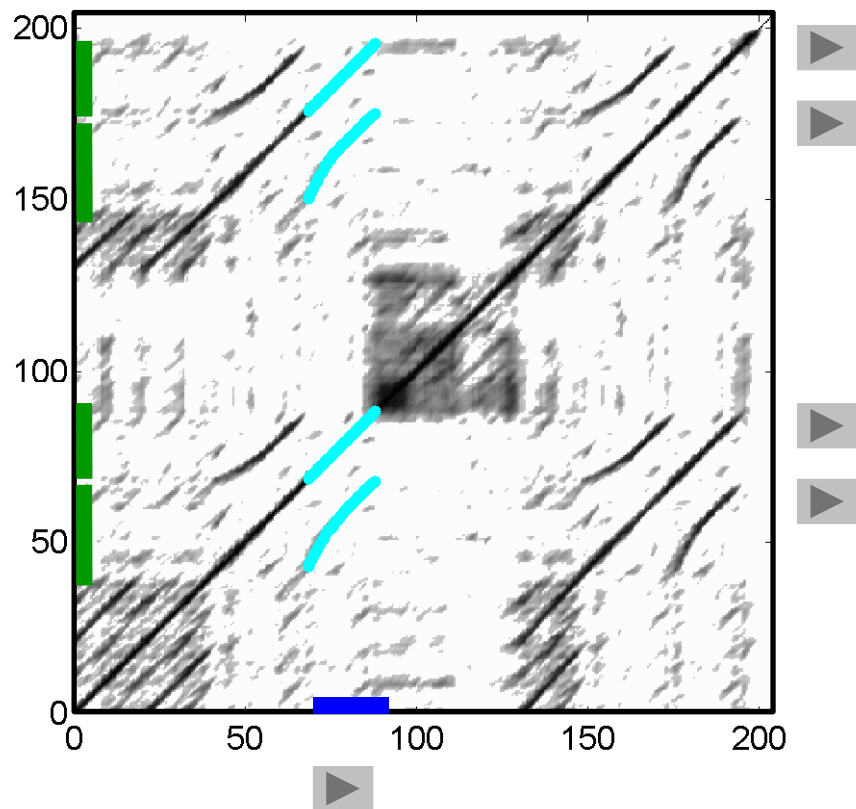


# Fitness Scape Plot

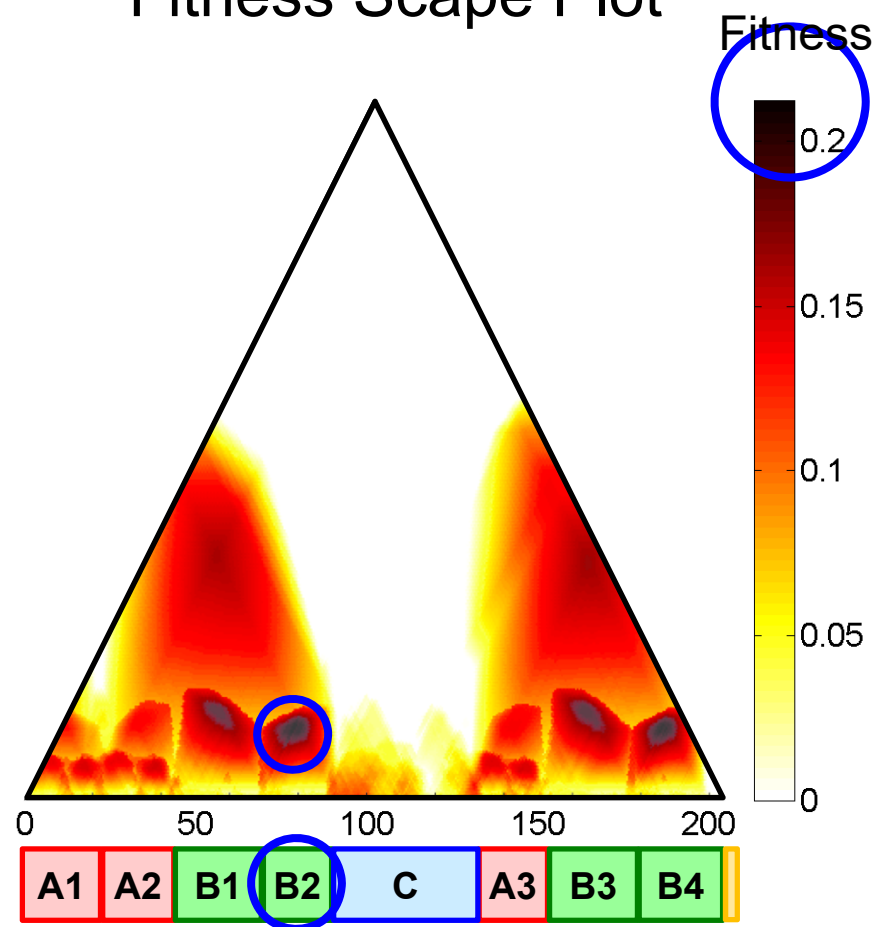


Thumbnail := segment having the highest fitness

# Thumbnail

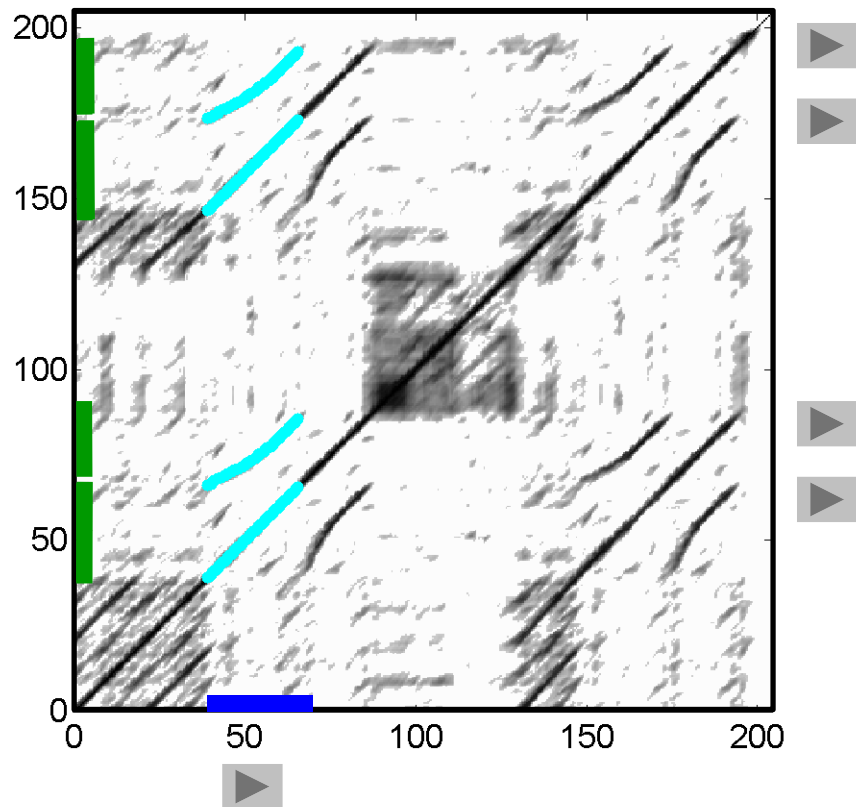


# Fitness Scape Plot

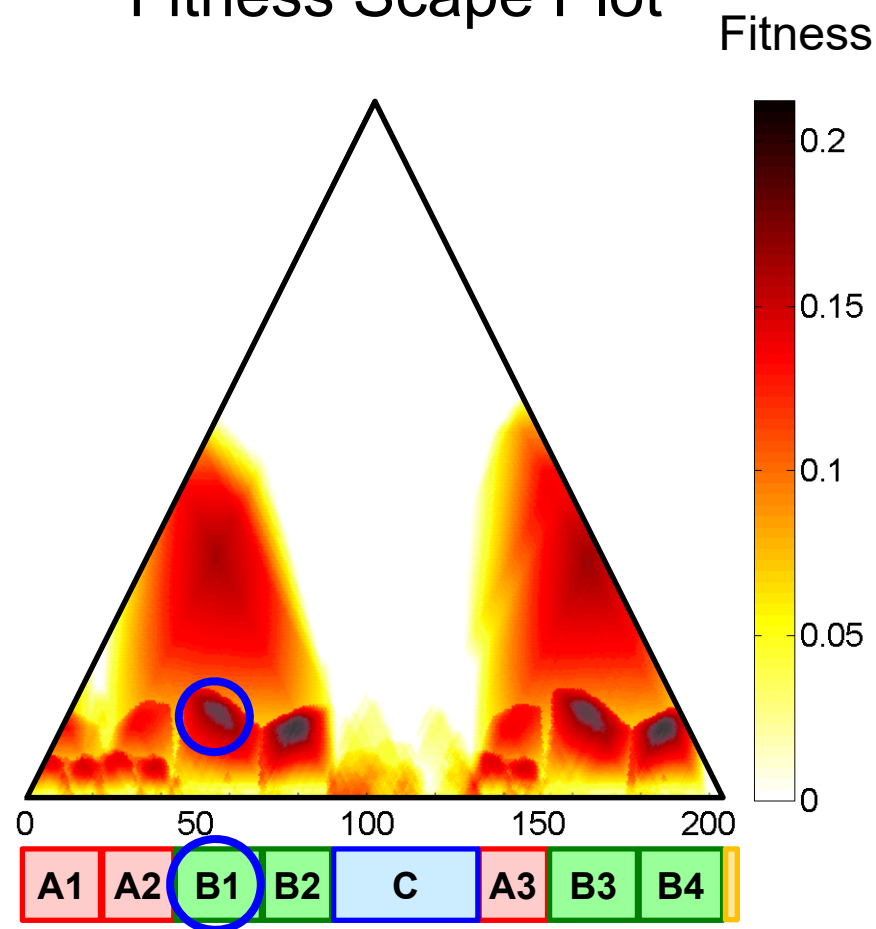


**Example:** Brahms Hungarian Dance No. 5 (Ormandy)

# Thumbnail

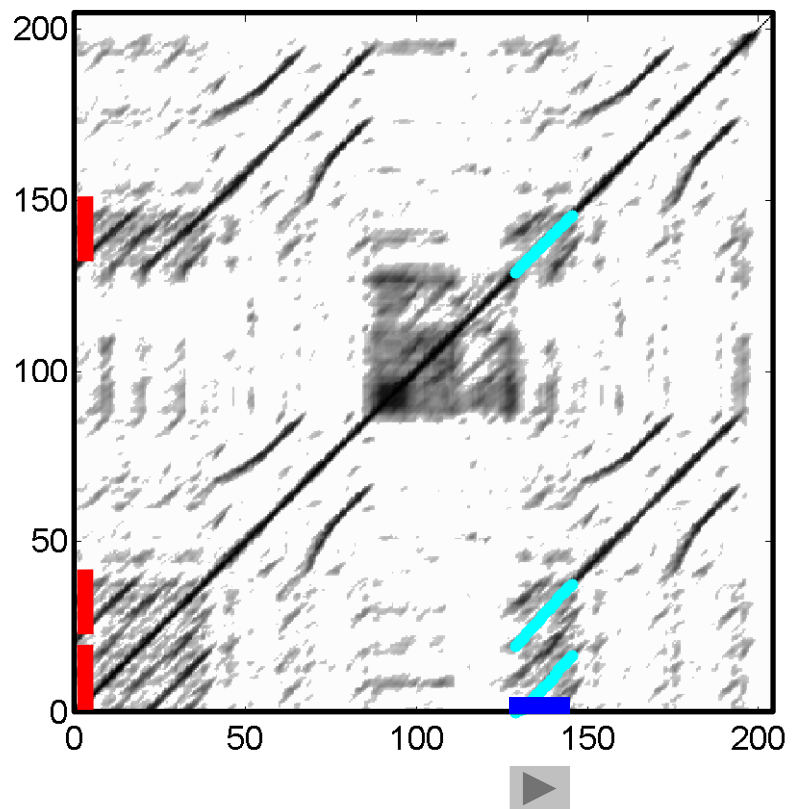


# Fitness Scape Plot

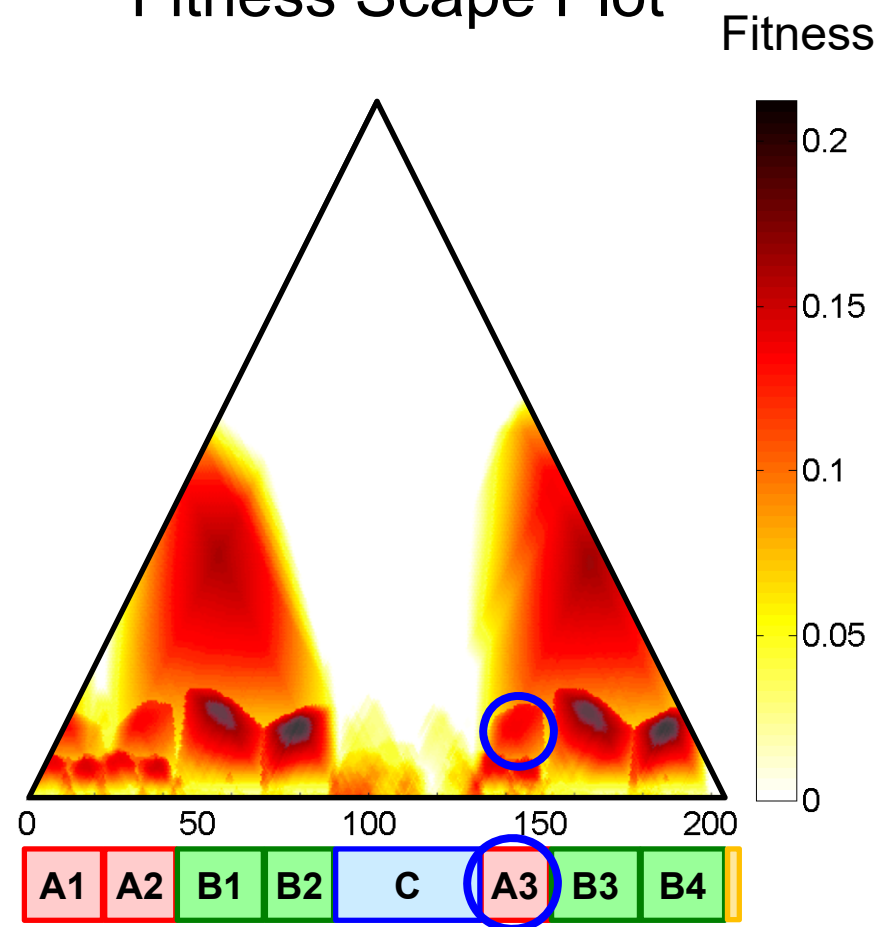


**Example:** Brahms Hungarian Dance No. 5 (Ormandy)

# Thumbnail

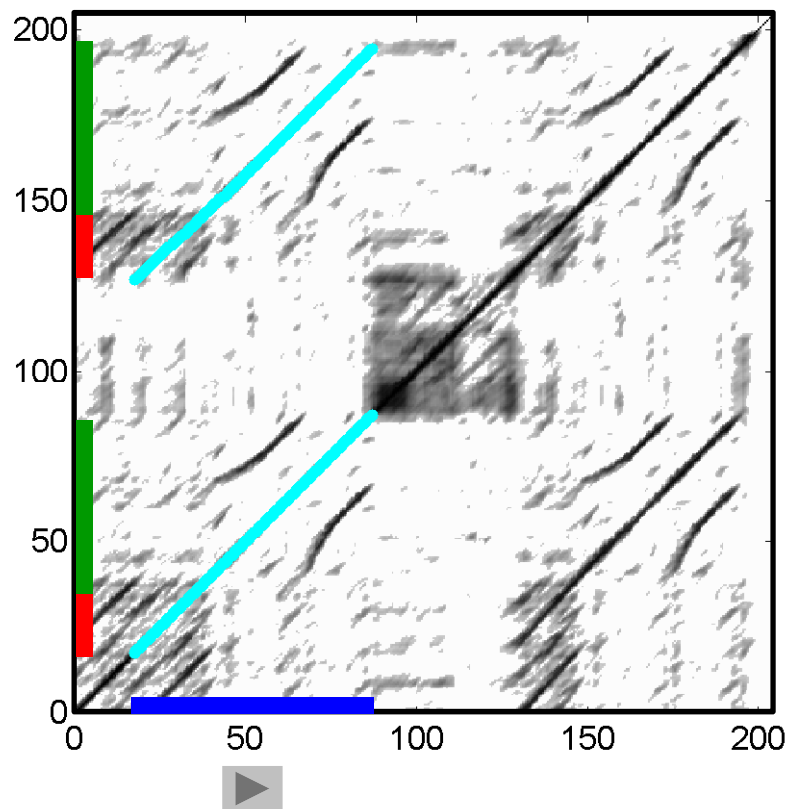


# Fitness Scape Plot

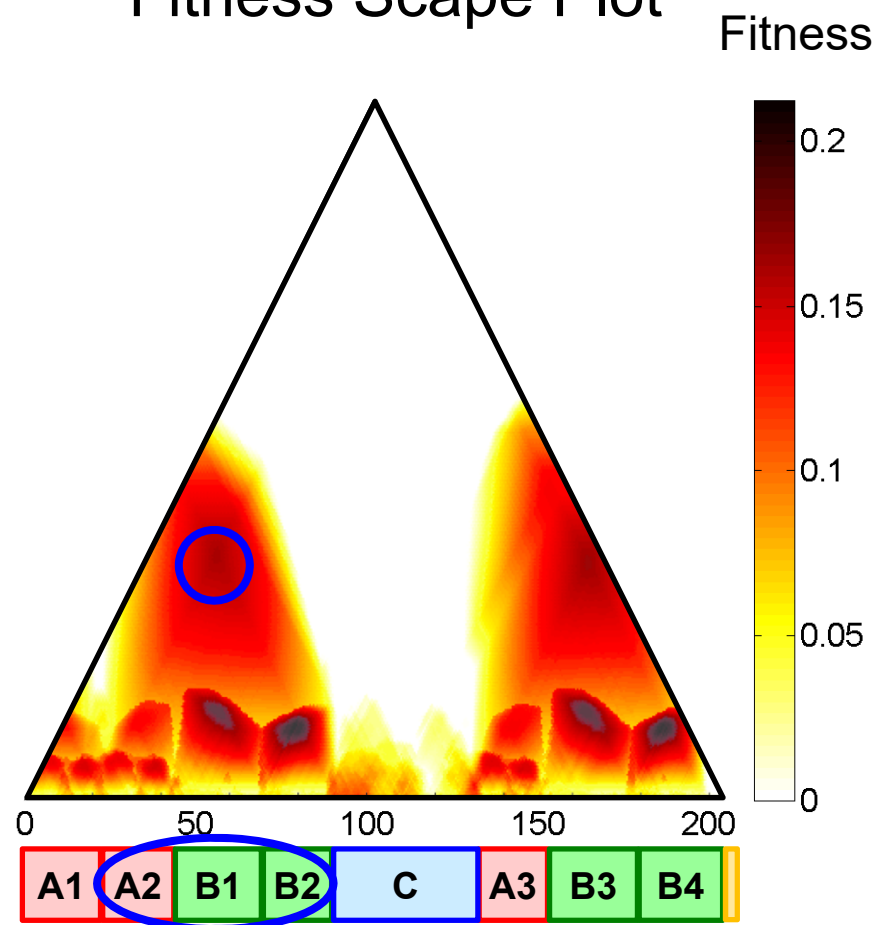


**Example:** Brahms Hungarian Dance No. 5 (Ormandy)

# Thumbnail

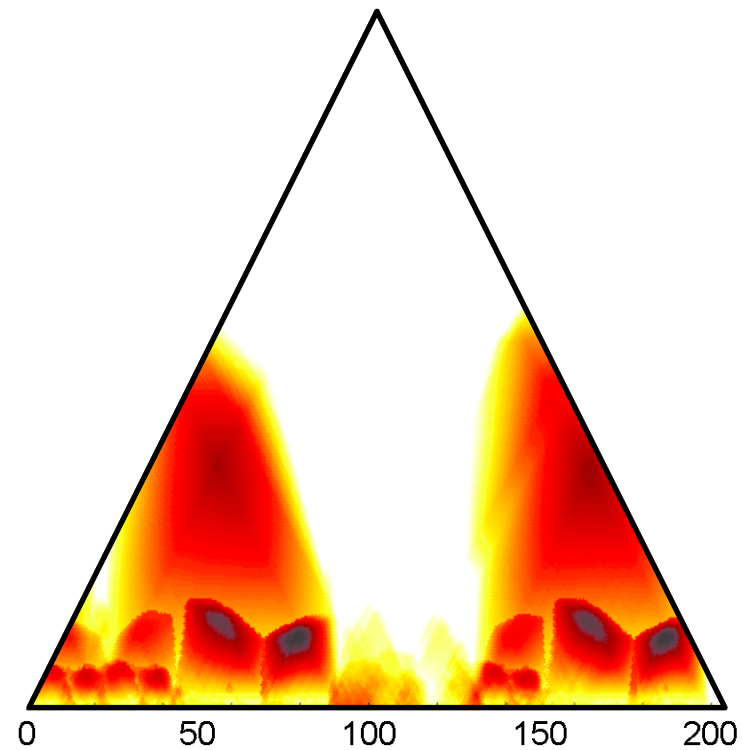


# Fitness Scape Plot



**Example:** Brahms Hungarian Dance No. 5 (Ormandy)

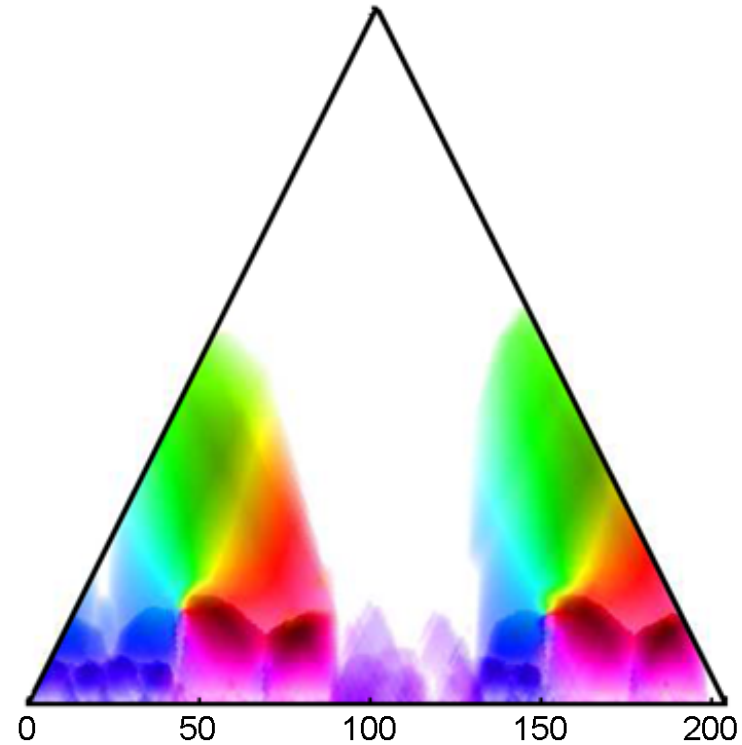
# Scape Plot



**Example:** Brahms Hungarian Dance No. 5 (Ormandy)

# Scape Plot

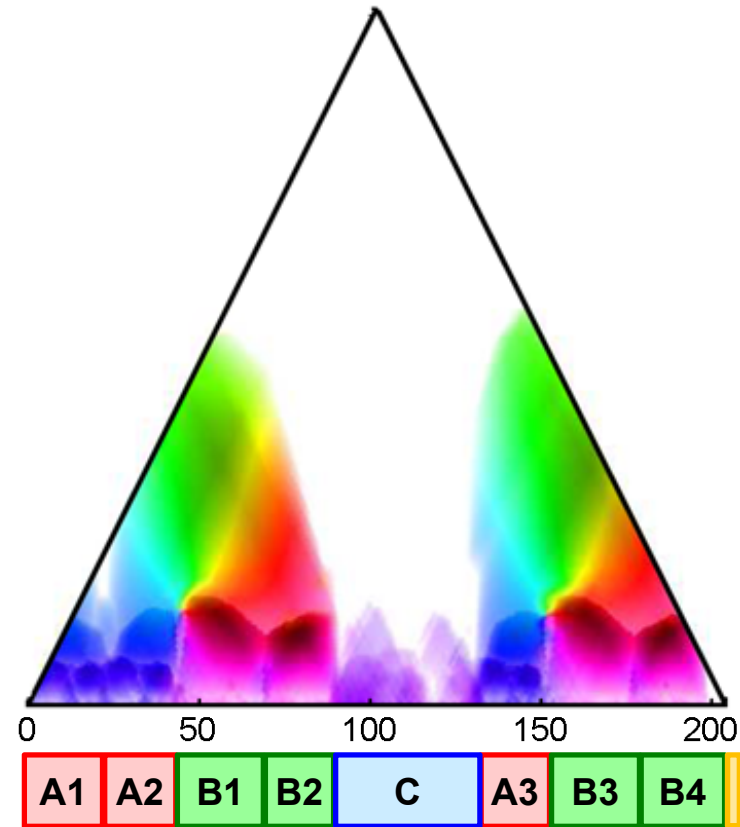
Coloring according to clustering result (grouping)



**Example:** Brahms Hungarian Dance No. 5 (Ormandy)

# Scape Plot

Coloring according to clustering result (grouping)



**Example:** Brahms Hungarian Dance No. 5 (Ormandy)

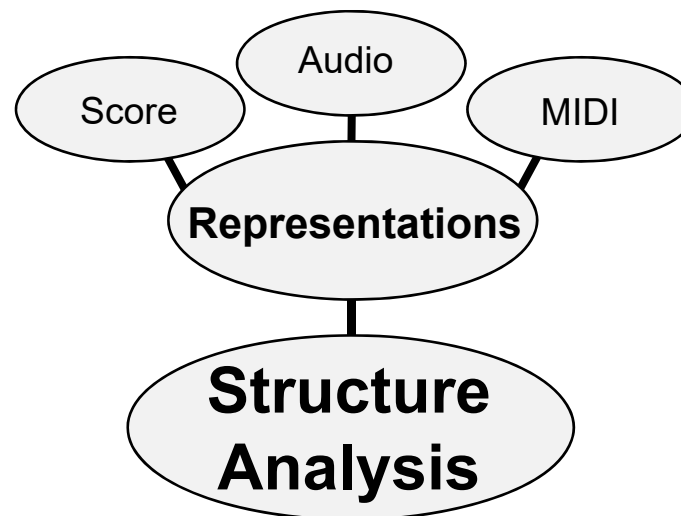


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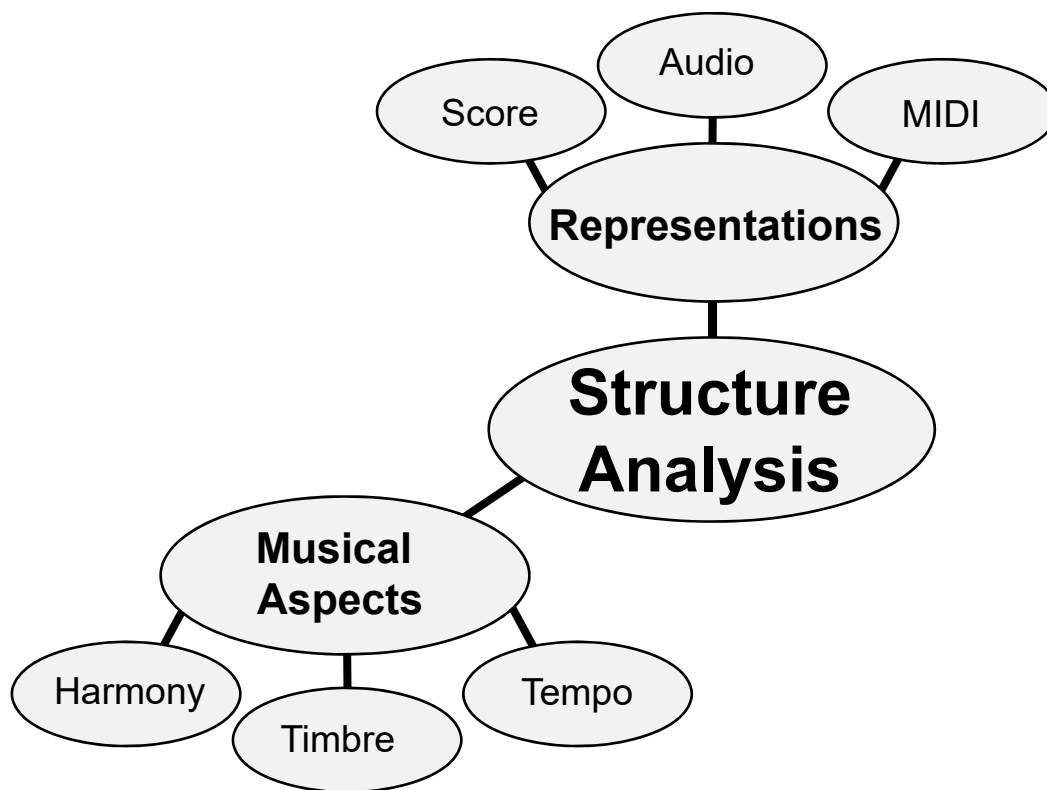
# Conclusions

**Structure  
Analysis**

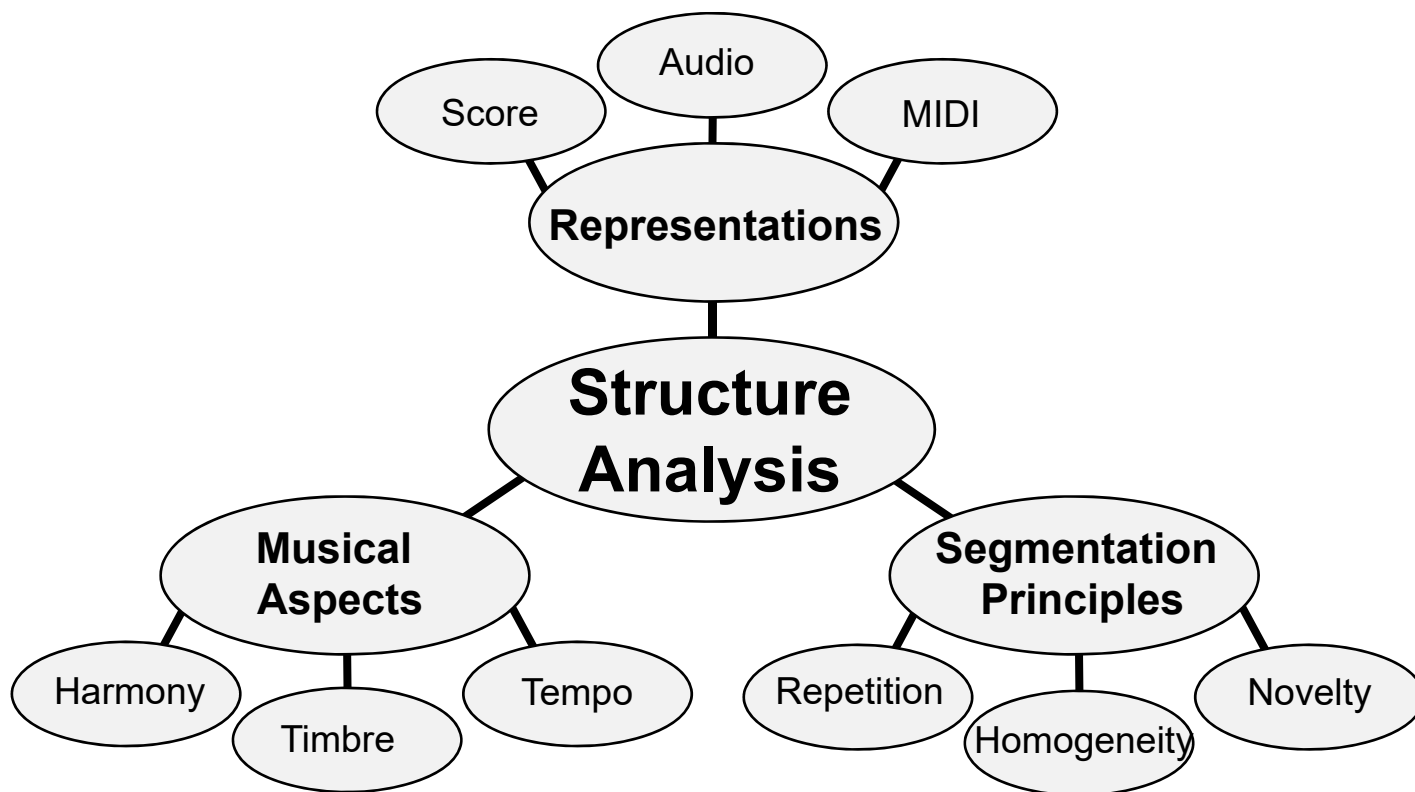
# Conclusions



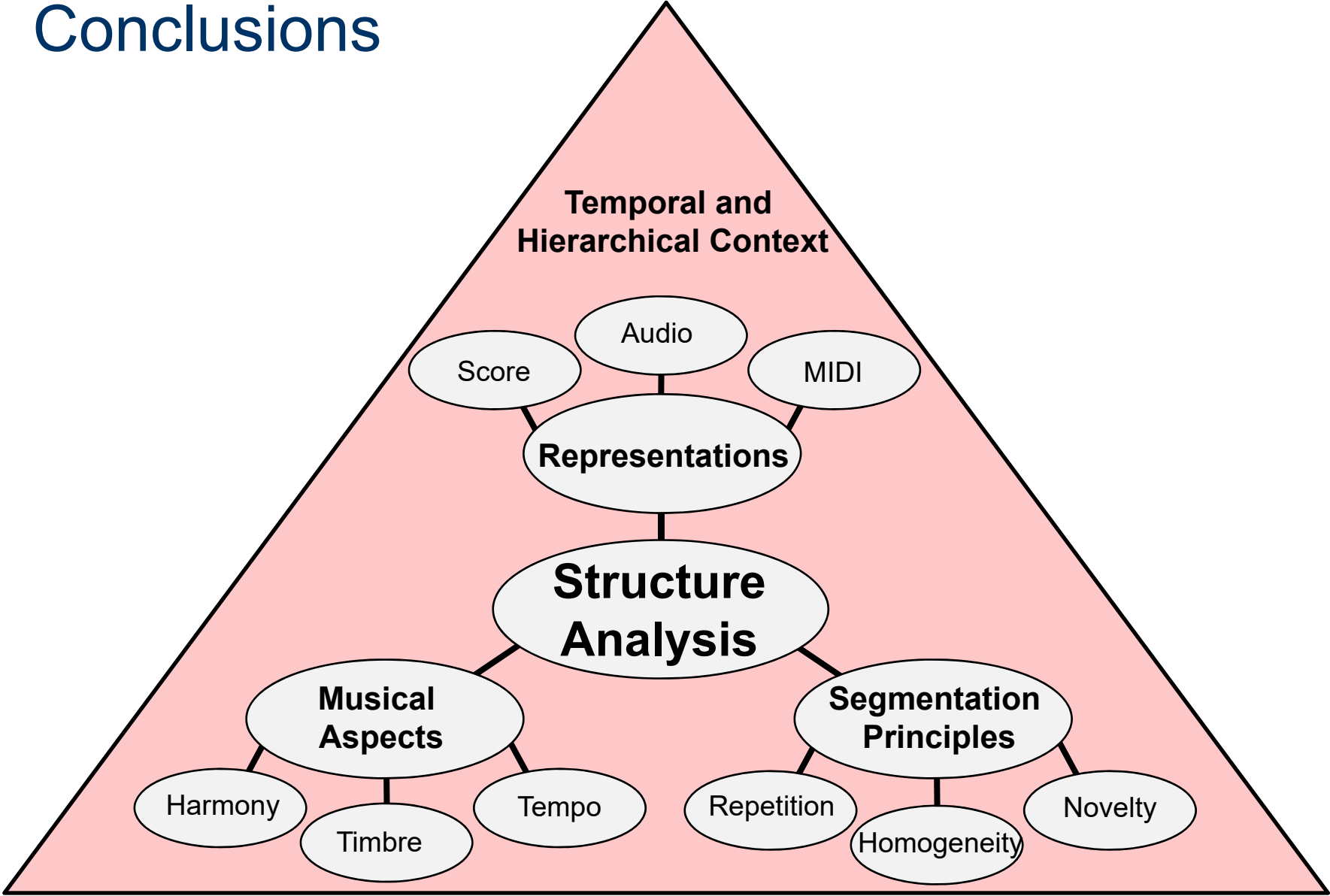
# Conclusions



# Conclusions



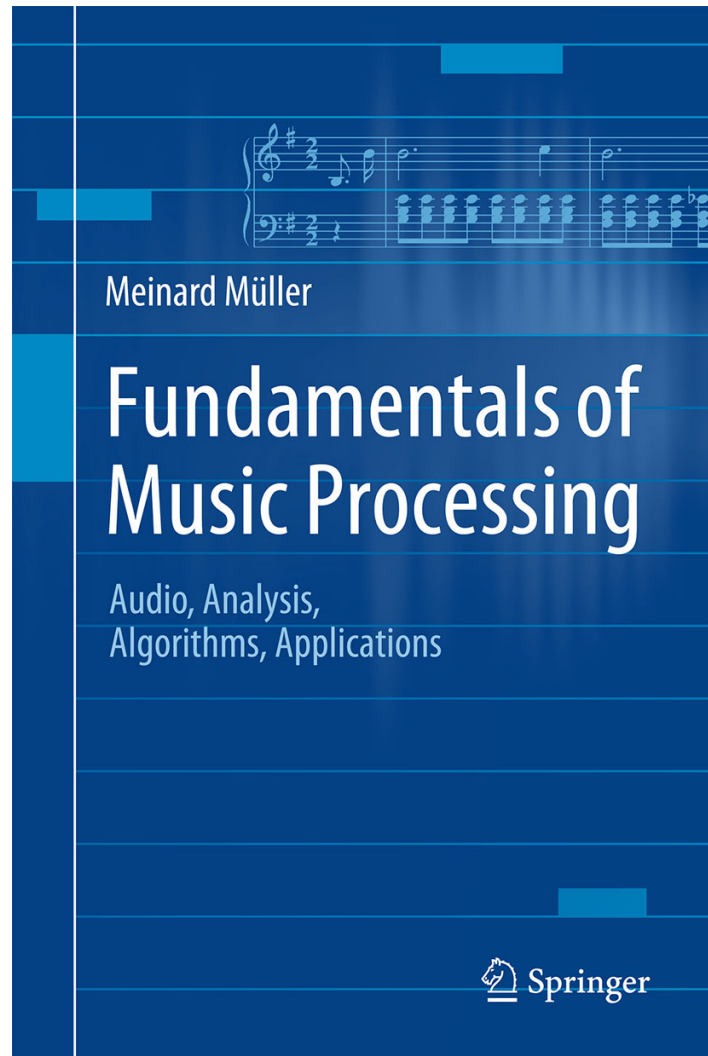
# Conclusions



## Links

- SM Toolbox (MATLAB)  
<http://www.audiolabs-erlangen.de/resources/MIR/SMtoolbox/>
- MSAF: Music Structure Analysis Framework (Python)  
<https://github.com/uriniето/msaf>
- SALAMI Annotation Data  
<http://ddmal.music.mcgill.ca/research/salami/annotations>
- LibROSA (Python)  
<https://librosa.github.io/librosa/>
- Evaluation: mir\_eval (Python)  
[https://craffel.github.io/mir\\_eval/](https://craffel.github.io/mir_eval/)
- Deep Learning: Boundary Detection  
Jan Schlüter (PhD thesis)

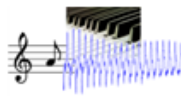

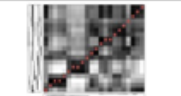


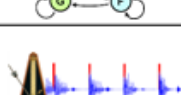


# Book: Fundamentals of Music Processing



Meinard Müller  
Fundamentals of Music Processing  
Audio, Analysis, Algorithms, Applications  
483 p., 249 illus., hardcover  
ISBN: 978-3-319-21944-8  
Springer, 2015

Accompanying website:  
[www.music-processing.de](http://www.music-processing.de)

# Book: Fundamentals of Music Processing

Chapter		Music Processing Scenario
1		Music Representations
2		Fourier Analysis of Signals
3		Music Synchronization
4		Music Structure Analysis
5		Chord Recognition
6		Tempo and Beat Tracking
7		Content-Based Audio Retrieval
8		Musically Informed Audio Decomposition

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