





A Basic Introduction to Audio-Related **Music Information Retrieval**

Audio Features

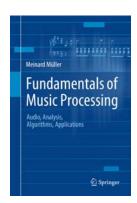
Meinard Müller, Christof Weiß

International Audio Laboratories Erlangen meinard.mueller@audiolabs-erlangen.de, christof.weiss@audiolabs-erlangen.de





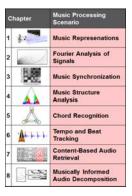
Book: Fundamentals of Music Processing



Meinard Müller Fundamentals of Music Processing Audio, Analysis, Algorithms, Applications 483 p., 249 illus., hardcover ISBN: 978-3-319-21944-8 Springer, 2015

Accompanying website: www.music-processing.de

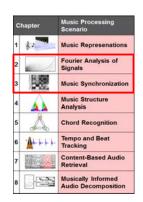
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Chapter 2: Fourier Analysis of Signals

- The Fourier Transform in a Nutshell
- 2.2 Signals and Signal Spaces 2.3 Fourier Transform
- Discrete Fourier Transform (DFT)
- 2.5 Short-Time Fourier Transform (STFT)
- **Further Notes**

Important technical terminology is covered in Chapter 2. In particular, we approach the Fourier transform—which is perhaps the most fundamental tool in signal processing—from various perspectives. For the reader who is more interested in the musical aspects of the book, Section 2.1 provides a summary of the most important facts on the Fourier transform. In particular, the notion of a spectrogram, which yields a time-frequency representation of an audio signal, is introduced. The remainder of the chapter treats the Fourier transform in greater mathematical depth and also includes the fast Fourier transform (FFT)—an algorithm of great beauty and high practical relevance.

Chapter 3: Music Synchronization

- Audio Features 3.1
- 3.2 Dynamic Time Warping
- 3.3 Applications

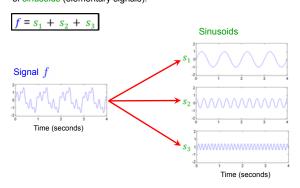




As a first music processing task, we study in Chapter 3 the problem of music synchronization. The objective is to temporally align compatible representations of the same piece of music. Considering this scenario, we explain the need for musically informed audio features. In particular, we introduce the concept of chroma-based music features, which capture properties that are related to harmony and melody. Furthermore, we study an alignment technique known as dynamic time warping (DTW), a concept that is applicable for the analysis of general time series. For its efficient computation, we discuss an algorithm based on dynamic programming—a widely used method for solving a complex problem by breaking it down into a collection of simpler subproblems

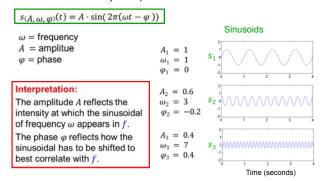
Fourier Transform

Idea: Decompose a given signal into a superposition of sinusoids (elementary signals).



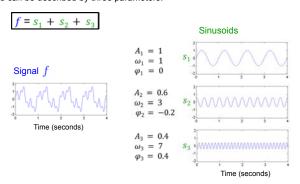
Fourier Transform

Each sinusoid has a physical meaning and can be described by three parameters:



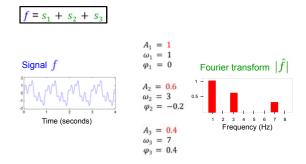
Fourier Transform

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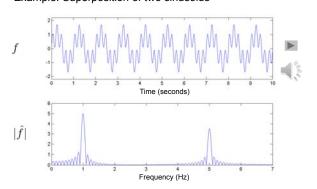
Fourier Transform

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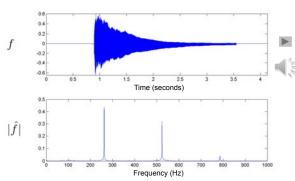
Fourier Transform

Example: Superposition of two sinusoids



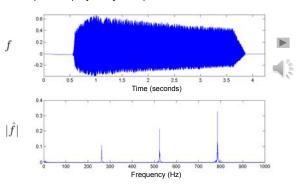
Fourier Transform

Example: C4 played by piano



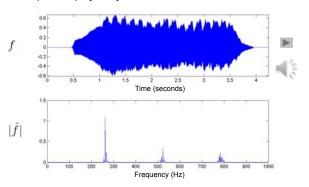
Fourier Transform

Example: C4 played by trumpet



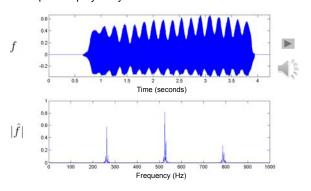
Fourier Transform

Example: C4 played by violin



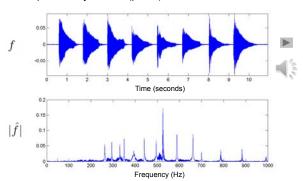
Fourier Transform

Example: C4 played by flute



Fourier Transform

Example: C-major scale (piano)



Fourier Transform

Signal $f: \mathbb{R} \to \mathbb{R}$

Fourier representation $f(t) = \int_{\omega \in \mathbb{R}} c_{\omega} \exp(2\pi i \omega t) d\omega$

Fourier transform $c_{\pmb{\omega}} = \hat{f}(\pmb{\omega}) = \int_{t \in \mathbb{R}} f(t) \exp(-2\pi i \pmb{\omega} t) dt$

Fourier Transform

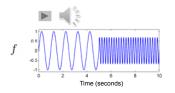
Signal $f: \mathbb{R}$

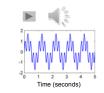
Fourier representation $f(t) \, = \, \int_{\omega \in \mathbb{R}} c_{\omega} \exp(2\pi i \omega t) d\omega$

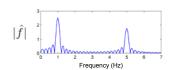
Fourier transform $c_{\omega} = \hat{f}(\omega) = \int_{t \in \mathbb{R}} f(t) \exp(-2\pi i \omega t) dt$

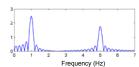
- Tells which frequencies occur, but does not tell when the frequencies occur.
- Frequency information is averaged over the entire time interval.
- Time information is hidden in the phase

Fourier Transform







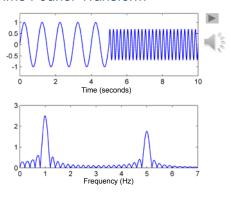


Short Time Fourier Transform

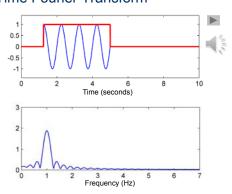
Idea (Dennis Gabor, 1946):

- Consider only a small section of the signal for the spectral analysis
 - → recovery of time information
- Short Time Fourier Transform (STFT)
- Section is determined by pointwise multiplication of the signal with a localizing window function

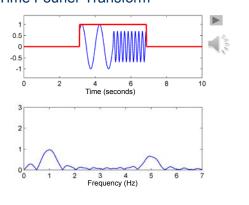
Short Time Fourier Transform



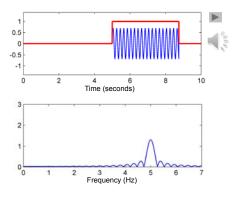
Short Time Fourier Transform



Short Time Fourier Transform



Short Time Fourier Transform



Short Time Fourier Transform

Definition

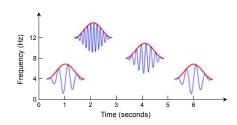
- Signal $f: \mathbb{R} \to \mathbb{R}$
- Window function $g:\mathbb{R}\to\mathbb{R}$ $(g\in L^2(\mathbb{R}),\|g\|_2\neq 0)$
- STFT $\widetilde{f}_g(t, \omega) = \int_{u \in \mathbb{R}} f(u)\overline{g}(u-t) \exp(-2\pi i \omega u) du = \langle f|g_{t,\omega} \rangle$

with
$$g_{t,\omega}(u) = \exp(2\pi i \omega(u-t))g(u-t)$$
 for $u \in \mathbb{R}$

Short Time Fourier Transform

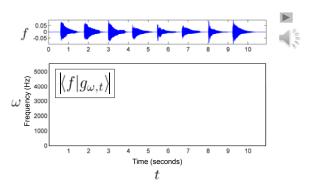
Intuition:

- $g_{t,\omega}$ is "musical note" of frequency ω centered at time t
- Inner product $\langle f|g_{t,\omega}\rangle$ measures the correlation between the musical note $g_{t,\omega}$ and the signal f



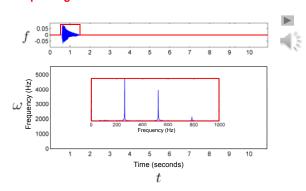
Time-Frequency Representation

Spectrogram



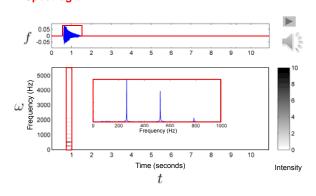
Time-Frequency Representation

Spectrogram



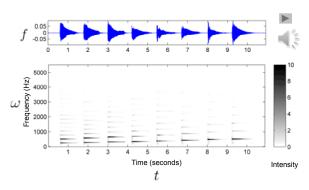
Time-Frequency Representation

Spectrogram



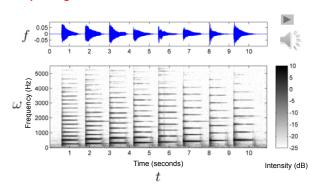
Time-Frequency Representation

Spectrogram



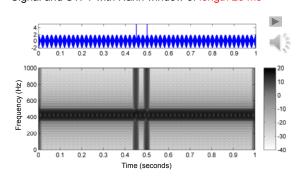
Time-Frequency Representation

Spectrogram



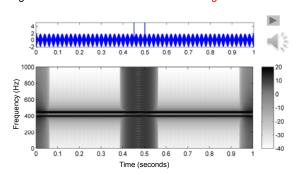
Time-Frequency Representation

Signal and STFT with Hann window of length 20 ms



Time-Frequency Representation

Signal and STFT with Hann window of length 100 ms



Time-Frequency Representation

Time-Frequency Localization

 Size of window constitutes a trade-off between time resolution and frequency resolution:

Large window: poor time resolution

good frequency resolution

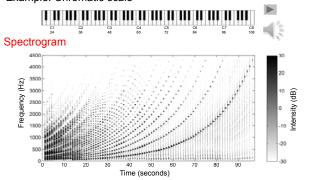
Small window: good time resolution

poor frequency resolution

 Heisenberg Uncertainty Principle: there is no window function that localizes in time and frequency with arbitrary precision.

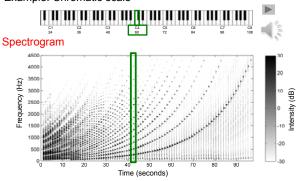
Audio Features

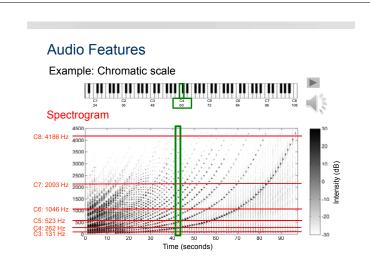
Example: Chromatic scale

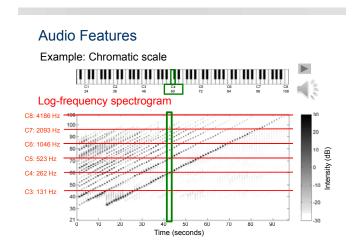


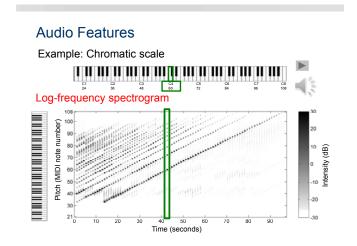
Audio Features

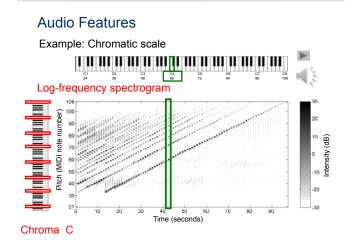
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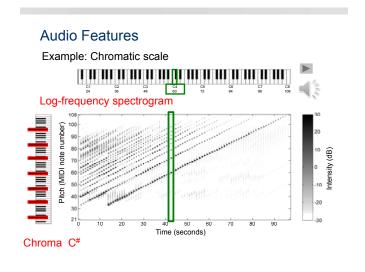


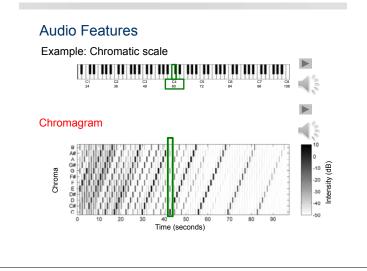










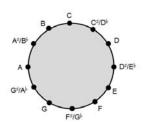


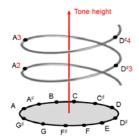
Audio Features

Chroma features

Chromatic circle

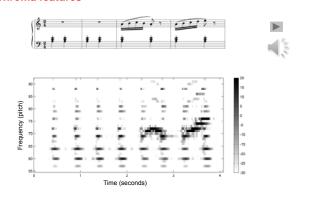
Shepard's helix of pitch





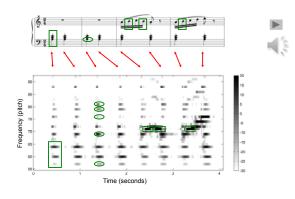
Audio Features

Chroma features



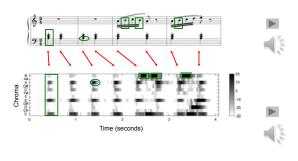
Audio Features

Chroma features



Audio Features

Chroma features



Audio Features

- There are many ways to implement chroma features
- Properties may differ significantly
- Appropriateness depends on respective application
- Chroma Toolbox (MATLAB) https://www.audiolabs-erlangen.de/resources/MIR/chromatoolbox
- LibROSA (Python) https://librosa.github.io/librosa/
- Feature learning: "Deep Chroma" [Korzeniowski/Widmer, ISMIR 2016]