

Learning-By-Doing: Using the FMP Python Notebooks for Audio and Music Processing

Meinard Müller

International Audio Laboratories Erlangen meinard.mueller@audiolabs-erlangen.de

NUS Computer Science Research Week 2022 Singapore, January 6, 2022





Meinard Müller



Mathematics (Diplom/Master)
 Computer Science (PhD)
 Information Retrieval (Habilitation)



Since 2012: Professor
 Semantic Audio Processing



 Former President of the International Society for Music Information Retrieval (MIR)



 Member of the Senior Editorial Board of the IEEE Signal Processing Magazine



IEEE Fellow for contributions to Music Signal Processing



Meinard Müller: Research Group Semantic Audio Processing

- Sebastian Rosenzweig
- Michael Krause
- Yigitcan Özer
- Peter Meier (external)
- Christof Weiß
- Frank Zalkow
- Christian Dittmar
- Stefan Balke
- Jonathan Driedger
- Thomas Prätzlich
- ...





















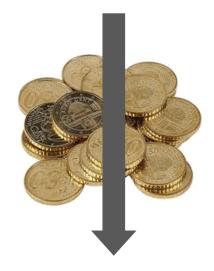
International Audio Laboratories Erlangen





- Fraunhofer Institute for Integrated Circuits IIS
- Largest Fraunhofer institute with
 ≈ 1000 members
- Applied research for sensor, audio, and media technology











- Friedrich-Alexander
 Universität Erlangen Nürnberg (FAU)
- One of Germany's largest universities with ≈ 40,000 students
- Strong Technical Faculty



International Audio Laboratories Erlangen



International Audio Laboratories Erlangen

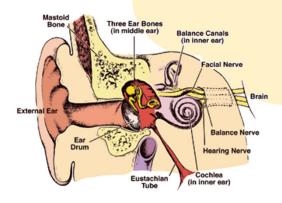
Audio Coding



Audio



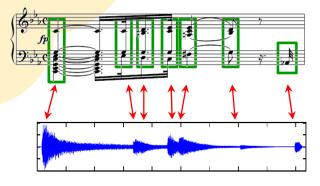




Psychoacoustics



Internet of Things



Music Processing



AudioLabs – FAU

- Prof. Dr. Jürgen Herre Audio Coding
- Prof. Dr. Bernd Edler Audio Signal Analysis
- Prof. Dr. Meinard Müller
 Semantic Audio Processing
- Prof. Dr. Emanuël Habets
 Spatial Audio Signal Processing
- Prof. Dr. Nils Peters
 Audio Signal Processing
- Dr. Stefan Turowski
 Coordinator AudioLabs-FAU













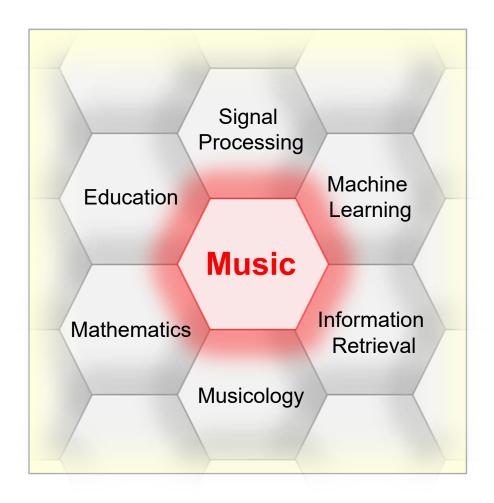
Music Processing





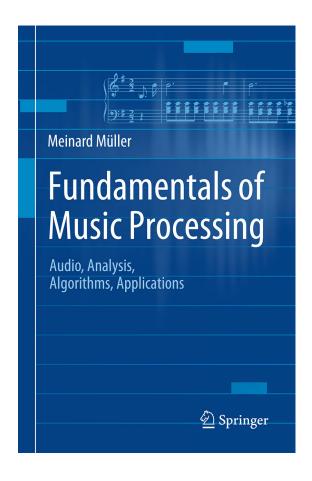


Music Processing: A Multifaceted Research Area



- Music is a ubiquitous and vital part of our lives
- Digital music services:
 Spotify, Pandora, iTunes, ...
- Music yields intuitive entry point to support and motivate education in technical disciplines
- Music bridges the gap between engineering, computer science, mathematics, and the humanities

Fundamentals of Music Processing (FMP)

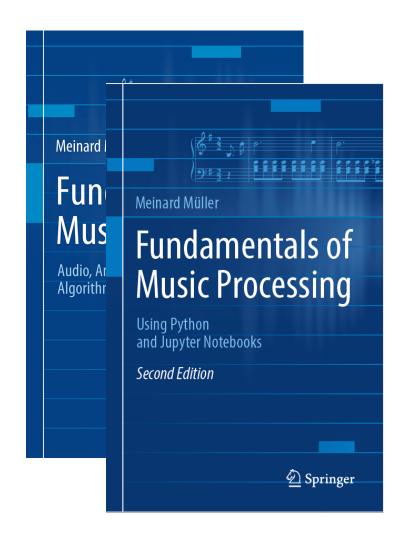


Meinard Müller Fundamentals of Music Processing Audio, Analysis, Algorithms, Applications Springer, 2015

Accompanying website: www.music-processing.de



Fundamentals of Music Processing (FMP)



Meinard Müller Fundamentals of Music Processing Audio, Analysis, Algorithms, Applications Springer, 2015

Accompanying website: www.music-processing.de

2nd edition
Meinard Müller
Fundamentals of Music Processing
Using Python and Jupyter Notebooks
Springer, 2021

Fundamentals of Music Processing (FMP)

Chapter		Music Processing Scenario
1		Music Represenations
2		Fourier Analysis of Signals
3	3.00	Music Synchronization
4		Music Structure Analysis
5		Chord Recognition
6	A++++	Tempo and Beat Tracking
7		Content-Based Audio Retrieval
8		Musically Informed Audio Decomposition

Meinard Müller Fundamentals of Music Processing Audio, Analysis, Algorithms, Applications Springer, 2015

Accompanying website: www.music-processing.de

2nd edition
Meinard Müller
Fundamentals of Music Processing
Using Python and Jupyter Notebooks
Springer, 2021

FMP Notebooks: Education & Research



FMP Notebooks



Python Notebooks for Fundamentals of Music Processing

The FMP notebooks offer a collection of educational material closely following the textbook <u>Fundamentals of Music Processing (FMP)</u>. This is the starting website, which is opened when calling <u>https://www.audiolabs-erlangen.de/FMP</u>. Besides giving an <u>overview</u>, this website provides information on the license, the main contributors, and some links.

https://www.audiolabs-erlangen.de/FMP



FMP Notebooks: Education & Research

- ... provide educational material for teaching and learning fundamentals of music processing.
- ... combine textbook-like explanations, technical concepts, mathematical details, Python code examples, illustrations, and sound examples.
- ... bridge the gap between theory and practice being based on interactive Jupyter notebook framework.
- ... are freely accessible under a Creative Commons license.

https://www.audiolabs-erlangen.de/FMP



Part	Title	Notions, Techniques & Algorithms	нтмь	IPYNB
B jupyter	Basics	Basic information on Python, Jupyter notebooks, Anaconda package management system, Python environments, visualizations, and other topics	[html]	[ipynb]
0	Overview	Overview of the notebooks (https://www.audiolabs- erlangen.de/FMP)	[html]	[ipynb]
1 😝	Music Representations	Music notation, MIDI, audio signal, waveform, pitch, loudness, timbre	[html]	[ipynb]
2	Fourier Analysis of Signals	Discrete/analog signal, sinusoid, exponential, Fourier transform, Fourier representation, DFT, FFT, STFT	[html]	[ipynb]
3	Music Synchronization	Chroma feature, dynamic programming, dynamic time warping (DTW), alignment, user interface	[html]	[ipynb]
4	Music Structure Analysis	Similarity matrix, repetition, thumbnail, homogeneity, novelty, evaluation, precision, recall, F- measure, visualization, scape plot	[html]	[ipynb]
5	Chord Recognition	Harmony, music theory, chords, scales, templates, hidden Markov model (HMM), evaluation	[html]	[ipynb]
6 1	Tempo and Beat Tracking	Onset, novelty, tempo, tempogram, beat, periodicity, Fourier analysis, autocorrelation	[html]	[ipynb]
7	Content-Based Audio Retrieval	Identification, fingerprint, indexing, inverted list, matching, version, cover song	[html]	[ipynb]
8	Musically Informed Audio Decomposition	Harmonic/percussive separation, signal reconstruction, instantaneous frequency, fundamental frequency (F0), trajectory, nonnegative matrix factorization (NMF)	[html]	[ipynb]



Part	Title	Notions, Techniques & Algorithms	HTML	IPYNB
B P jupyter	Basics	Basic information on Python, Jupyter notebooks, Anaconda package management system, Python environments, visualizations, and other topics	[html]	[ipynb]
0	Overview	Overview of the notebooks (https://www.audiolabs- erlangen.de/FMP)	[html]	[ipynb]
1 🗱	Music Representations	Music notation, MIDI, audio signal, waveform, pitch, loudness, timbre	[html]	[ipynb]
2	Fourier Analysis of Signals	Discrete/analog signal, sinusoid, exponential, Fourier transform, Fourier representation, DFT, FFT, STFT	[html]	[ipynb]
3	Music Synchronization	Chroma feature, dynamic programming, dynamic time warping (DTW), alignment, user interface	[html]	[ipynb]
4	Music Structure Analysis	Similarity matrix, repetition, thumbnail, homogeneity, novelty, evaluation, precision, recall, F- measure, visualization, scape plot	[html]	[ipynb]
5	Chord Recognition	Harmony, music theory, chords, scales, templates, hidden Markov model (HMM), evaluation	[html]	[ipynb]
6	Tempo and Beat Tracking	Onset, novelty, tempo, tempogram, beat, periodicity, Fourier analysis, autocorrelation	[html]	[ipynb]
7	Content-Based Audio Retrieval	Identification, fingerprint, indexing, inverted list, matching, version, cover song	[html]	[ipynb]
S Train Firm	Musically Informed Audio Decomposition	Harmonic/percussive separation, signal reconstruction, instantaneous frequency, fundamental frequency (F0), trajectory, nonnegative matrix factorization (NMF)	[html]	[ipynb]



- Part B: Basic introductions to
 - Jupyter notebook framework
 - Python programming
 - Other technical concepts underlying these notebooks

Part	Title	Notions, Techniques & Algorithms	HTML	IPYNB
B 👶 jupyter	Basics	Basic information on Python, Jupyter notebooks, Anaconda package management system, Python environments, visualizations, and other topics	[html]	[ipynb]
0 19.1	Overview	Overview of the notebooks (https://www.audiolabs- erlangen.de/FMP)	[html]	[ipynb]
1 🗱	Music Representations	Music notation, MIDI, audio signal, waveform, pitch, loudness, timbre	[html]	[ipynb]
2	Fourier Analysis of Signals	Discrete/analog signal, sinusoid, exponential, Fourier transform, Fourier representation, DFT, FFT, STFT	[html]	[ipynb]
3	Music Synchronization	Chroma feature, dynamic programming, dynamic time warping (DTW), alignment, user interface	[html]	[ipynb]
4	Music Structure Analysis	Similarity matrix, repetition, thumbnail, homogeneity, novelty, evaluation, precision, recall, F- measure, visualization, scape plot	[html]	[ipynb]
5	Chord Recognition	Harmony, music theory, chords, scales, templates, hidden Markov model (HMM), evaluation	[html]	[ipynb]
6	Tempo and Beat Tracking	Onset, novelty, tempo, tempogram, beat, periodicity, Fourier analysis, autocorrelation	[html]	[ipynb]
7	Content-Based Audio Retrieval	Identification, fingerprint, indexing, inverted list, matching, version, cover song	[html]	[ipynb]
8	Musically Informed Audio Decomposition	Harmonic/percussive separation, signal reconstruction, instantaneous frequency, fundamental frequency (F0), trajectory, nonnegative matrix factorization (NMF)	[html]	[ipynb]



- Part B: Basic introductions to
 - Jupyter notebook framework
 - Python programming
 - Other technical concepts underlying these notebooks
- Part 0: Starting notebook

Part	Title	Notions, Techniques & Algorithms	HTML	IPYNB
B jupyter	<u>Basics</u>	Basic information on Python, Jupyter notebooks, Anaconda package management system, Python environments, visualizations, and other topics	[html]	[ipynb]
0 19:33 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	<u>Overview</u>	Overview of the notebooks (https://www.audiolabs- erlangen.de/FMP)	[html]	[ipynb]
1 🚁	Music Representations	Music notation, MIDI, audio signal, waveform, pitch, loudness, timbre	[html]	[ipynb]
2	Fourier Analysis of Signals	Discrete/analog signal, sinusoid, exponential, Fourier transform, Fourier representation, DFT, FFT, STFT	[html]	[ipynb]
3	Music Synchronization	Chroma feature, dynamic programming, dynamic time warping (DTW), alignment, user interface	[html]	[ipynb]
4	Music Structure Analysis	Similarity matrix, repetition, thumbnail, homogeneity, novelty, evaluation, precision, recall, F- measure, visualization, scape plot	[html]	[ipynb]
5	Chord Recognition	Harmony, music theory, chords, scales, templates, hidden Markov model (HMM), evaluation	[html]	[ipynb]
6	Tempo and Beat Tracking	Onset, novelty, tempo, tempogram, beat, periodicity, Fourier analysis, autocorrelation	[html]	[ipynb]
7	Content-Based Audio Retrieval	Identification, fingerprint, indexing, inverted list, matching, version, cover song	[html]	[ipynb]
8	Musically Informed Audio Decomposition	Harmonic/percussive separation, signal reconstruction, instantaneous frequency, fundamental frequency (F0), trajectory, nonnegative matrix factorization (NMF)	[html]	[ipynb]

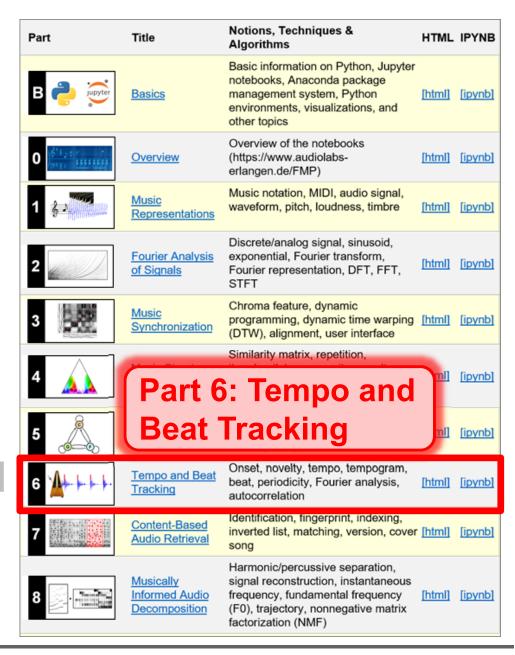


- Part B: Basic introductions to
 - Jupyter notebook framework
 - Python programming
 - Other technical concepts underlying these notebooks
- Part 0: Starting notebook
- Part 1 to Part 8:
 Different music processing scenarios

Part	Title	Notions, Techniques & Algorithms	HTML	IPYNB
B 🔁 jupyter	Basics	Basic information on Python, Jupyter notebooks, Anaconda package management system, Python environments, visualizations, and other topics	[html]	[ipynb]
0	Overview	Overview of the notebooks (https://www.audiolabs- erlangen.de/FMP)	[html]	[ipynb]
1 🚁	Music Representations	Music notation, MIDI, audio signal, waveform, pitch, loudness, timbre	[html]	[ipynb]
2	Fourier Analysis of Signals	Discrete/analog signal, sinusoid, exponential, Fourier transform, Fourier representation, DFT, FFT, STFT	[html]	[ipynb]
3	Music Synchronization	Chroma feature, dynamic programming, dynamic time warping (DTW), alignment, user interface	[html]	[ipynb]
4	Music Structure Analysis	Similarity matrix, repetition, thumbnail, homogeneity, novelty, evaluation, precision, recall, F- measure, visualization, scape plot	[html]	[ipynb]
5	Chord Recognition	Harmony, music theory, chords, scales, templates, hidden Markov model (HMM), evaluation	[html]	[ipynb]
6	Tempo and Beat Tracking	Onset, novelty, tempo, tempogram, beat, periodicity, Fourier analysis, autocorrelation	[html]	[ipynb]
7	Content-Based Audio Retrieval	Identification, fingerprint, indexing, inverted list, matching, version, cover song	[html]	[ipynb]
8	Musically Informed Audio Decomposition	Harmonic/percussive separation, signal reconstruction, instantaneous frequency, fundamental frequency (F0), trajectory, nonnegative matrix factorization (NMF)	[html]	[ipynb]

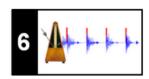


- Part B: Basic introductions to
 - Jupyter notebook framework
 - Python programming
 - Other technical concepts underlying these notebooks
- Part 0: Starting notebook
- Part 1 to Part 8:
 Different music processing scenarios

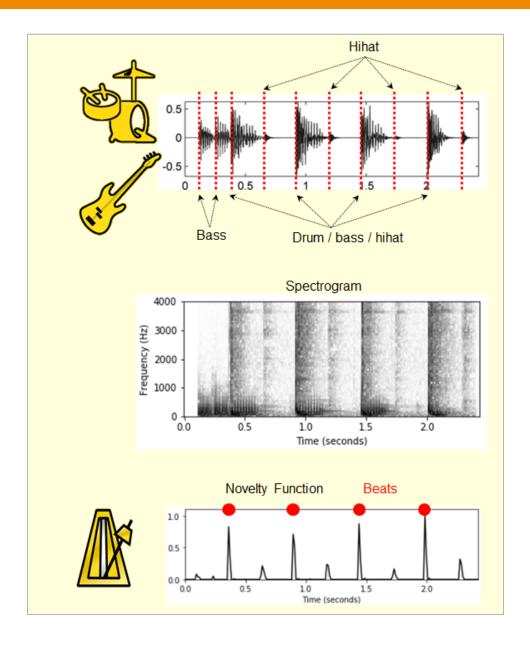




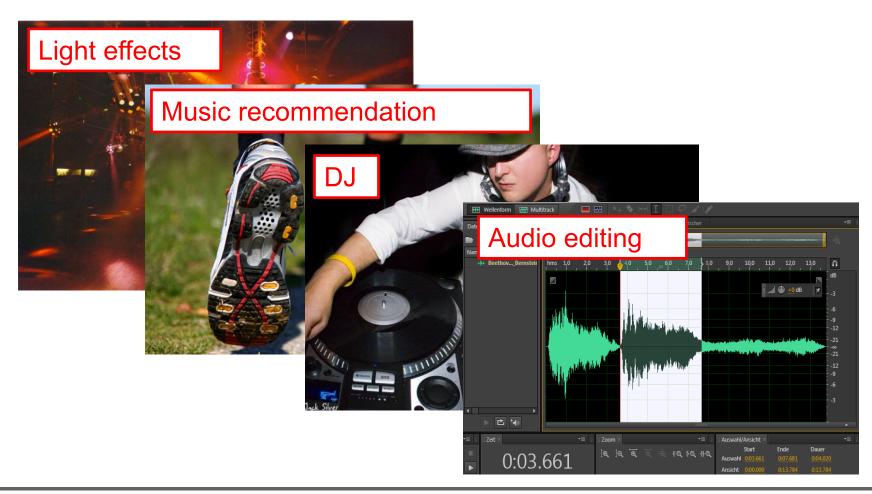
Part 6: Tempo and Beat Tracking



- When listening to a piece of music, we as humans are often able to tap along with the musical beat
- Automated beat tracking:
 Simulate this cognitive process by a computer



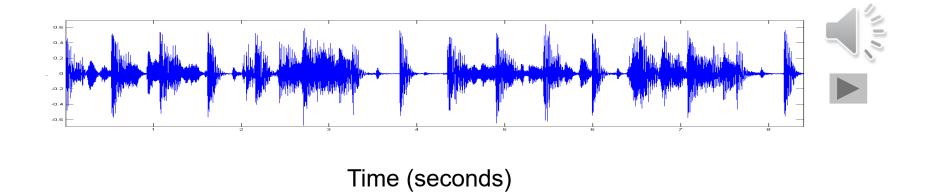
Basic task: "Tapping the foot when listening to music"





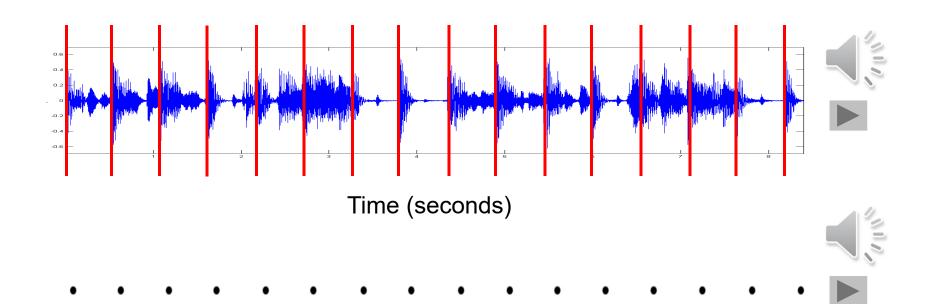
Basic task: "Tapping the foot when listening to music"

Example: Queen – Another One Bites The Dust



Basic task: "Tapping the foot when listening to music"

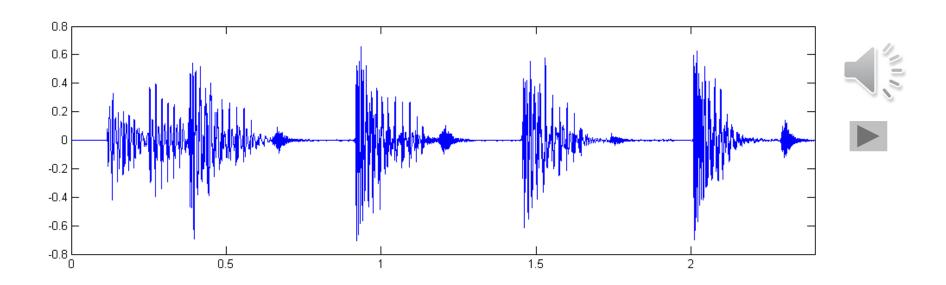
Example: Queen – Another One Bites The Dust





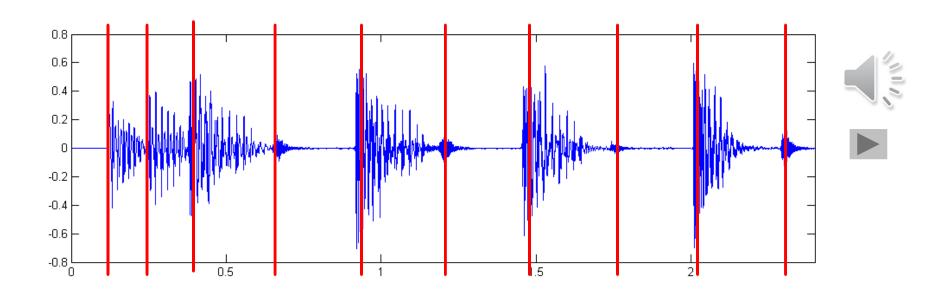
Tasks

- Onset detection
- Beat tracking
- Tempo estimation



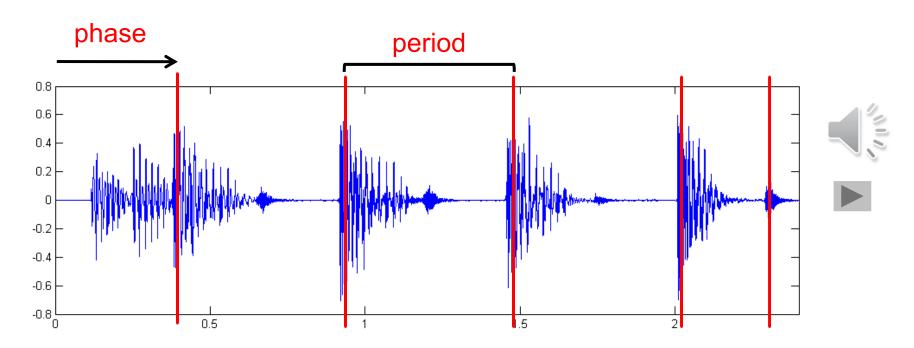
Tasks

- Onset detection
- Beat tracking
- Tempo estimation



Tasks

- Onset detection
- Beat tracking
- Tempo estimation

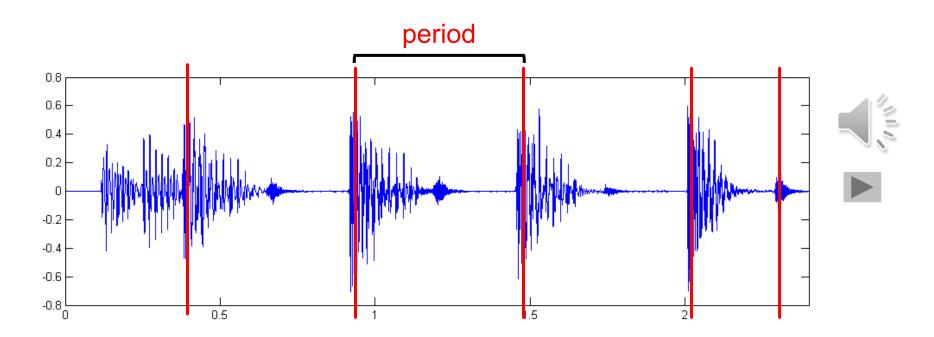


Tasks

- Onset detection
- Beat tracking
- Tempo estimation

Tempo := 60 / period

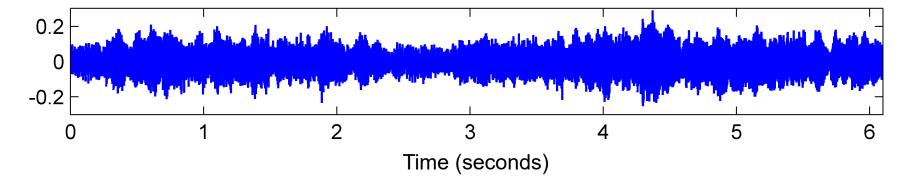
Beats per minute (BPM)

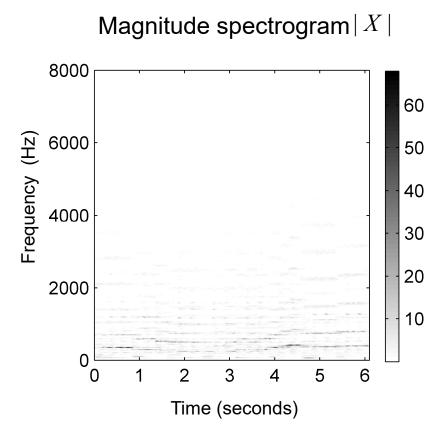




Audio recording



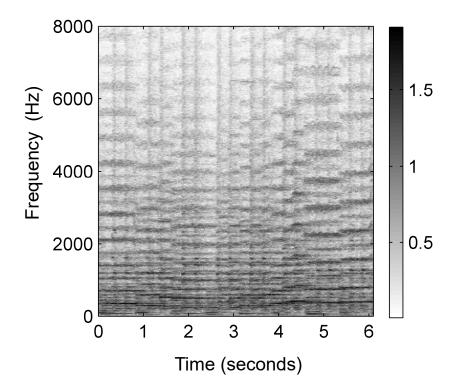




Steps:

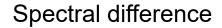
1. Spectrogram

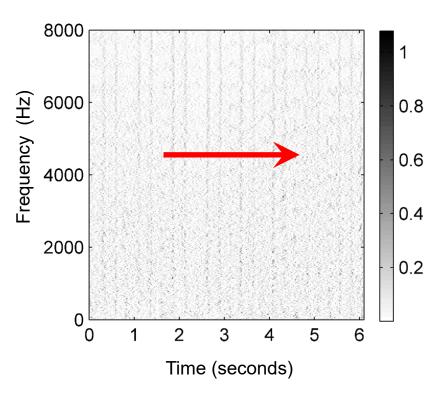
Compressed spectrogram Y



Steps:

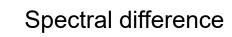
- 1. Spectrogram
- 2. Logarithmic compression

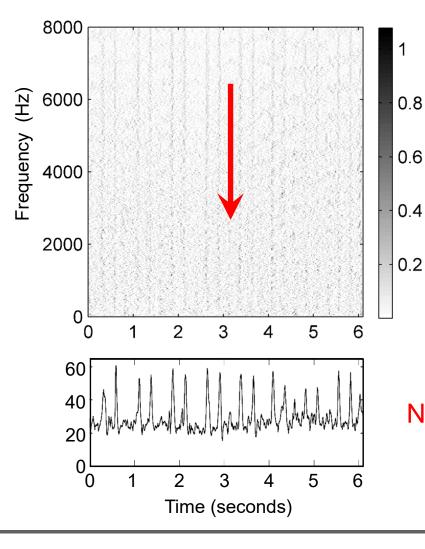




Steps:

- 1. Spectrogram
- 2. Logarithmic compression
- Differentiation & half wave rectification





Steps:

- 1. Spectrogram
- 2. Logarithmic compression
- 3. Differentiation & half wave rectification
- Accumulation

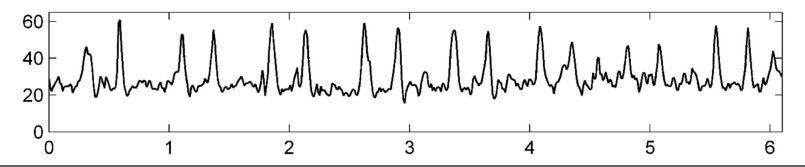
Novelty curve



Steps:

- 1. Spectrogram
- 2. Logarithmic compression
- Differentiation & half wave rectification
- 4. Accumulation

Novelty function

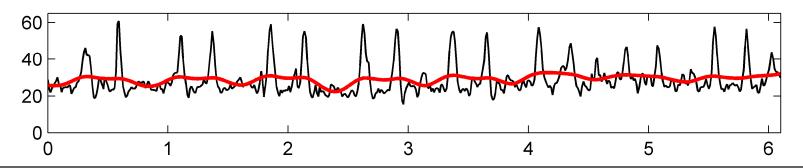


Steps:

- 1. Spectrogram
- 2. Logarithmic compression
- Differentiation & half wave rectification
- Accumulation
- Normalization

Novelty function

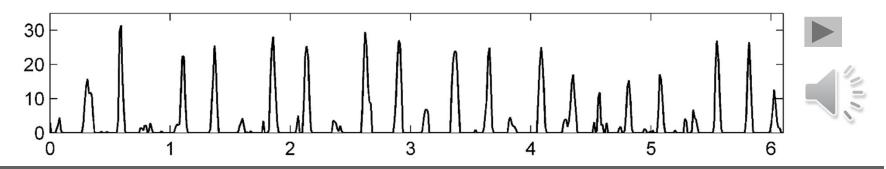
Substraction of local average



Steps:

- 1. Spectrogram
- 2. Logarithmic compression
- Differentiation & half wave rectification
- Accumulation
- Normalization

Normalized novelty function





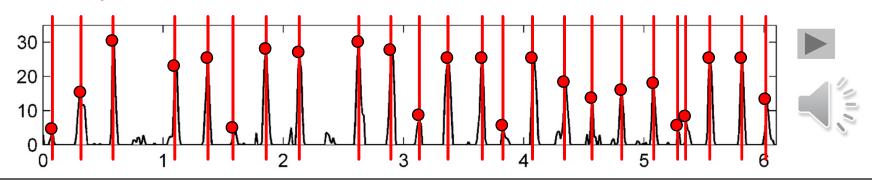
Onset Detection (Spectral Flux)

Steps:

- 1. Spectrogram
- 2. Logarithmic compression
- Differentiation & half wave rectification
- Accumulation
- Normalization

Normalized novelty function

Peak positions indicate beat candidates



Onset Detection (Spectral Flux)

Deep Learning

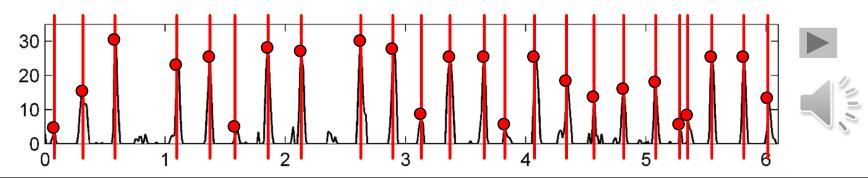
- 1. Input representation
- 2. Sigmoid activation
- Convolution & rectified linear unit (ReLU)
- 4. Pooling
- Convolution & ReLU

Steps:

- 1. Spectrogram
- 2. Logarithmic compression
- Differentiation & half wave rectification
- Accumulation
- Normalization

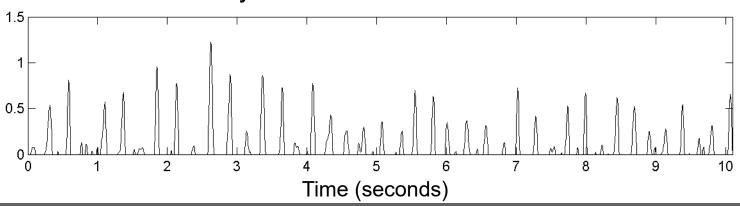
Normalized novelty function

Peak positions indicate beat candidates

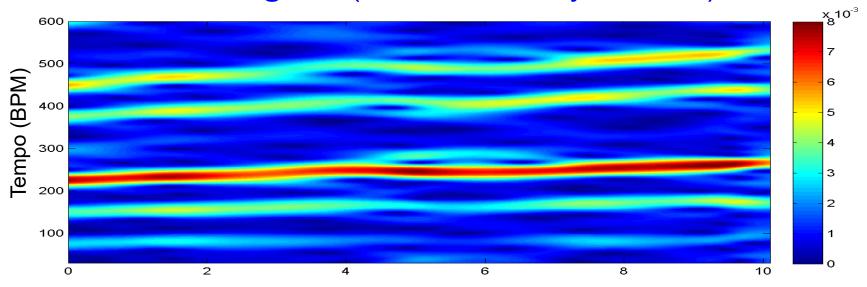




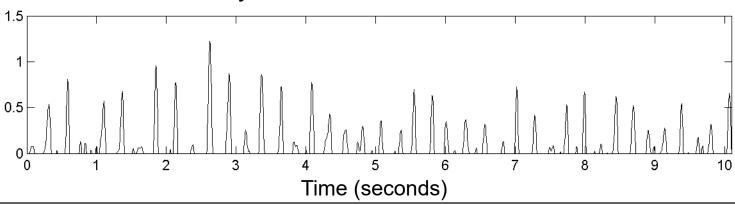
Normalized novelty function



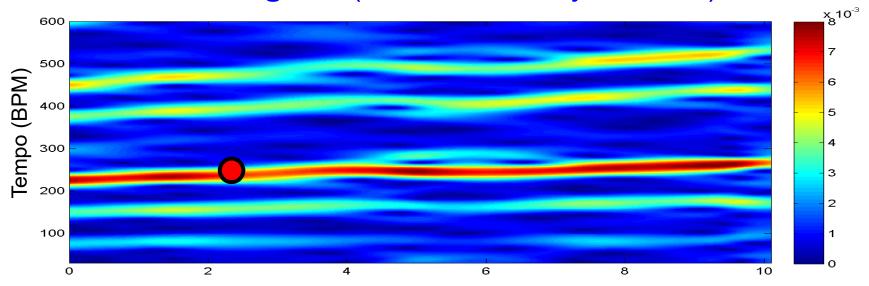
Fourier temogram (STFT of novelty function)



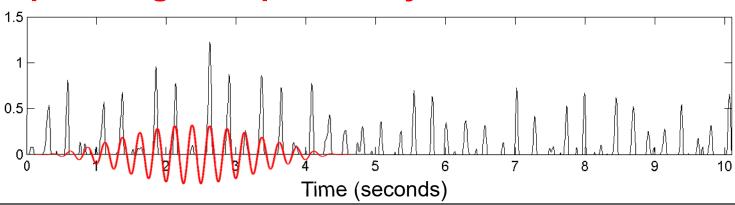
Normalized novelty function



Fourier temogram (STFT of novelty function)

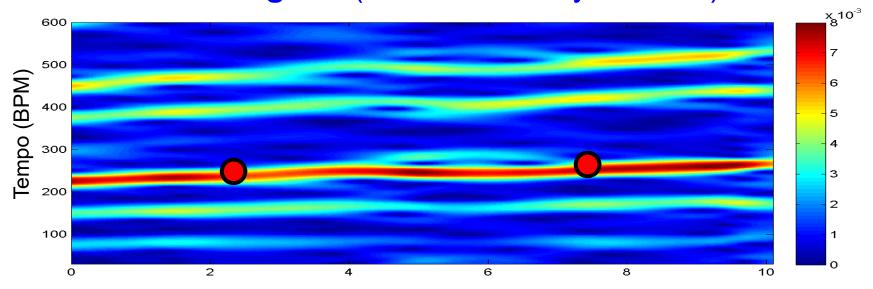


Optimizing local periodicity kernel

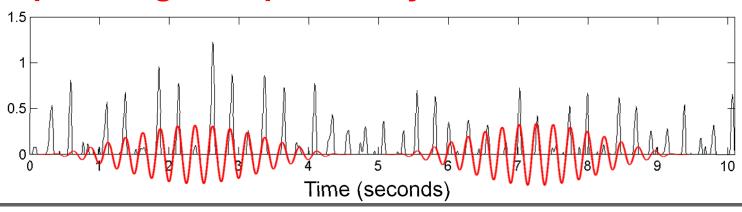




Fourier temogram (STFT of novelty function)

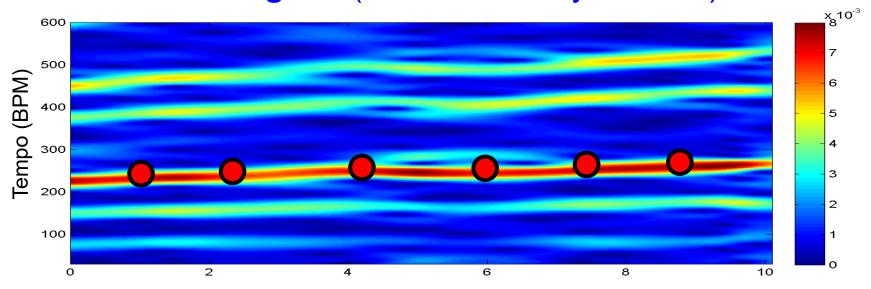


Optimizing local periodicity kernel

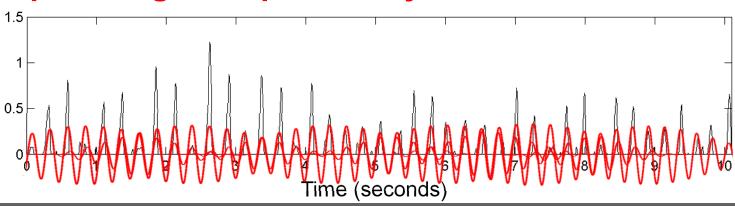




Fourier temogram (STFT of novelty function)

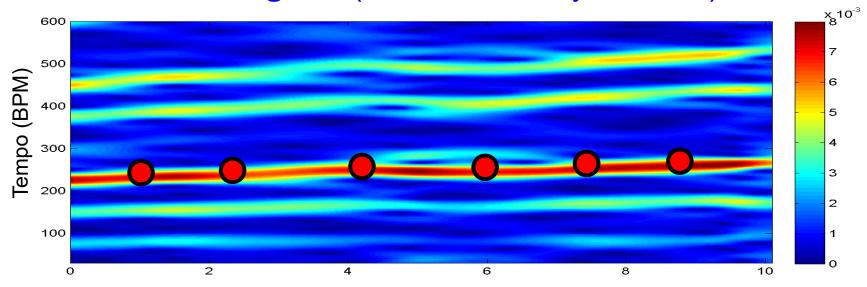


Optimizing local periodicity kernel

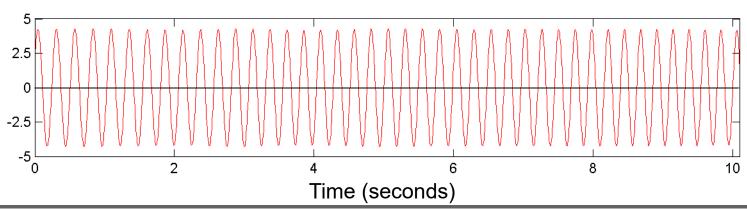




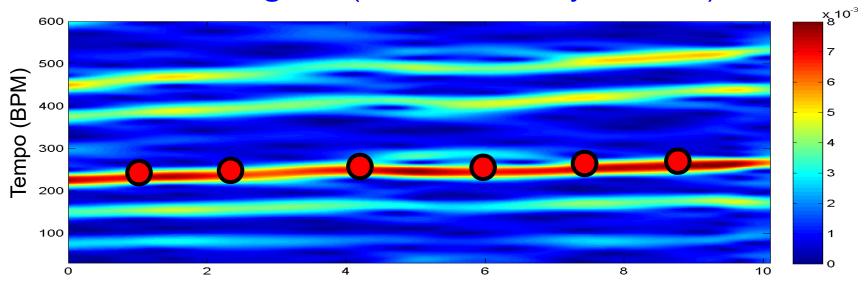
Fourier temogram (STFT of novelty function)



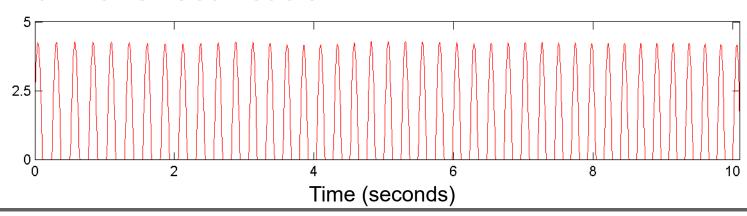
Accumulation of kernels



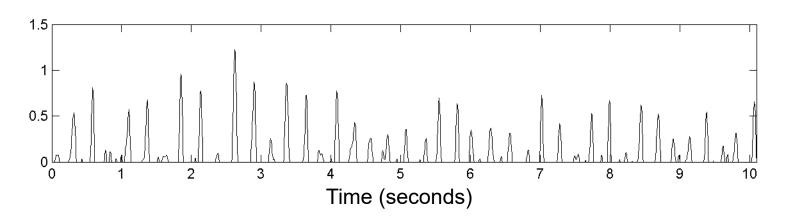
Fourier temogram (STFT of novelty function)



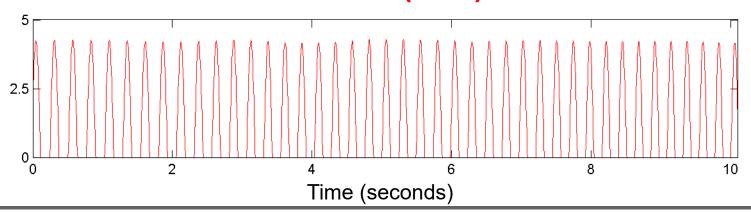
Halfwave rectification



Novelty Curve



Predominant Local Pulse (PLP)



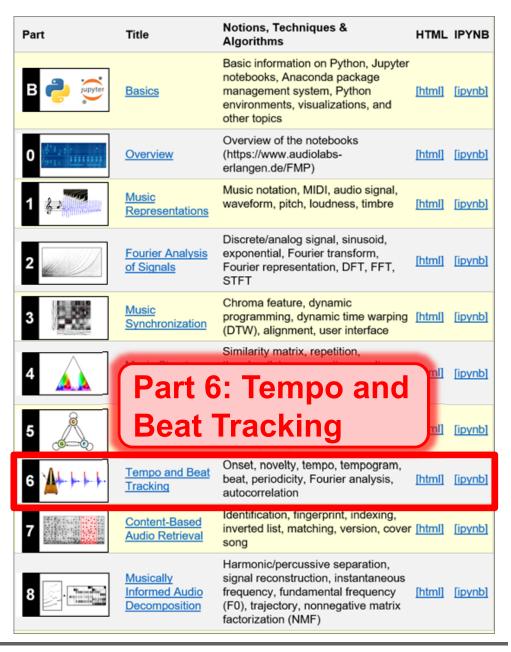




FMP Notebooks

Structured in 10 parts

- Part B: Basic introductions to
 - Jupyter notebook framework
 - Python programming
 - Other technical concepts underlying these notebooks
- Part 0: Starting notebook
- Part 1 to Part 8:
 Different music processing scenarios





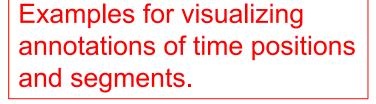
Part B: Basics

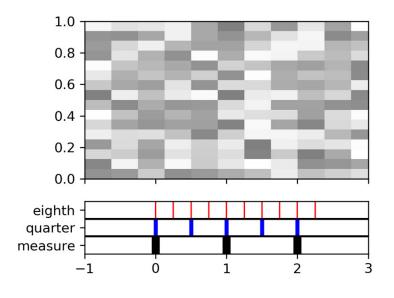


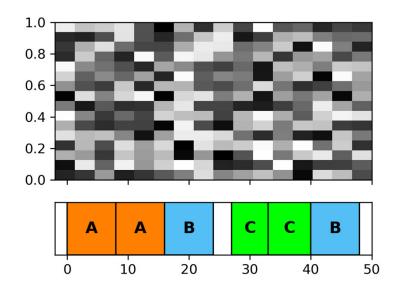
Topic	Description
Get Started	Explanation on how to install and use the FMP notebooks
Installation	Installation of Python using Conda
Jupyter Notebook	Usage of Jupyter notebook framework
Python Basics	Introduction of data types, control structures, and functions
Python Style Guide	Recommendations for programming style
<u>Multimedia</u>	Integration of multimedia objects into notebooks
Python Visualization	Generation of figures and images
Python Audio	Reading and writing audio files
<u>Numba</u>	Acceleration of Python functions via JIT compilation
Annotation Visualization	Visualization of annotations (single value, segments)
<u>Sonification</u>	Sonification methods (onsets, F0 trajectories, pitch, chroma)
<u>libfmp</u>	Library of FMP-specific Python functions
MIR Resources	Links to resources that are useful for MIR

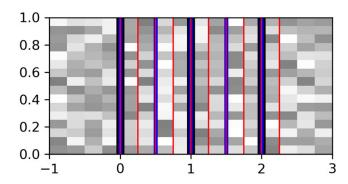


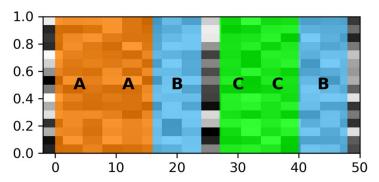
Part B: Basics Annotation Visualization









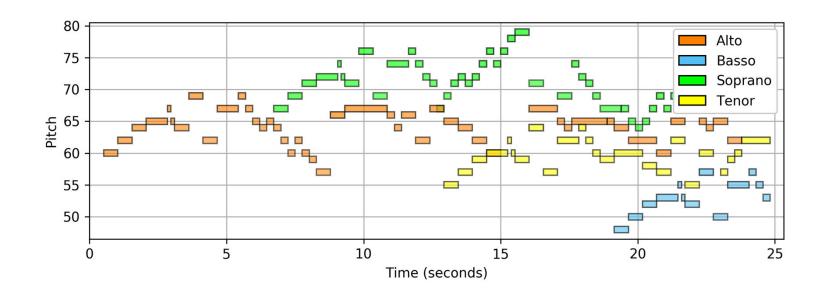




Part 1: Music Representations

Symbolic Format: CSV





Visualization of a piano-roll representation (Fugue BWV 846 by Bach).









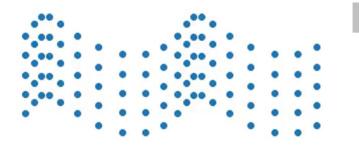


Part 1: Music Representations

Waves and Waveforms





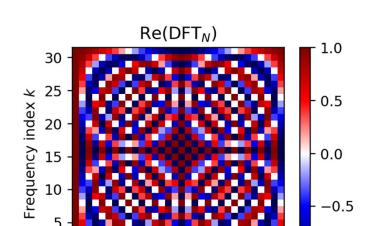


Videos illustrating the concepts of transverse, longitudinal, and combined waves.



Part 2: Fourier Analysis of Signals

Discrete Fourier Transform (DFT)

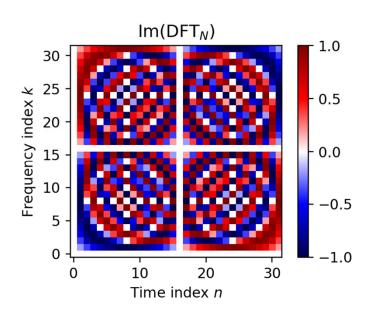


20

Time index n

10

0



The matrix DFT_N and a visualization of its real and imaginary parts for the case N = 32

30

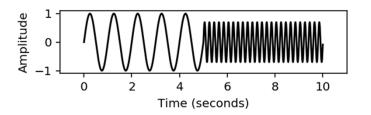
-1.0

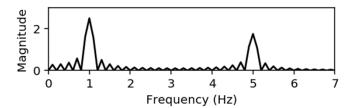


Part 2: Fourier Analysis of Signals

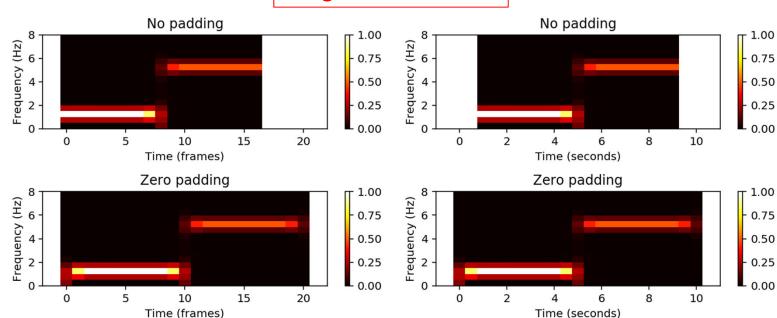
STFT: Padding







Magnitude STFT.



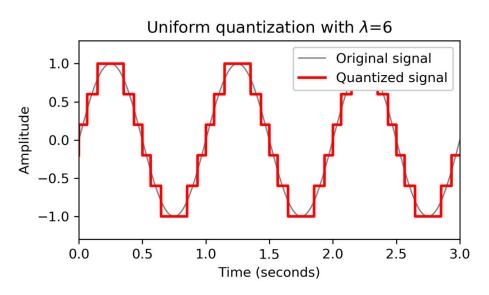


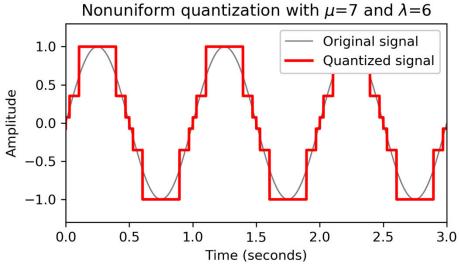
Part 2: Fourier Analysis of Signals

Digital Signals: Quantization



Uniform and nonuniform quantization (based on μ -law encoding) using $\lambda = 6$ quantization levels.



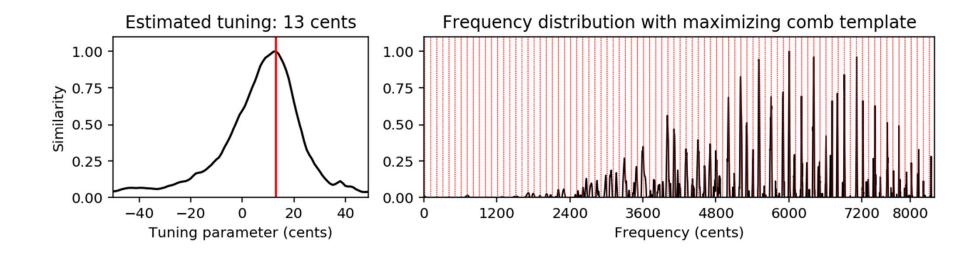


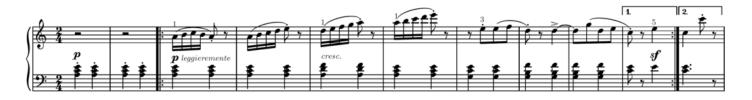


Part 3: Music Synchronization

Transposition and Tuning









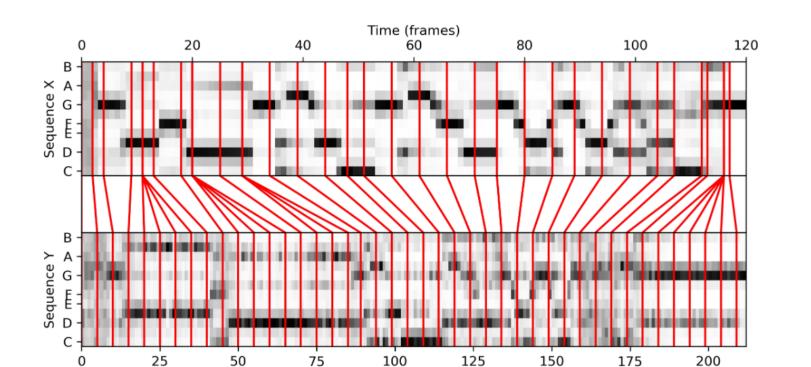




Part 3: Music Synchronization

Music Synchronization

Music synchronization result obtained for two input chromagrams (obtained from two recordings of the beginning of Beethoven's Fifth Symphony).



Time (frames)









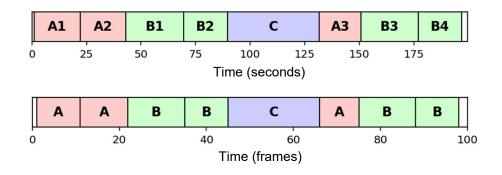
Part 4: Music Structure Analysis

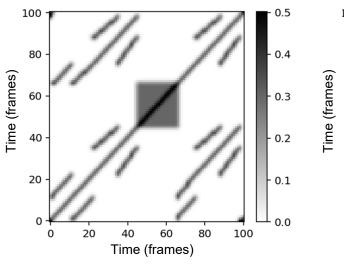
SSM: Synthetic Generation

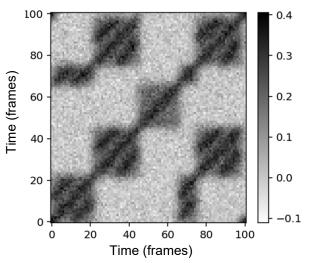
Structure annotation and different synthetically generated SSMs.



	start	end	label
0	0.00	1.01	
1	1.01	22.11	A1
2	22.11	43.06	A2
3	43.06	69.42	B1
4	69.42	89.57	B2
5	89.57	131.64	С
6	131.64	150.84	А3
7	150.84	176.96	В3
8	176.96	196.90	B4
9	196.90	199.64	







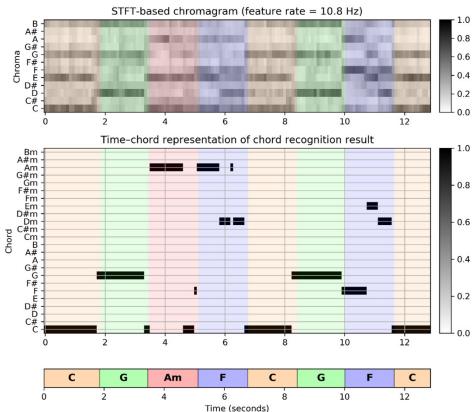


Part 5: Chord Recognition

Template-Based Chord Recognition

Chord recognition task illustrated by the first measures of the Beatles song "Let It Be."





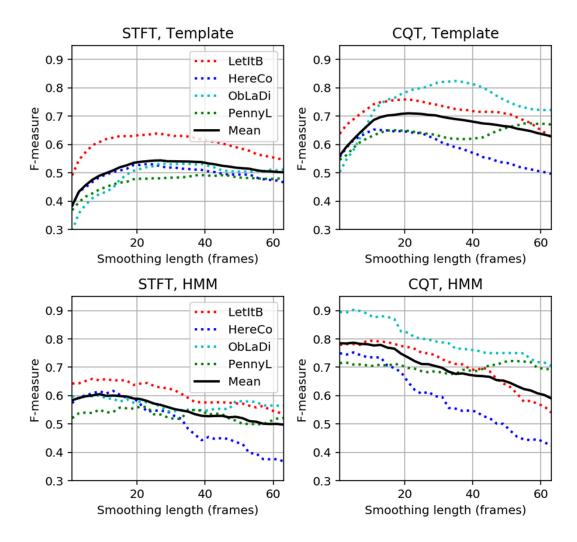


Part 5: Chord Recognition

Experiments: Beatles Collection

Prefiltering experiments for a template-based and an HMM-based chord recognizer applied to two different input chroma representations (STFT, CQT).

The evaluation is performed on the basis of four Beatles songs (LetItB, HereCo, ObLaDi, PennyL).

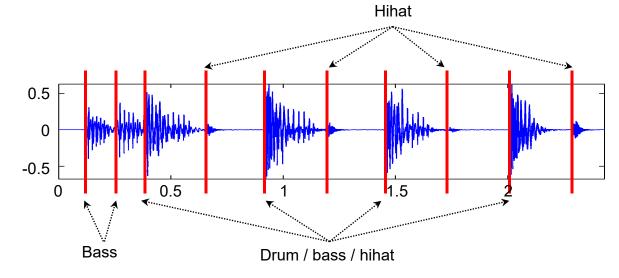




Part 6: Tempo and Beat Tracking

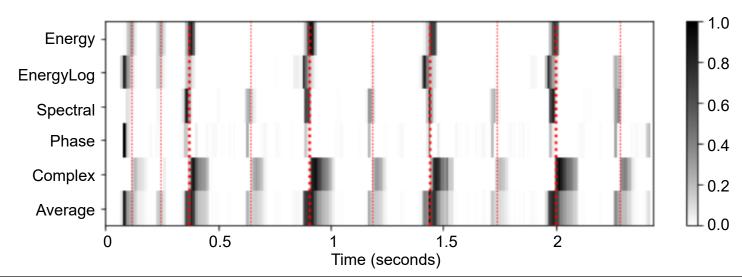
Novelty: Comparison of Approaches

Comparison of novelty detectors using a matrix-based visualization.





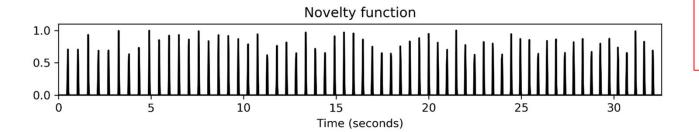






Part 6: Tempo and Beat Tracking

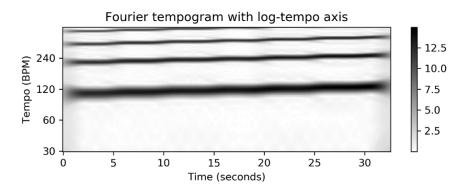
Cyclic Tempogram

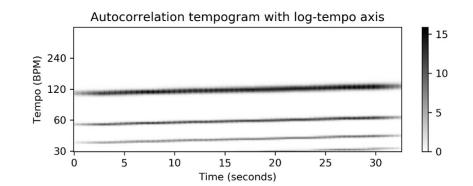


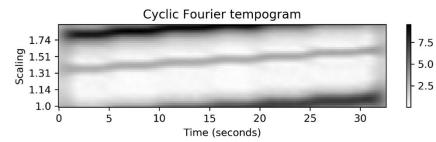


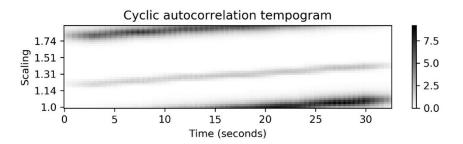
Different tempogram representations of a click track with increasing tempo.











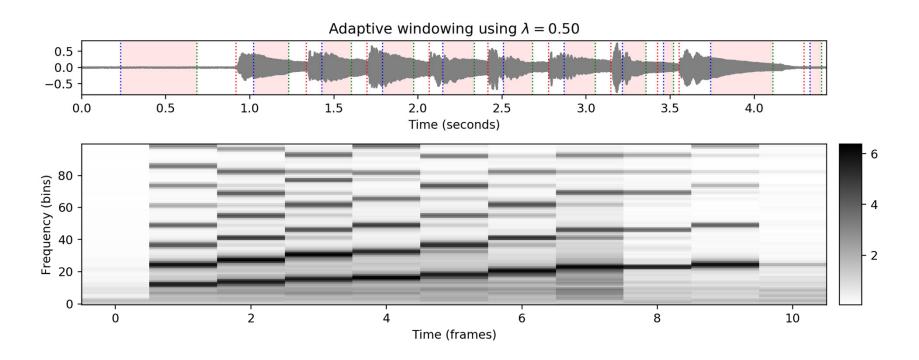


Part 6: Tempo and Beat Tracking

Adaptive Windowing

Example of adaptive windowing using a parameter λ to control the neighborhood's relative size to be excluded.



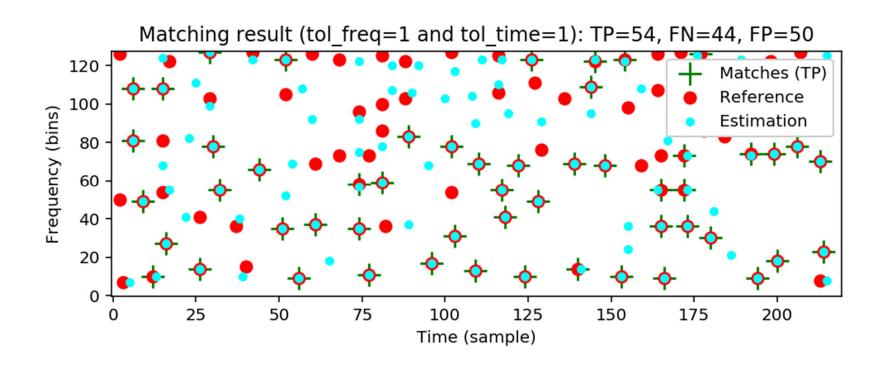




Part 7: Content-Based Audio Retrieval

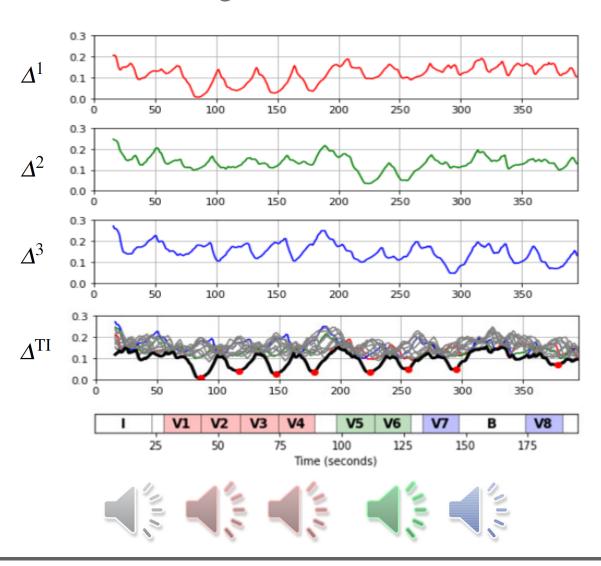
Audio Identification

Evaluation measures that indicate the agreement between two constellation maps computed for an original version (Reference) and a noisy version (Estimation).



Part 7: Content-Based Audio Retrieval

Audio Matching



Transposition-invariant matching function illustrated by Zager and Evans' song "In the Year 2525."





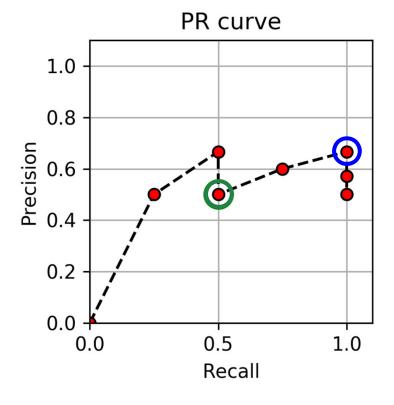
Part 7: Content-Based Audio Retrieval

Evaluation Measures

Various evaluation metrics applied to a toy example.

Rank	ID	Score	χQ	P(r)	R(r)	F(r)
1	6	3.70	False	0.00	0.00	0.00
		3.60				
3	4	3.50	True	0.67	0.50	0.57
4	5	3.20	False	0.50	0.50	0.50
		3.10				
6	2	2.60	True	0.67	1.00	0.80
7	7	1.50	False	0.57	1.00	0.73
8	1	0.70	False	0.50	1.00	0.67

Break-even point = 0.50 F_max = 0.80 Average precision = 0.60833

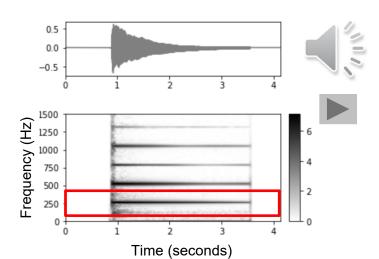


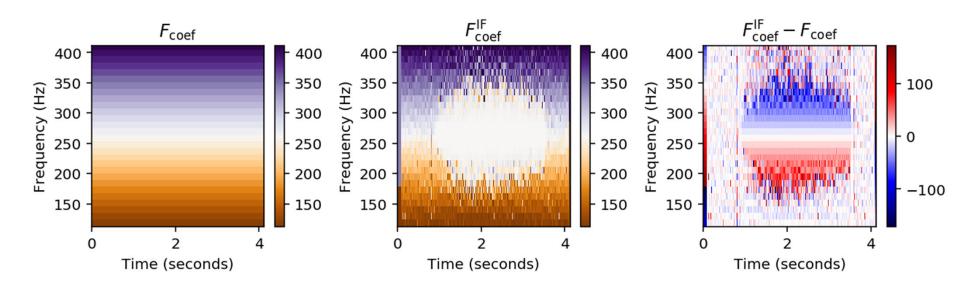


Part 8: Audio Decomposition

Instantaneous Frequency Estimation

Interpretation of time—frequency bins of an STFT using (frame-dependent) instantaneous frequency values.







Part 8: Audio Decomposition

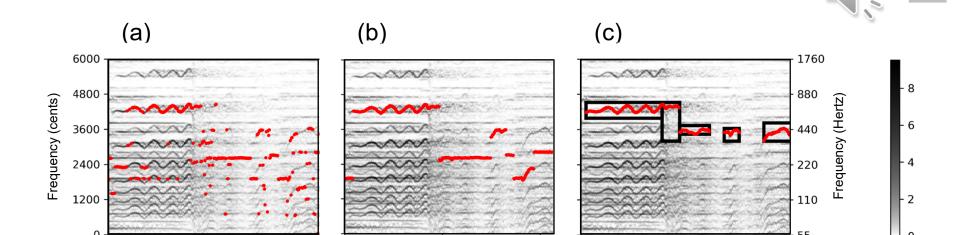
Fundamental Frequency Tracking



- (a) a frame-wise approach,
- (b) an approach using continuity constraints, and
- (c) a score-informed approach.



Figure 8.10a from [Müller, FMP, Springer 2015]





Time (seconds)

Time (seconds)

Time (seconds)

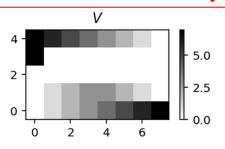
Part 8: Audio Decomposition

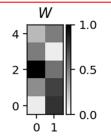
Nonnegative Matrix Factorization (NMF)

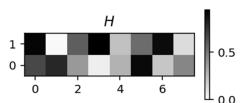
NMF procedure applied to a toy example.

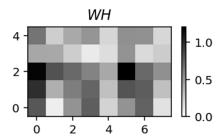


Matrix V and randomly initialized matrices W and H.

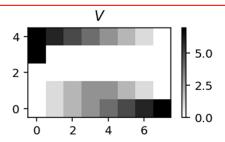


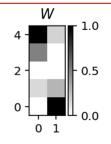


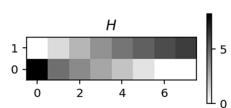


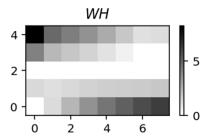


Matrix V and matrices W and H after training.

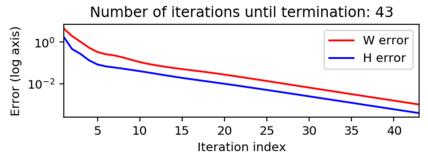




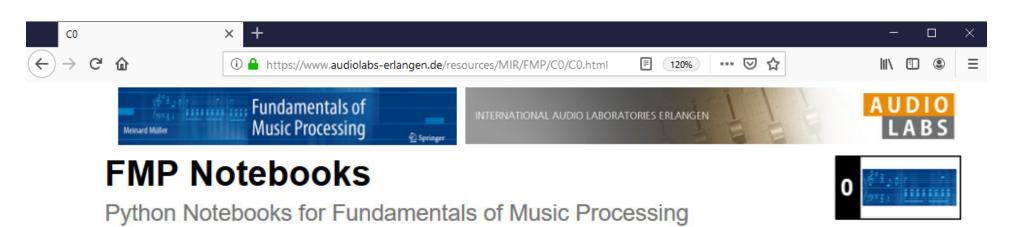




Error terms over iteration.







https://www.audiolabs-erlangen.de/FMP



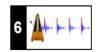






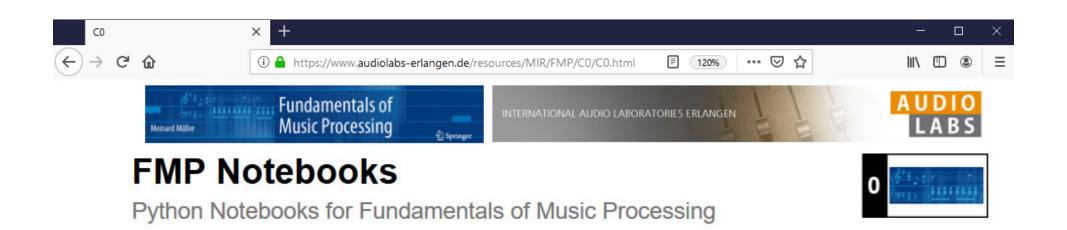




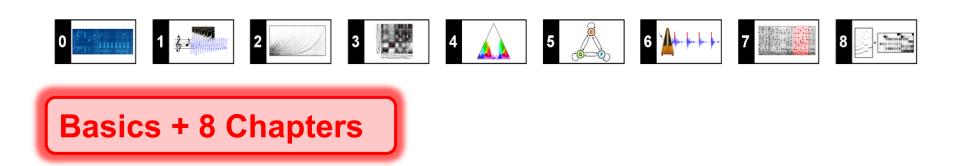


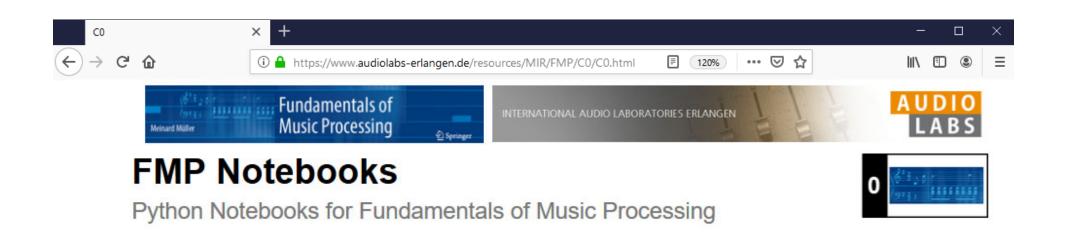




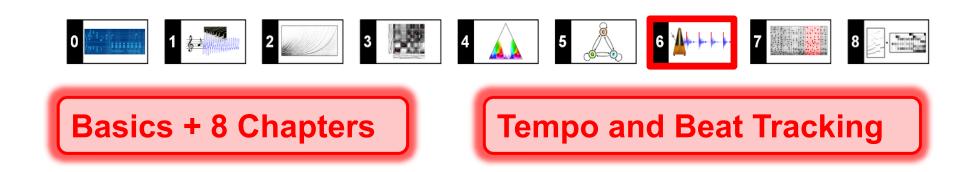


https://www.audiolabs-erlangen.de/FMP



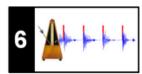


https://www.audiolabs-erlangen.de/FMP

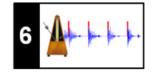




Tempo and Beat Tracking





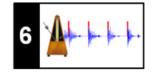


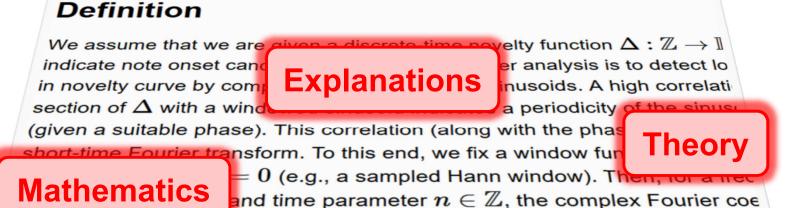
Definition

We assume that we are given a discrete-time novelty function $\Delta:\mathbb{Z}\to\mathbb{I}$ indicate note onset candidates. The idea of Fourier analysis is to detect lo in novelty curve by comparing it with windowed sinusoids. A high correlating section of Δ with a windowed sinusoid indicates a periodicity of the sinusoid (given a suitable phase). This correlation (along with the phase) can be considered as short-time Fourier transform. To this end, we fix a window function $w:\mathbb{Z}$ be length centered at n=0 (e.g., a sampled Hann window). Then, for a free parameter $\omega\in\mathbb{R}_{\geq 0}$ and time parameter $n\in\mathbb{Z}$, the complex Fourier coefficient by

$$\mathcal{F}(n,\omega) := \sum_{m \in \mathbb{Z}} \Delta(m) \overline{w}(m-n) \mathrm{exp}(-2\pi i \omega m).$$



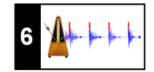


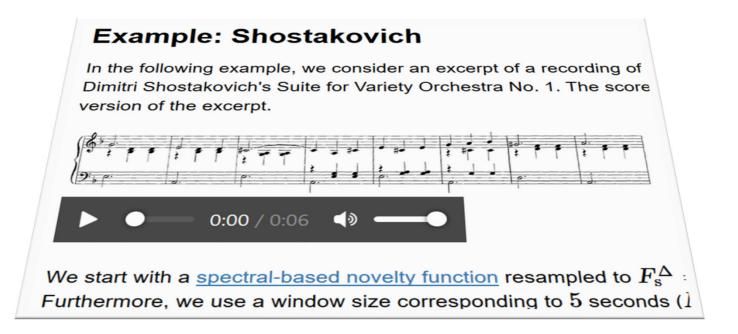


$$\mathcal{F}(n,\omega) := \sum_{m \in \mathbb{Z}} \Delta(m) \overline{w}(m-n) \mathrm{exp}(-2\pi i \omega m).$$

is aetinea by

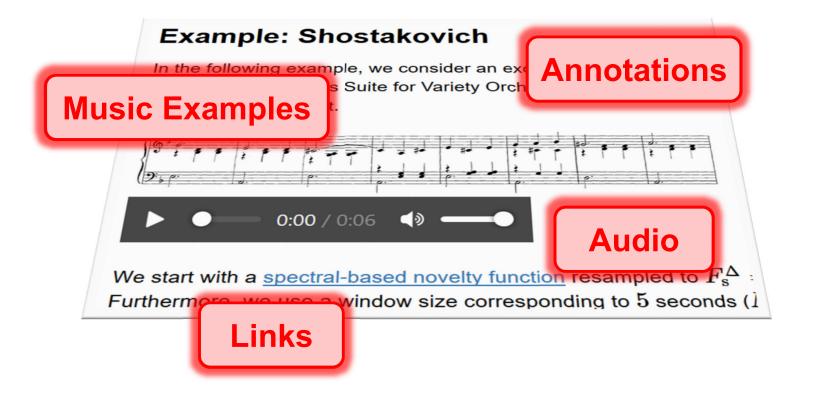






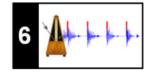




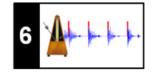






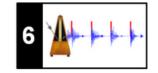


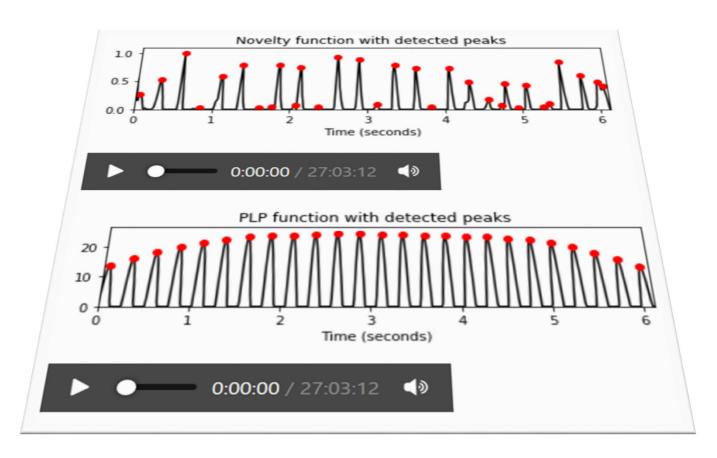




```
In [2]:
       def compute sinusoid
                                            n, Fs, N
           """Compute windows
                                            optimal p
                             Algorithms
                 k: C6/C6S2
                                            .ipynb
Python Code
                 Coefficient of tempogram (c=X(k,n))
              tempo: Tempo parameter corresponding to
      coef BPM[k])
                Frame parameter of c
              Fs: Samplin
                             Functions
                Window 1
             H: Hop size
```

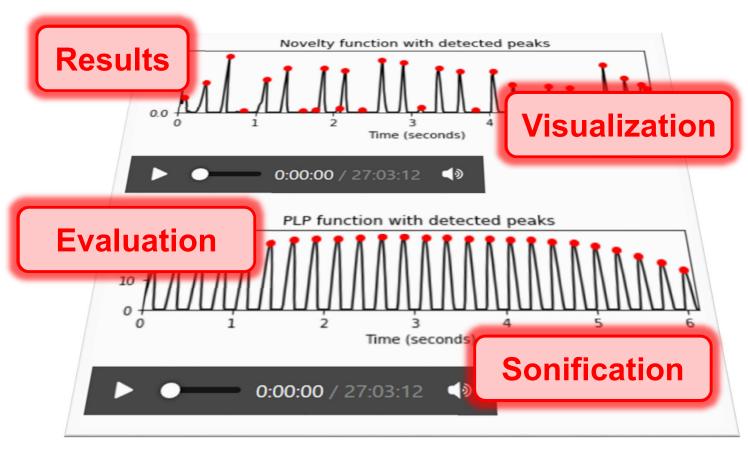




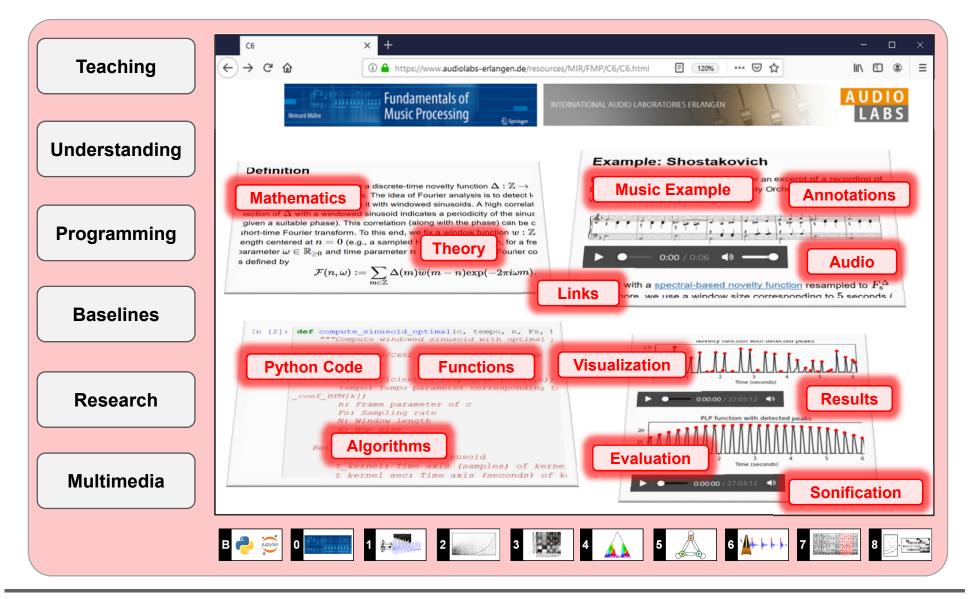








FMP Notebooks





References

Meinard Müller: Fundamentals of Music Processing – Using Python and Jupyter Notebooks.
 2nd Edition, Springer, 2021.

https://www.springer.com/gp/book/9783030698072

- Meinard Müller and Frank Zalkow: libfmp: A Python Package for Fundamentals of Music Processing.
 Journal of Open Source Software (JOSS), 6(63): 1–5, 2021.
 https://joss.theoj.org/papers/10.21105/joss.03326
- Meinard Müller: An Educational Guide Through the FMP Notebooks for Teaching and Learning Fundamentals of Music Processing. Signals, 2(2): 245–285, 2021.
 https://www.mdpi.com/2624-6120/2/2/18
- Meinard Müller and Frank Zalkow: FMP Notebooks: Educational Material for Teaching and Learning Fundamentals of Music Processing. Proc. International Society for Music Information Retrieval Conference (ISMIR): 573–580, 2019. https://zenodo.org/record/3527872#.YOhEQOgzaUk
- Meinard Müller, Brian McFee, and Katherine Kinnaird: Interactive Learning of Signal Processing Through Music: Making Fourier Analysis Concrete for Students. IEEE Signal Processing Magazine, 38(3): 73–84, 2021.

https://ieeexplore.ieee.org/document/9418542



Resources (Group Meinard Müller)

FMP Notebooks:

https://www.audiolabs-erlangen.de/FMP

libfmp:

https://github.com/meinardmueller/libfmp

synctoolbox:

https://github.com/meinardmueller/synctoolbox

libtsm:

https://github.com/meinardmueller/libtsm

Preparation Course Python (PCP) Notebooks:

https://www.audiolabs-erlangen.de/resources/MIR/PCP/PCP.html

https://github.com/meinardmueller/PCP



Resources

librosa:

https://librosa.org/

madmom:

https://github.com/CPJKU/madmom

Essentia Python tutorial:

https://essentia.upf.edu/essentia_python_tutorial.html

mirdata:

https://github.com/mir-dataset-loaders/mirdata

open-unmix:

https://github.com/sigsep/open-unmix-pytorch

Open Source Tools & Data for Music Source Separation:

https://source-separation.github.io/tutorial/landing.html









