INTERNATIONAL AUDIO LABORATORIES ERLANGEN



Lecture Music Processing

Music Synchronization

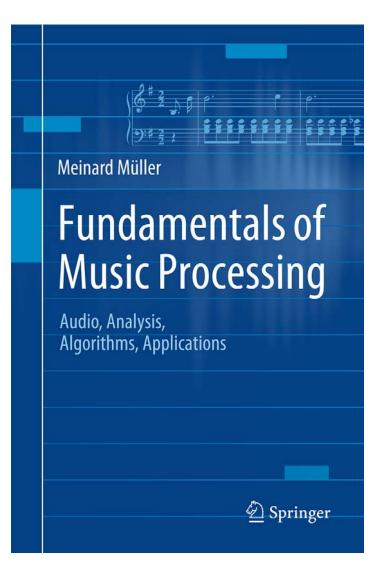
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Book: Fundamentals of Music Processing



Meinard Müller Fundamentals of Music Processing Audio, Analysis, Algorithms, Applications 483 p., 249 illus., hardcover ISBN: 978-3-319-21944-8 Springer, 2015

Accompanying website: www.music-processing.de

Book: Fundamentals of Music Processing

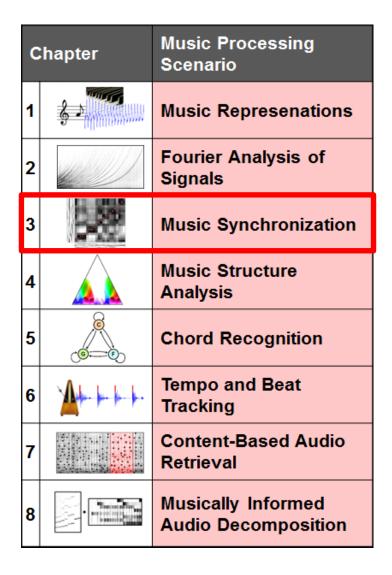
Chapter		Music Processing Scenario
1	<u> </u>	Music Represenations
2		Fourier Analysis of Signals
3		Music Synchronization
4		Music Structure Analysis
5		Chord Recognition
6		Tempo and Beat Tracking
7		Content-Based Audio Retrieval
8		Musically Informed Audio Decomposition

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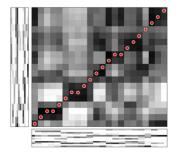
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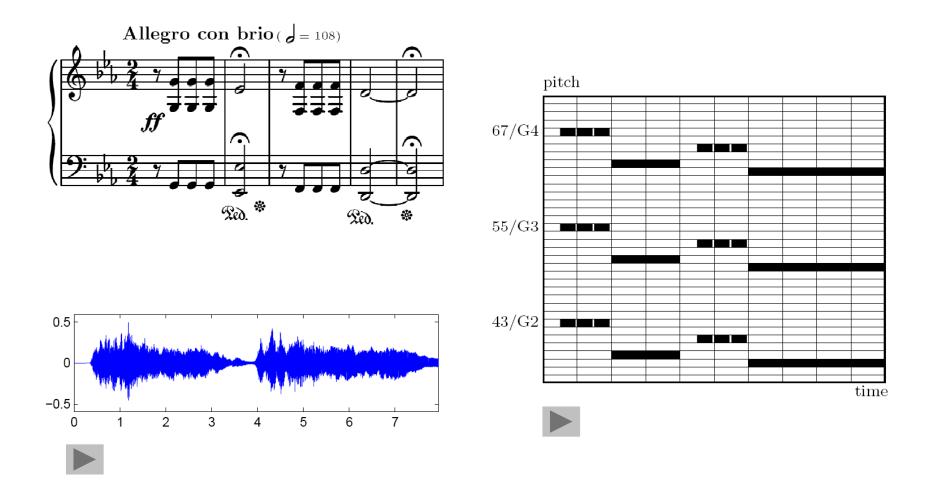
Chapter 3: Music Synchronization

- 3.1 Audio Features
- 3.2 Dynamic Time Warping
- 3.3 Applications
- 3.4 Further Notes



As a first music processing task, we study in Chapter 3 the problem of music synchronization. The objective is to temporally align compatible representations of the same piece of music. Considering this scenario, we explain the need for musically informed audio features. In particular, we introduce the concept of chroma-based music features, which capture properties that are related to harmony and melody. Furthermore, we study an alignment technique known as dynamic time warping (DTW), a concept that is applicable for the analysis of general time series. For its efficient computation, we discuss an algorithm based on dynamic programming—a widely used method for solving a complex problem by breaking it down into a collection of simpler subproblems.

Music Data



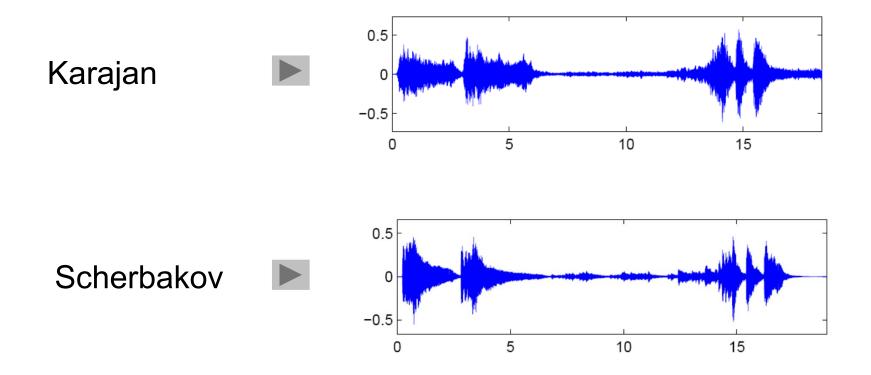
Music Data

Various interpretations – Beethoven's Fifth

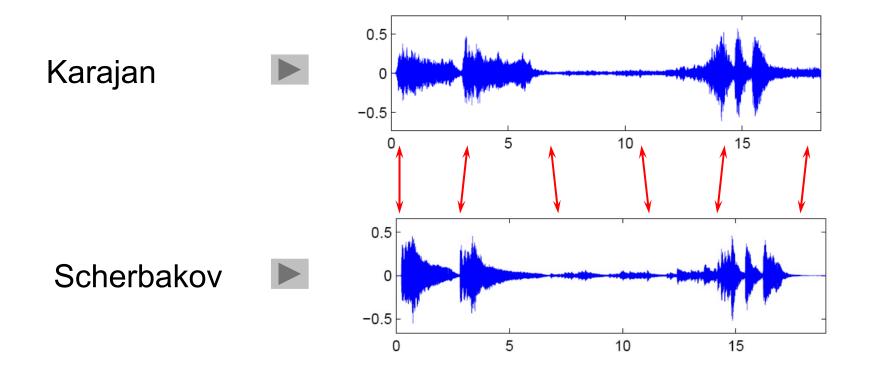
Bernstein	
Karajan	
Scherbakov (piano)	
MIDI (piano)	

- **Given:** Two different audio recordings of the same underlying piece of music.
- **Goal:** Find for each position in one audio recording the musically corresponding position in the other audio recording.

Music Synchronization: Audio-Audio Beethoven's Fifth



Music Synchronization: Audio-Audio Beethoven's Fifth



Synchronization: Karajan \rightarrow Scherbakov

Application: Interpretation Switcher

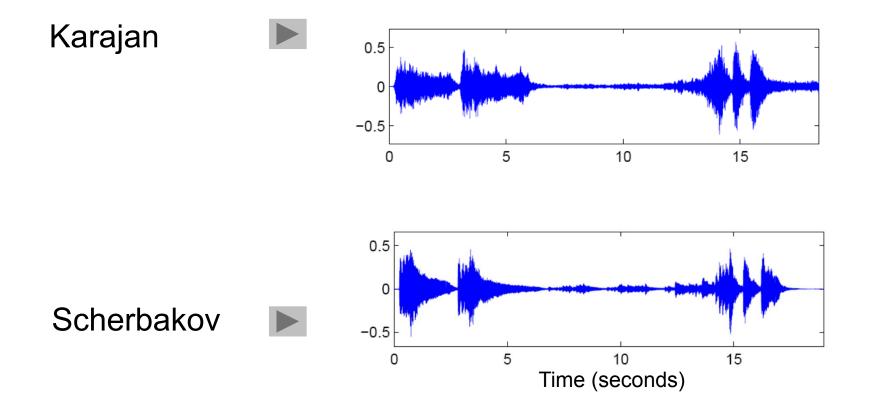


Two main steps:

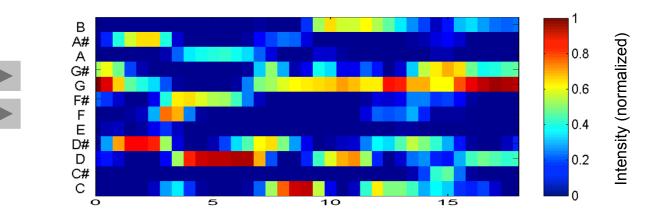
1.) Audio features

- Robust but discriminative
- Chroma features
- Robust to variations in instrumentation, timbre, dynamics
- Correlate to harmonic progression
- 2.) Alignment procedure
 - Deals with local and global tempo variations
 - Needs to be efficient

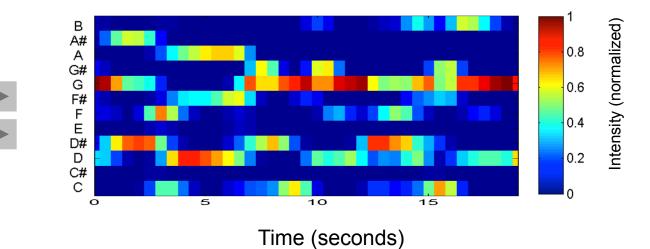
Music Synchronization: Audio-Audio Beethoven's Fifth



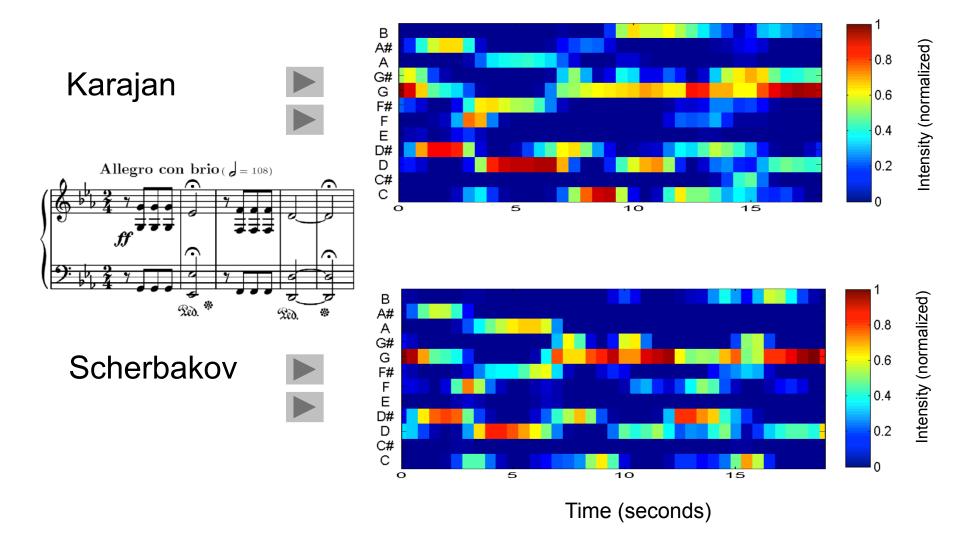
Beethoven's Fifth

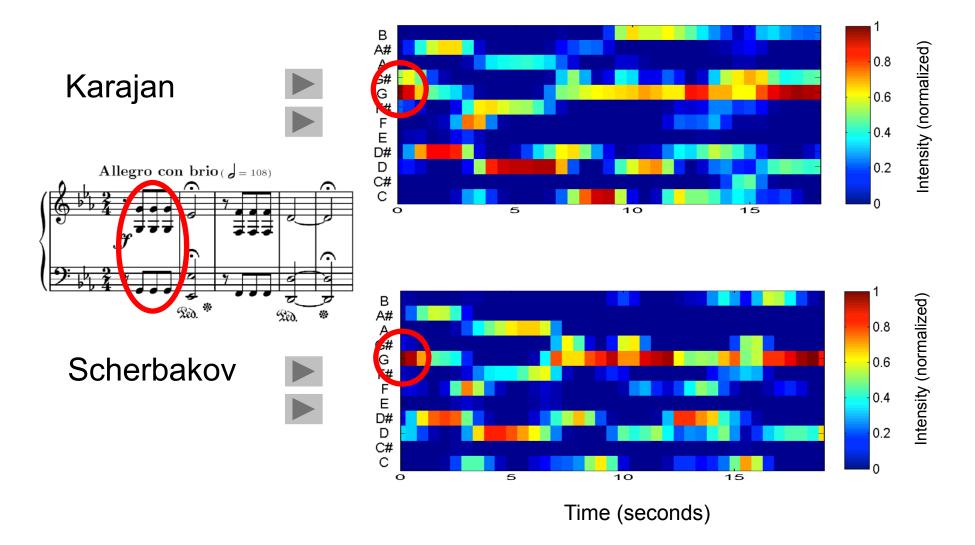


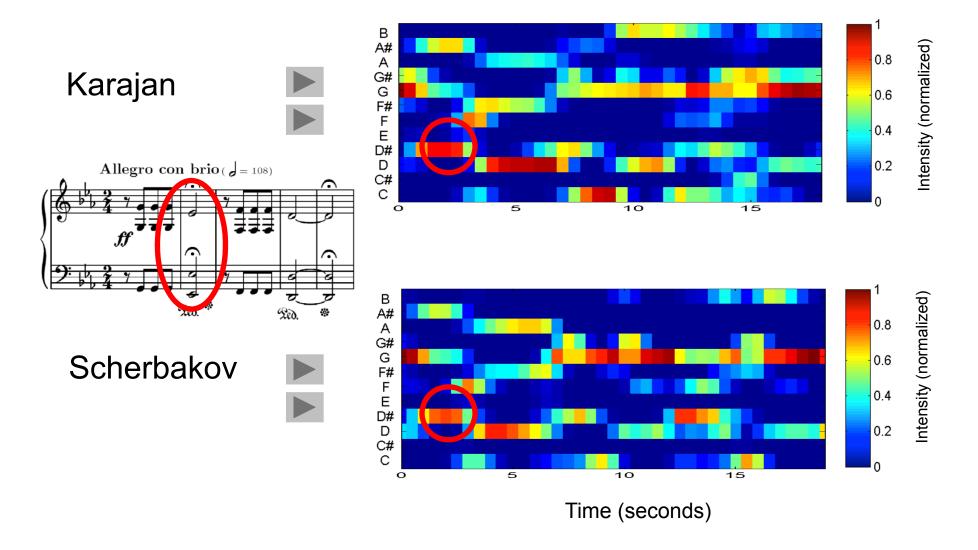
Karajan

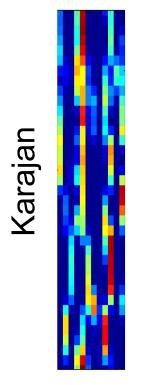


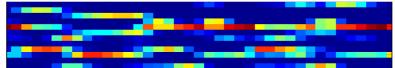
Scherbakov





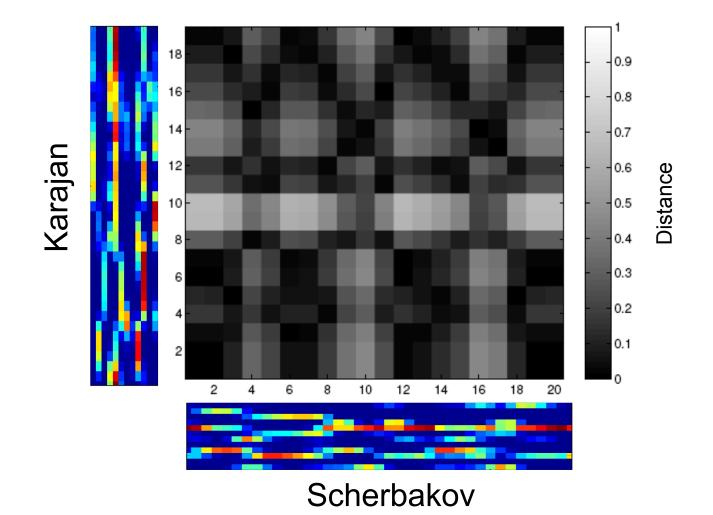




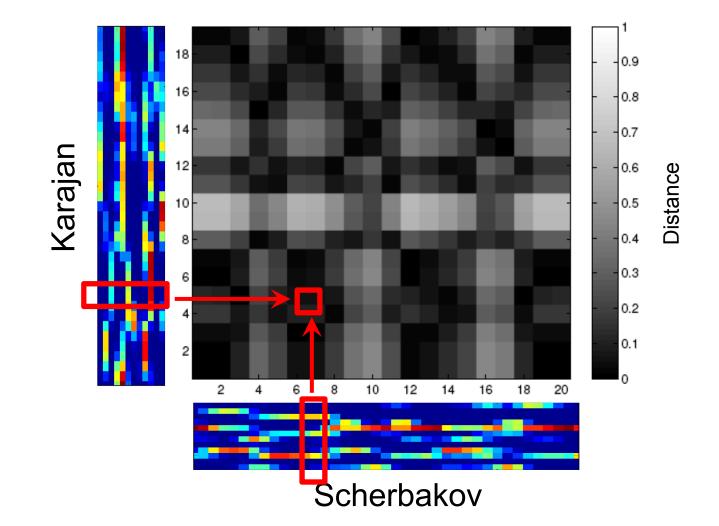


Scherbakov

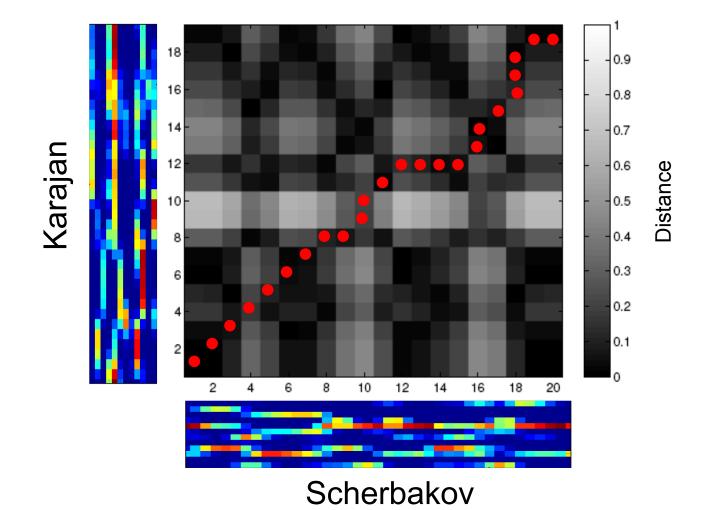
Music Synchronization: Audio-Audio Cost matrix

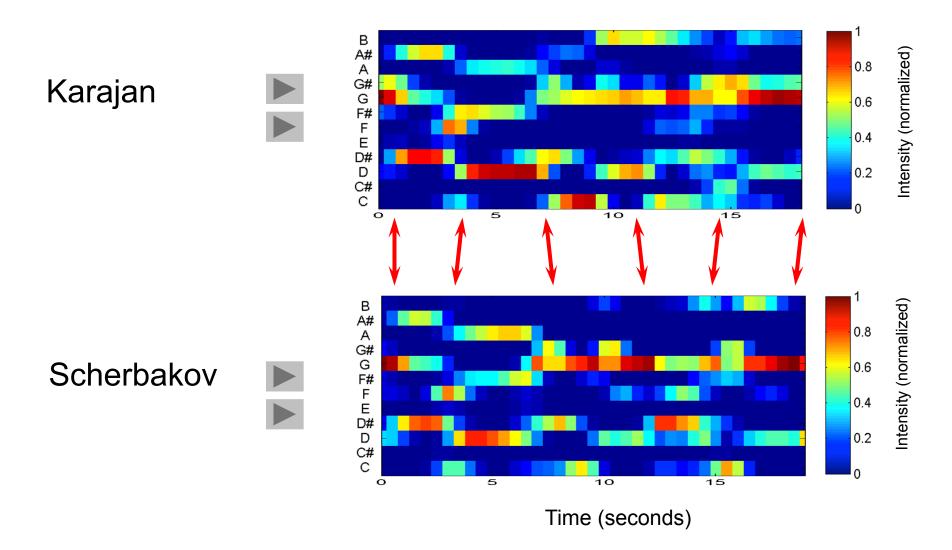


Music Synchronization: Audio-Audio Cost matrix



Music Synchronization: Audio-Audio Cost-minimizing alignment path





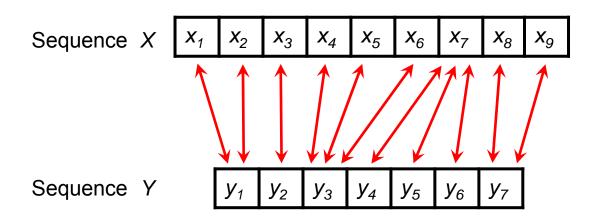
How to compute the alignment?

- \Rightarrow Cost matrices
- \Rightarrow Dynamic programming
- \Rightarrow Dynamic Time Warping (DTW)

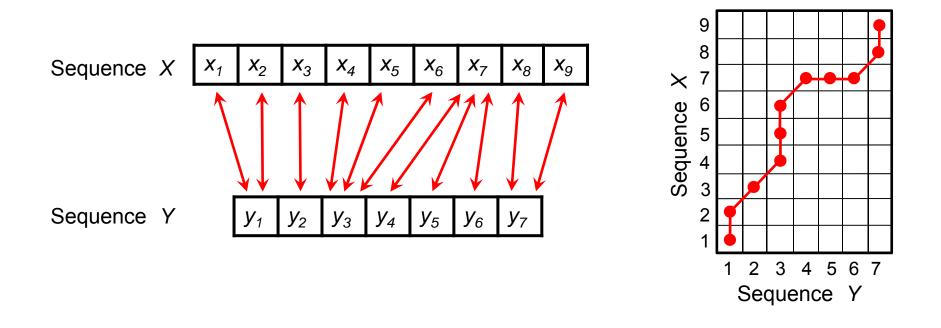
- Well-known technique to find an optimal alignment between two given (time-dependent) sequences under certain restrictions.
- Intuitively, sequences are warped in a non-linear fashion to match each other.
- Originally used to compare different speech patterns in automatic speech recognition

Sequence
$$X$$
 X_1 X_2 X_3 X_4 X_5 X_6 X_7 X_8 X_9

Sequence Y
$$y_1$$
 y_2 y_3 y_4 y_5 y_6 y_7



Time alignment of two time-dependent sequences, where the aligned points are indicated by the arrows.



Time alignment of two time-dependent sequences, where the aligned points are indicated by the arrows.

The objective of DTW is to compare two (time-dependent) sequences

$$X := (x_1, x_2, \dots, x_N)$$

of length $N \in \mathbb{N}$ and

$$Y := (y_1, y_2, \ldots, y_M)$$

of length $M \in \mathbb{N}$. Here,

$$x_n, y_m \in \mathcal{F}$$
, $n \in [1:N]$, $m \in [1:M]$,

are suitable features that are elements from a given feature space denoted by ${\mathcal F}$.

To compare two different features $x, y \in \mathcal{F}$ one needs a local cost measure which is defined to be a function

$$c: \mathcal{F} \times \mathcal{F} \to \mathbb{R}_{\geq 0}$$

Typically, c(x, y) is small (low cost) if x and y are similar to each other, and otherwise c(x, y) is large (high cost).

Evaluating the local cost measure for each pair of elements of the sequences X and Y, one obtains the cost matrix

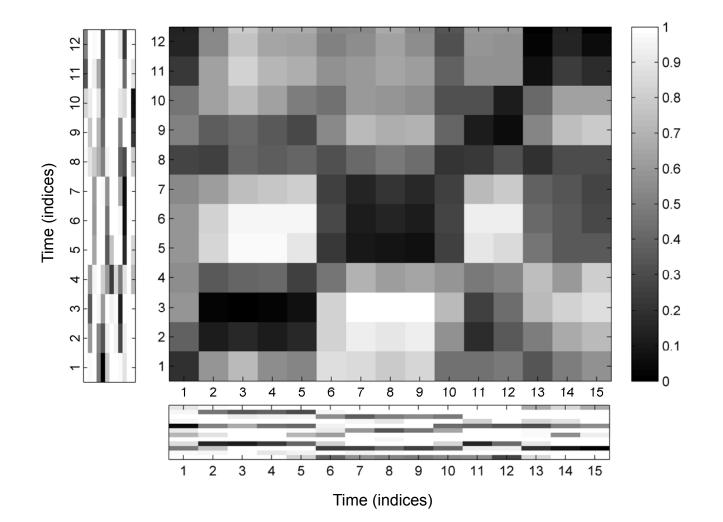
$$C \in \mathbb{R}^{N \times M}$$

denfined by

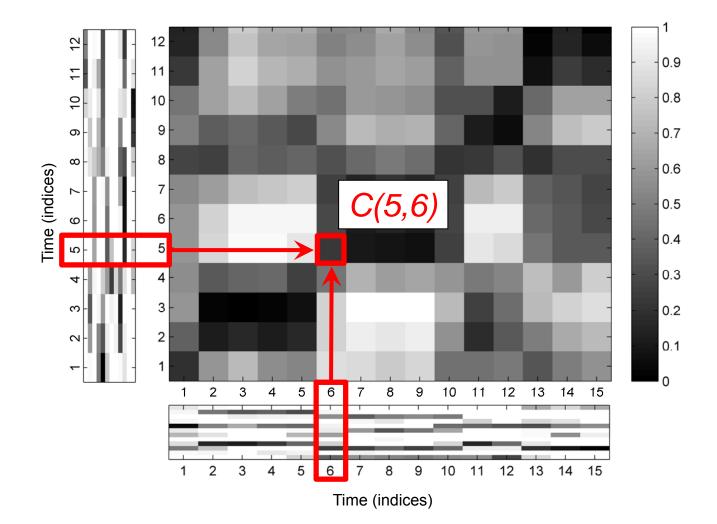
$$C(n,m) := c(x_n, y_m).$$

Then the goal is to find an alignment between X and Y having minimal overall cost. Intuitively, such an optimal alignment runs along a "valley" of low cost within the cost matrix C.

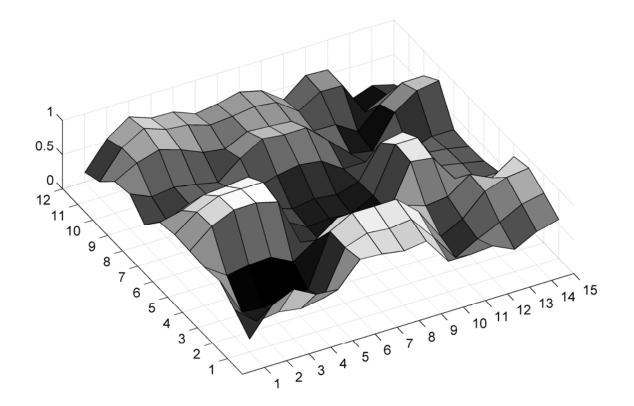
Cost matrix C



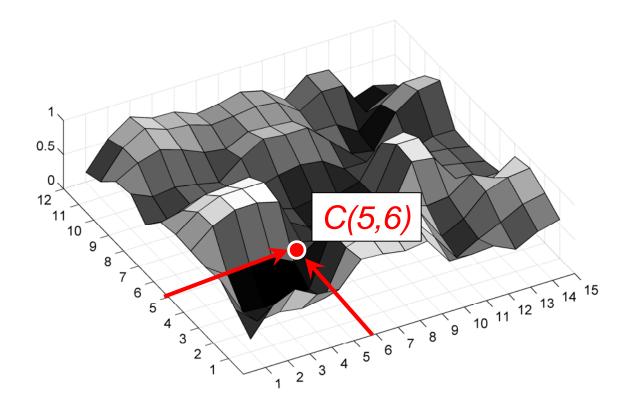
Cost matrix C



Dynamic Time Warping Cost matrix *C*



Dynamic Time Warping Cost matrix *C*



The next definition formalizes the notion of an alignment.

A warping path is a sequence $p = (p_1, \ldots, p_L)$ with $p_{\ell} = (n_{\ell}, m_{\ell}) \in [1:N] \times [1:M]$

for $\ell \in [1:L]$ satisfying the following three conditions:

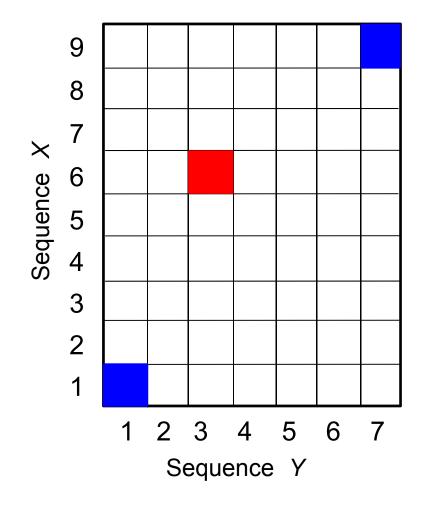
- Boundary condition: $p_1 = (1, 1)$ and $p_L = (N, M)$

Monotonicity condition: $n_1 \leq n_2 \leq \ldots \leq n_L$ and $m_1 < m_2 < \ldots < m_L$

Step size condition:

 $p_{\ell+1} - p_{\ell} \in \{(1,0), (0,1), (1,1)\}$ for $\ell \in [1:L-1]$

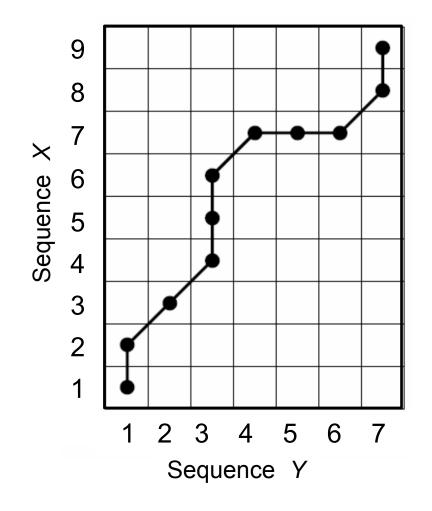
Dynamic Time Warping Warping path



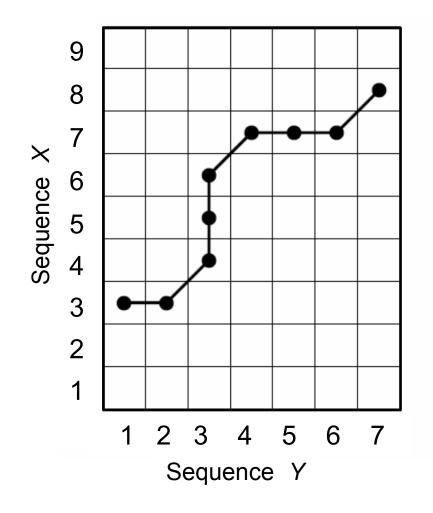
Each matrix entry (cell) corresponds to a pair of indices.

Cell = (6,3)

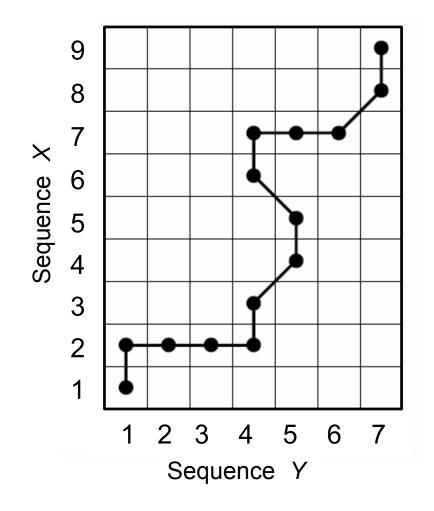
Boundary cells: $p_1 = (1,1)$ $p_L = (N,M) = (9,7)$

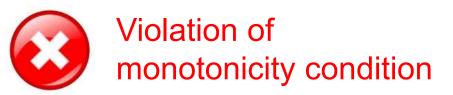


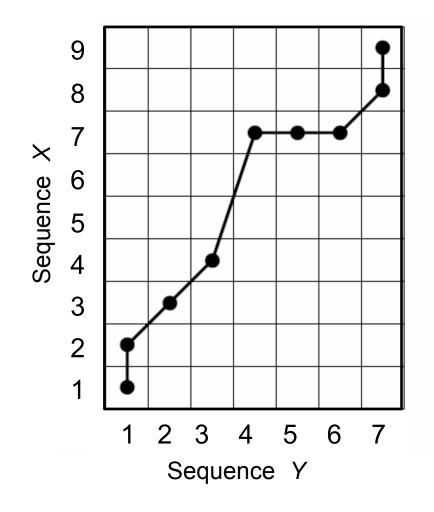














The total cost $c_p(X, Y)$ of a warping path p between Xand Y with respect to the local cost measure c is defined as L

$$c_p(X,Y) := \sum_{\ell=1}^{2} c(x_{n_\ell}, y_{m_\ell})$$

Furthermore, an optimal warping path between X and Y is a warping path p^* having minimal total cost among all possible warping paths. The DTW distance DTW(X, Y) between X and Y is then defined as the total cost o p^*

$$DTW(X,Y) := c_{p^*}(X,Y)$$

= min{c_p(X,Y) | p is a warping path}

- The warping path p^* is not unique (in general).
- DTW does (in general) not definne a metric since it may not satisfy the triangle inequality.
- There exist exponentially many warping paths.
- How can p^* be computed efficiently?

Notation:
$$X(1:n) := (x_1, ..., x_n), \quad 1 \le n \le N$$

 $Y(1:m) := (y_1, ..., y_m), \quad 1 \le m \le M$
 $D(n,m) := DTW(X(1:n), Y(1:m))$

The matrix D is called the accumulated cost matrix.

The entry D(n,m) specifies the cost of an optimal warping path that aligns X(1:n) with Y(1:m).

Lemma:

(i)
$$D(N,M) = DTW(X,Y)$$

(ii) $D(1,1) = C(1,1)$
(iii) $D(n,1) = \sum_{k=1}^{n} C(k,1)$
 $D(1,m) = \sum_{k=1}^{m} C(1,k)$
(iv) $D(n,m) = \min \begin{pmatrix} D(n-1,m-1) \\ D(n-1,m) \\ D(n,m-1) \end{pmatrix} + C(n,m)$
for $n > 1, m > 1$

Proof: (i) - (iii) are clear by definition

Proof of *(iv)*: Induction via n, m:

Let n > 1, m > 1 and $q = (q_1, \ldots, p_{L-1}, p_L)$ be an optimal warping path for X(1:n) and Y(1:m). Then $q_L = (n, m)$ (boundary condition).

Let $q_{L-1} = (a, b)$. The step size condition implies

$$(a,b) \in \{(n-1,m-1), (n-1,m), (n,m-1)\}$$

The warping path (q_1, \ldots, q_{L-1}) must be optimal for X(1:a), Y(1:b). Thus,

$$D(n,m) = c_{(q_1,\dots,q_{L-1})}(X(1:a),Y(1:b)) + C(n,m)$$

Accumulated cost matrix

Given the two feature sequences X and Y, the matrix D is computed recursively.

- Initialize D using (ii) and (iii) of the lemma.
- Compute D(n, m) for n > 1, m > 1 using *(iv)*.
- DTW(X, Y) = D(N, M) using (i).

Note:

- Complexity *O(NM)*.
- Dynamic programming: "overlapping-subproblem property"

Optimal warping path

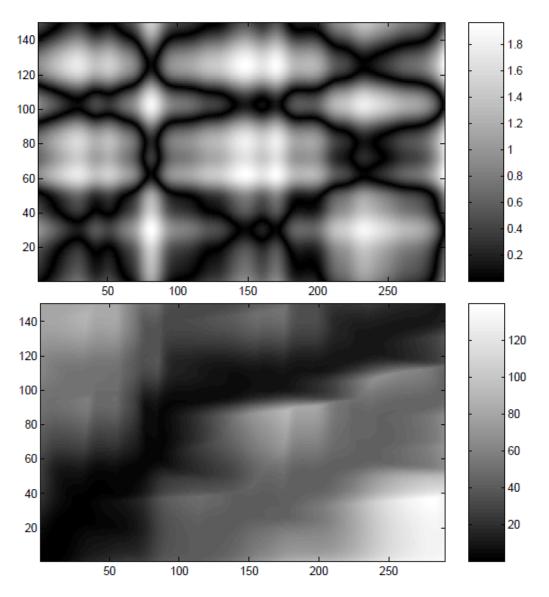
Given to the algorithm is the accumulated cost matrix D. The optimal path $p^* = (p_1, \ldots, p_L)$ is computed in reverse order of the indices starting with $p_L = (N, M)$. Suppose $p_\ell = (n, m)$ has been computed. In case (n, m) = (1, 1), one must have $\ell = 1$ and we are done. Otherwise,

$$p_{\ell-1} := \begin{cases} (1, m-1), & \text{if } n = 1\\ (n-1, 1), & \text{if } m = 1\\ \arg\min\{D(n-1, m-1), \\ D(n-1, m), D(n, m-1)\}, & \text{otherwise}, \end{cases}$$

where we take the lexicographically smallest pair in case "argmin" is not unique.

Cost matrix C

Accumulated cost martrix D

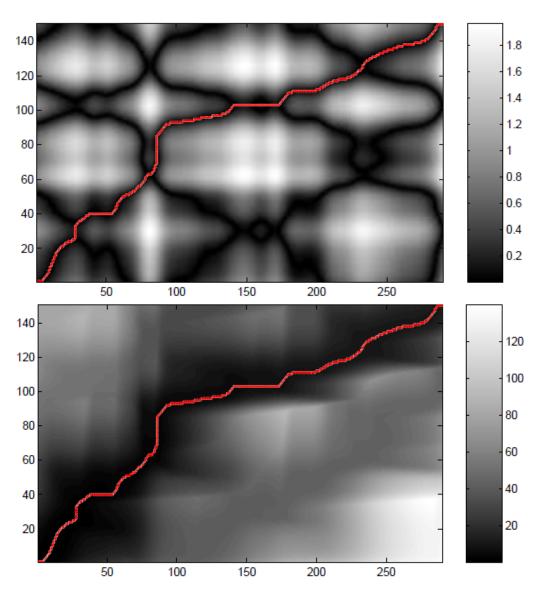


Cost matrix C

Optimal warping path

Accumulated cost martrix D

Optimal warping path



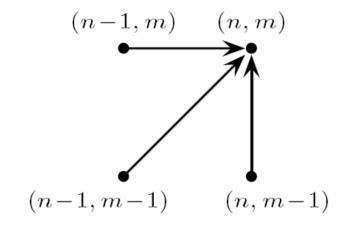
1	1	1	1	7	6	1
8	6	8	8	0	1	6
3	1	3	3	5	4	1
3	1	3	3	5	4	1
٦	1	1	1	7	6	1
	2	0	0	8	7	2

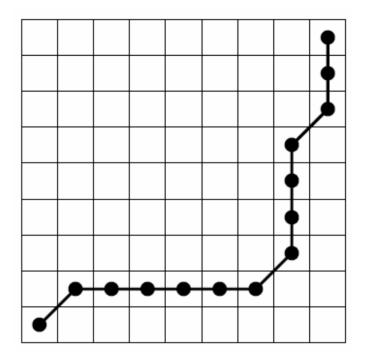
-	10	10	11	14	13	9
∞	9	11	13	7	8	14
S	3	5	7	10	12	13
С	2	4	5	8	12	13
~	1	2	3	10	16	17

8 7

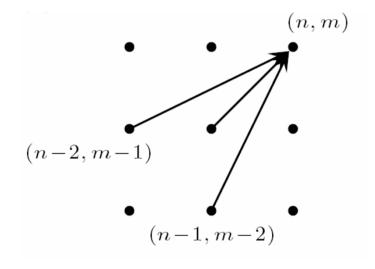
1	3	3 3	3 8	3	1
	1	1	1	\uparrow	\uparrow
V	V	V	V	V	V
2	0	0	8	7	2

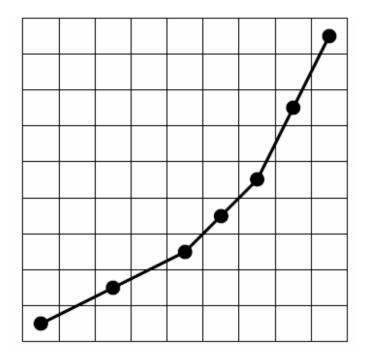
Dynamic Time Warping Variation of step size condition



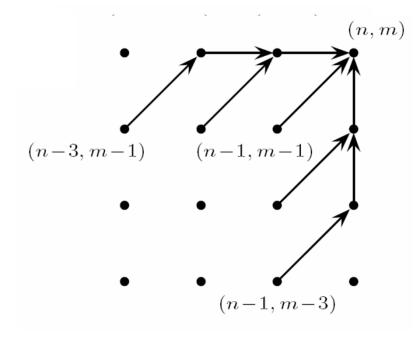


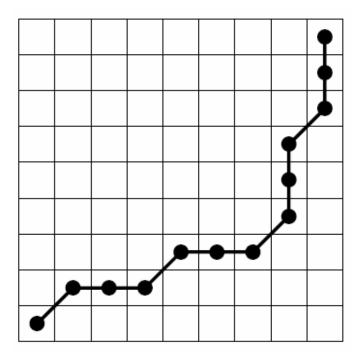
Dynamic Time Warping Variation of step size condition





Dynamic Time Warping Variation of step size condition

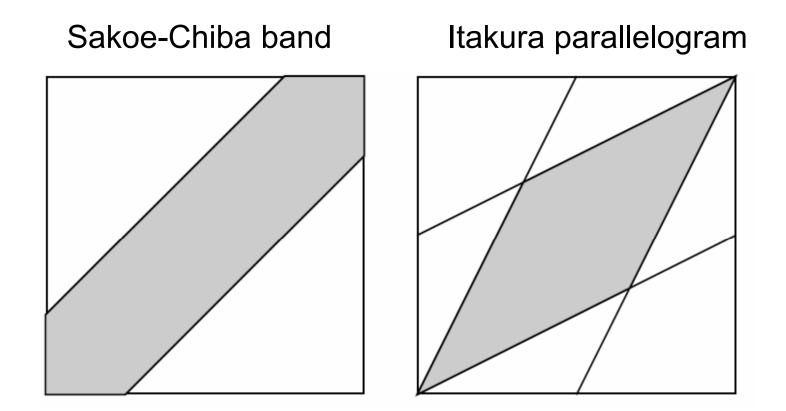




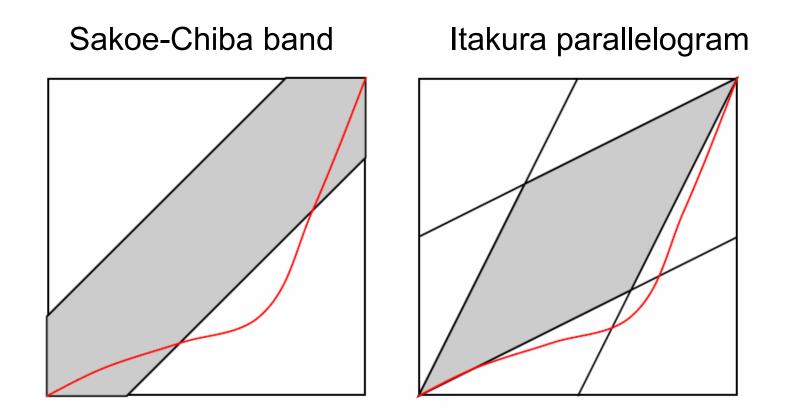
- Computation via dynamic programming
- Memory requirements and running time: O(NM)
- Problem: Infeasible for large *N* and *M*
- Example: Feature resolution 10 Hz, pieces 15 min

 $\Rightarrow N, M \sim 10,000$ $\Rightarrow N \cdot M \sim 100,000,000$

Dynamic Time Warping Strategy: Global constraints

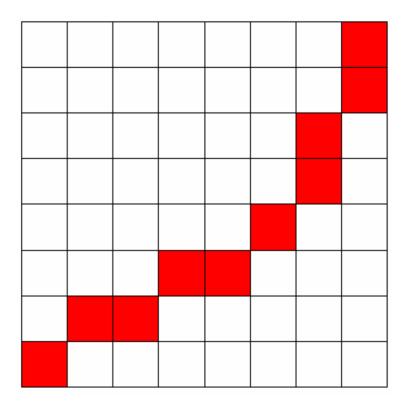


Dynamic Time Warping Strategy: Global constraints



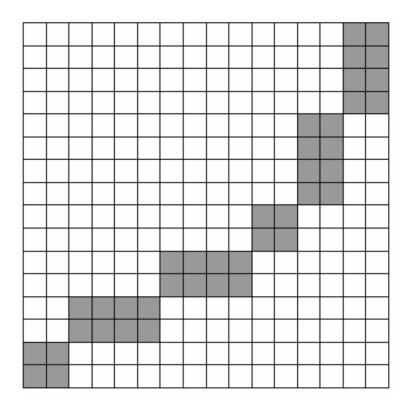
Problem: Optimal warping path not in constraint region

Strategy: Multiscale approach



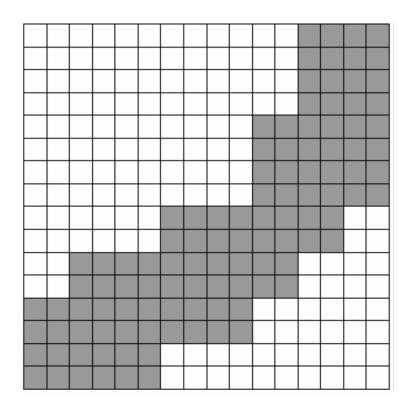
Compute optimal warping path on coarse level

Strategy: Multiscale approach



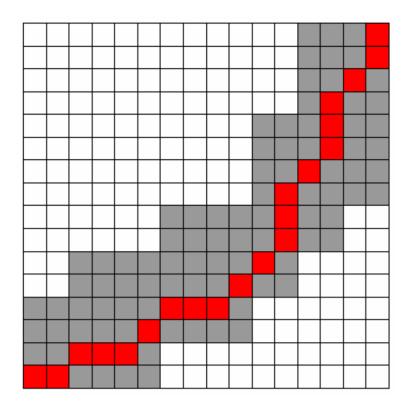
Project on fine level

Strategy: Multiscale approach



Specify constraint region

Strategy: Multiscale approach



Compute *constrained* optimal warping path

Dynamic Time Warping Strategy: Multiscale approach

- Suitable features?
- Suitable resolution levels?
- Size of constraint regions?

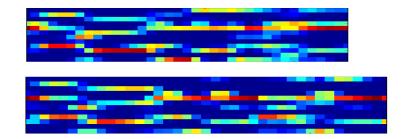
Good trade-off between efficiency and robustness? Suitable parameters depend very much on application!

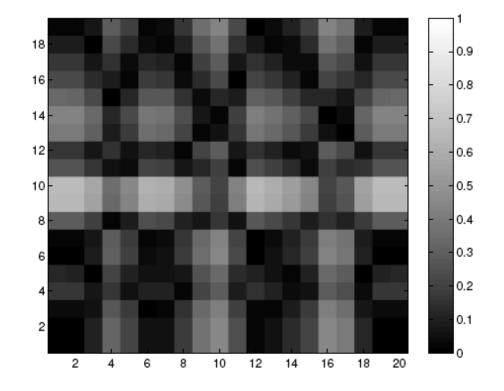
Music Synchronization: Audio-Audio

 Transform audio recordings into chroma vector sequences

 $\stackrel{\longrightarrow}{\longrightarrow} X := (x_1, x_2, \dots, x_N)$ $\stackrel{\longrightarrow}{\longrightarrow} Y := (y_1, y_2, \dots, y_M)$

• Compute cost matrix $C(n,m) := c(x_n, y_m)$ with respect to local cost measure c



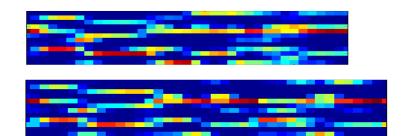


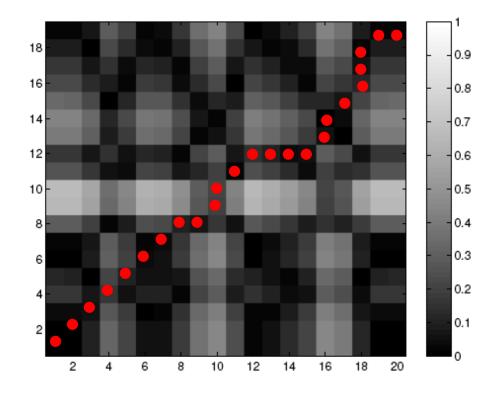
Music Synchronization: Audio-Audio

 Transform audio recordings into chroma vector sequences

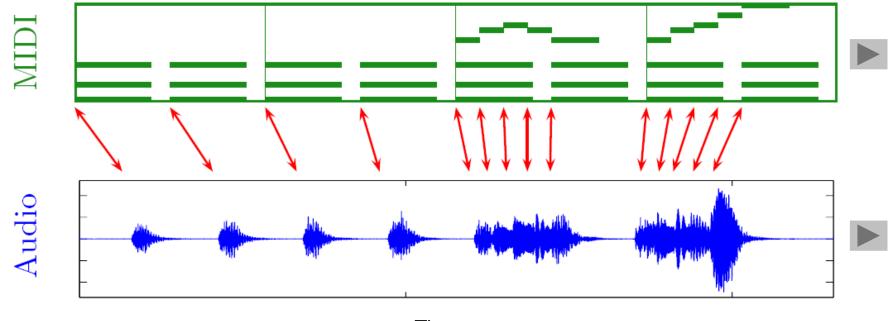
 $\stackrel{\longrightarrow}{\longrightarrow} X := (x_1, x_2, \dots, x_N) \\ \stackrel{\longrightarrow}{\longrightarrow} Y := (y_1, y_2, \dots, y_M)$

- Compute cost matrix $C(n,m) := c(x_n, y_m)$ with respect to local cost measure c
- Compute cost-minimizing warping path from C





Music Synchronization: MIDI-Audio



Time

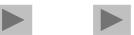
Music Synchronization: MIDI-Audio

MIDI = meta data

Automated annotation

Audio recording

Sonification of annotations

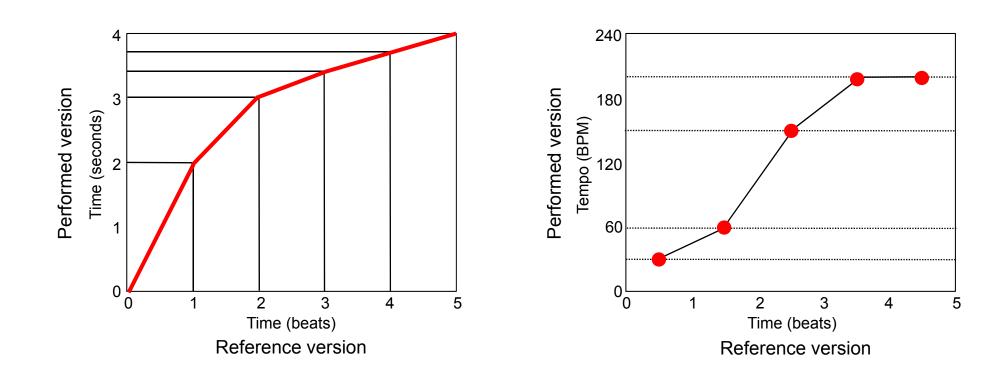


Music Synchronization: MIDI-Audio

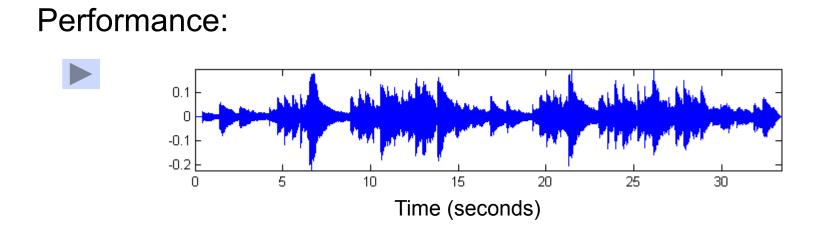
MIDI = reference (score)

Tempo information

Audio recording



Schumann: Träumerei

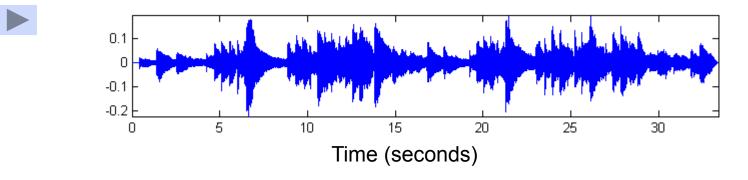


Schumann: Träumerei

Score (reference):



Performance:



Schumann: Träumerei

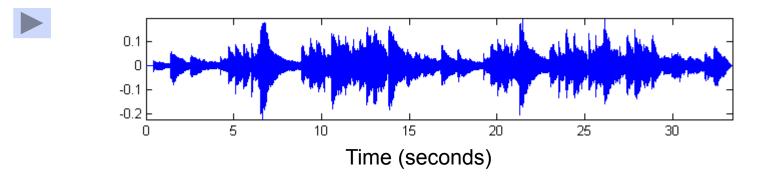
Score (reference):





Strategy: Compute score-audio synchronization and derive tempo curve

Performance:

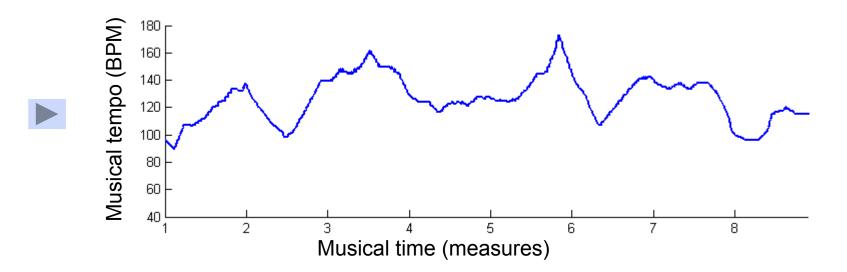


Schumann: Träumerei

Score (reference):



Tempo curve:



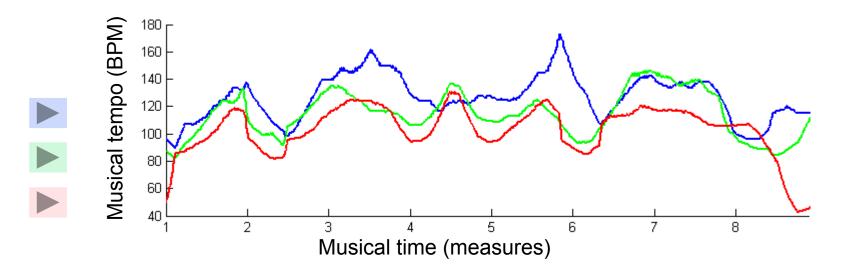
Schumann: Träumerei

Score (reference):





Tempo curves:



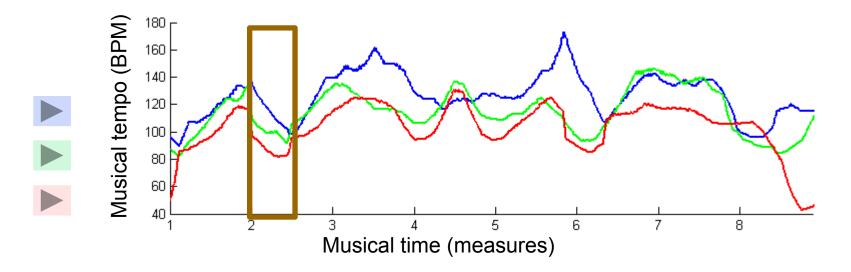
Performance Analysis: Tempo Curves

Schumann: Träumerei

Score (reference):

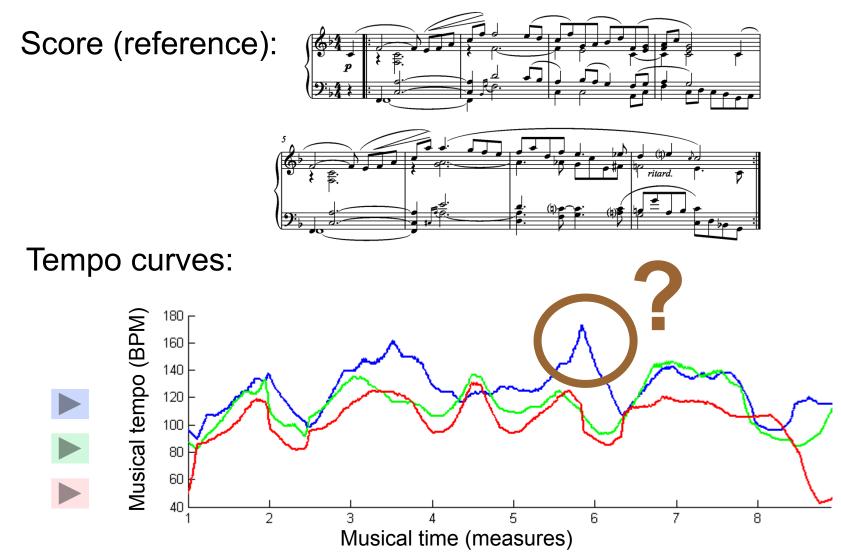


Tempo curves:



Performance Analysis: Tempo Curves

Schumann: Träumerei

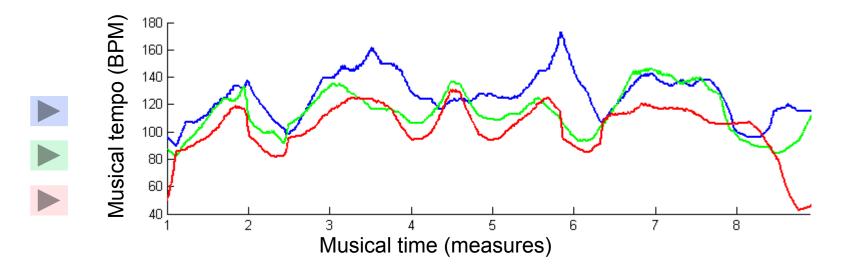


Performance Analysis: Tempo Curves

Schumann: Träumerei

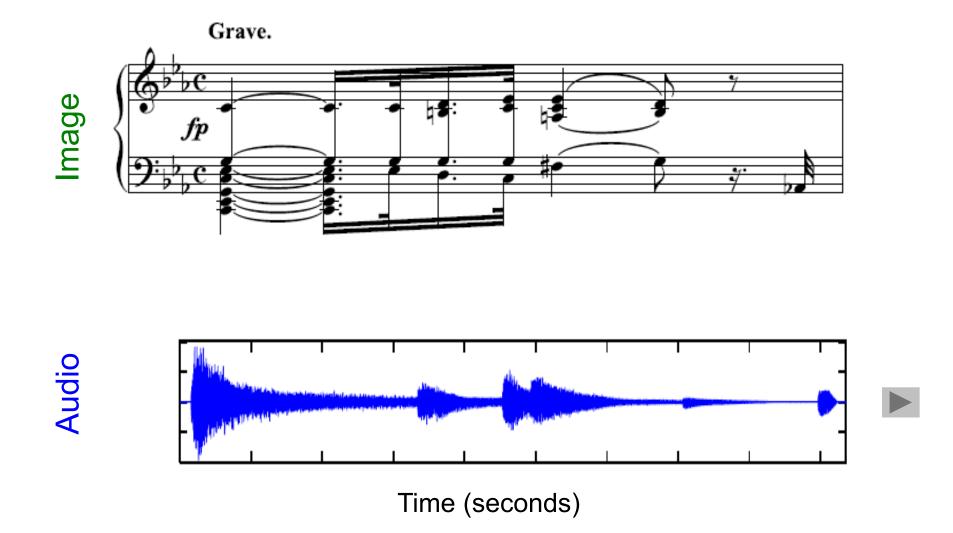
What can be done if no reference is available?

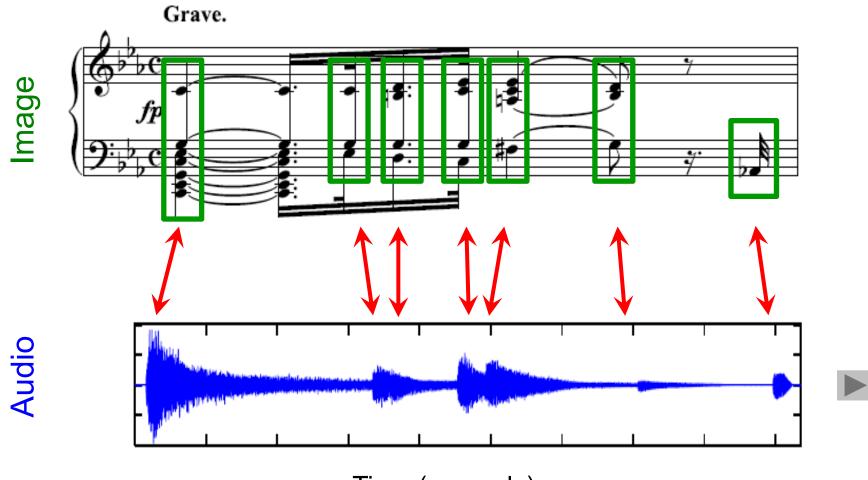
Tempo curves:



Music Synchronization: MIDI-Audio Applications

- Automated audio annotation
- Accurate audio access after MIDI-based retrieval
- Automated tracking of MIDI note parameters during audio playback
- Performance Analysis



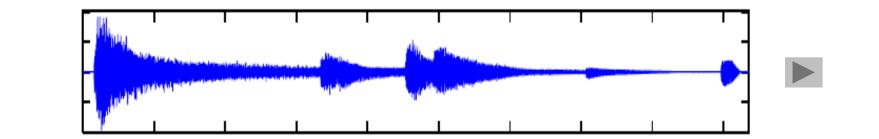


Time (seconds)

Audio

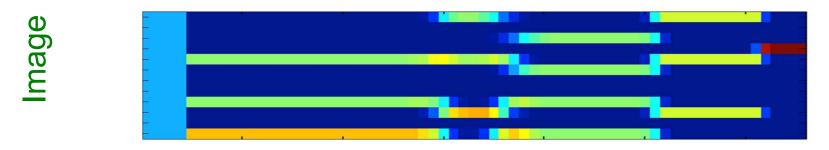
Convert data into common mid-level feature representation





Audio

Image Processing: Optical Music Recognition



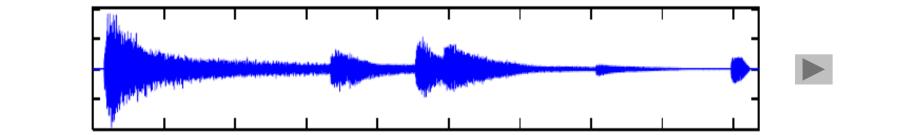
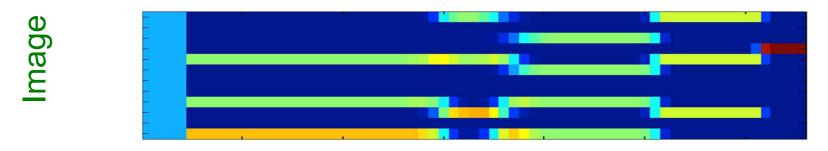
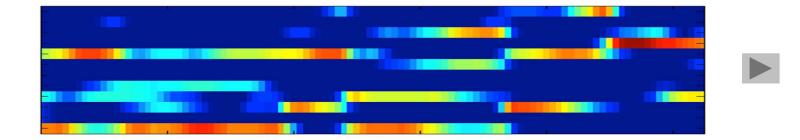


Image Processing: Optical Music Recognition

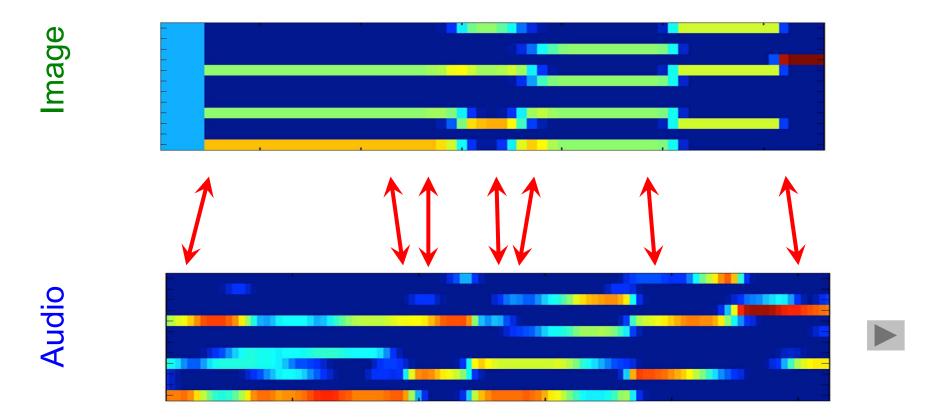






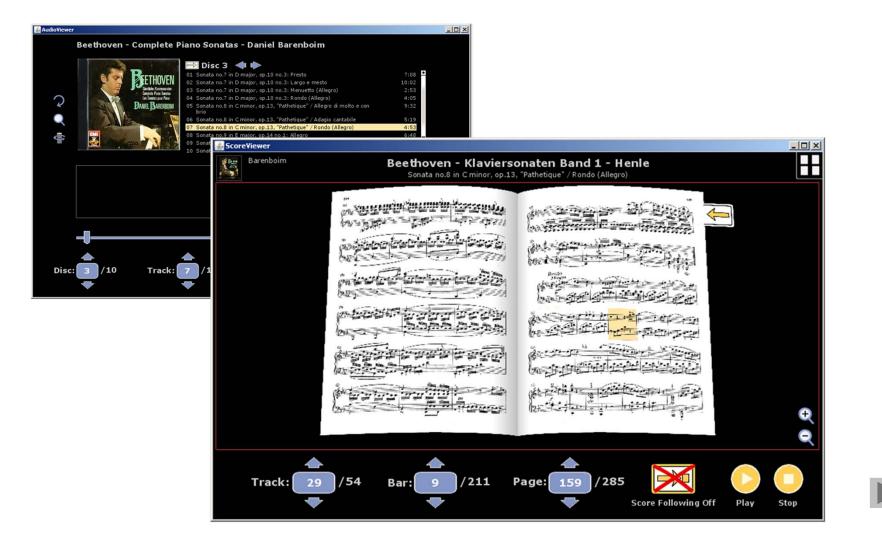
Audio Processing: Fourier Analyse

Image Processing: Optical Music Recognition

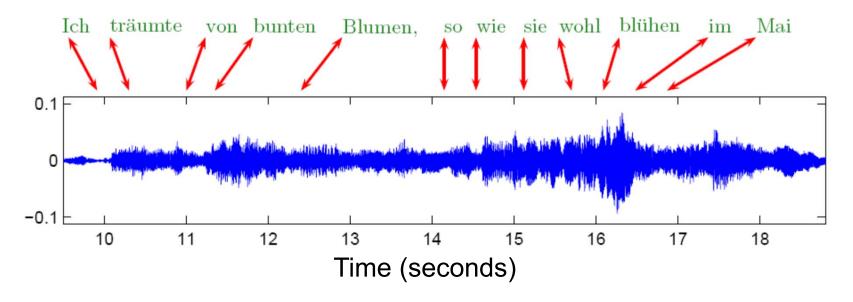


Audio Processing: Fourier Analyse

Application: Score Viewer



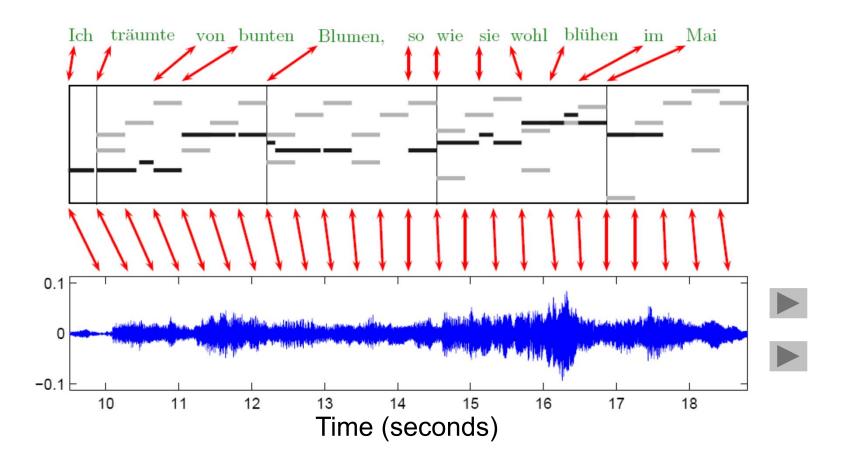
Music Synchronization: Lyrics-Audio



Difficult task!

Music Synchronization: Lyrics-Audio

Lyrics-Audio \rightarrow Lyrics-MIDI + MIDI-Audio



Music Synchronization: Lyrics-Audio

Application: SyncPlayer/LyricsSeeker



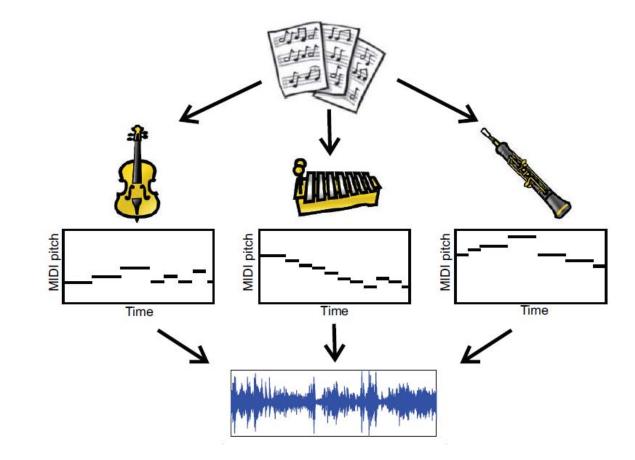
Source Separation

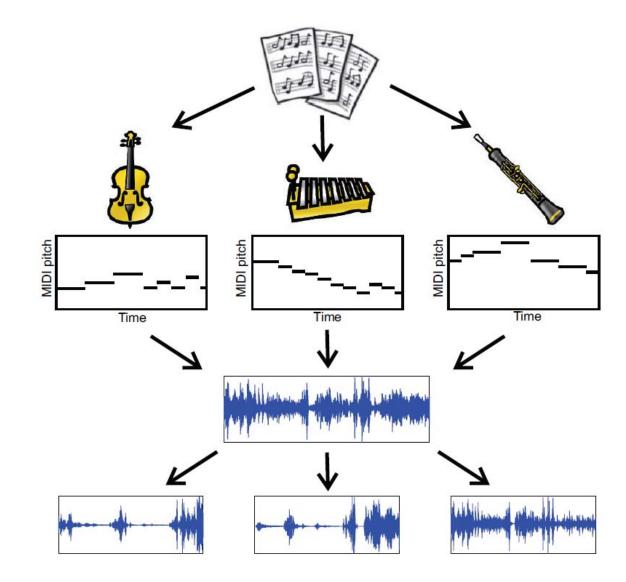
- Decomposition of audio stream into different sound sources
- Central task in digital signal processing
- "Cocktail party effect"
- Sources are often assumed to be statistically independent
- This is often not the case in music

Strategy: Exploit additional information (e.g. musical score) to support the seperation process

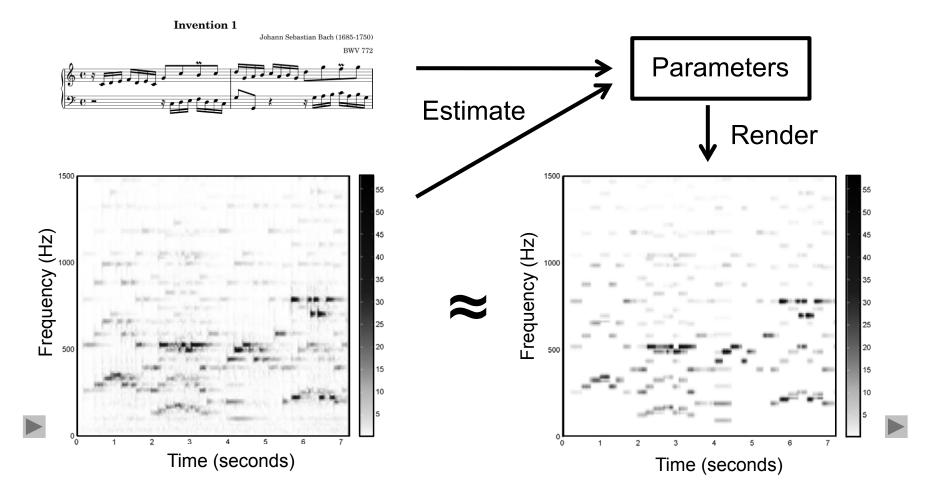


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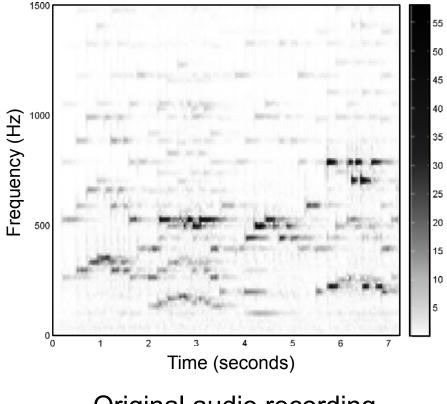




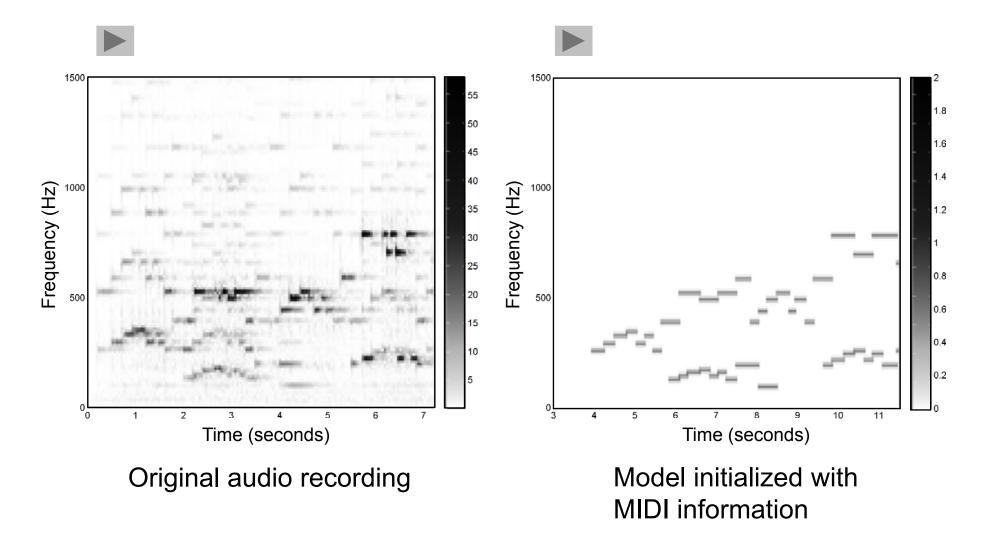
Goal: Approximate spectrogram using a parametric model exploiting availablity of score information



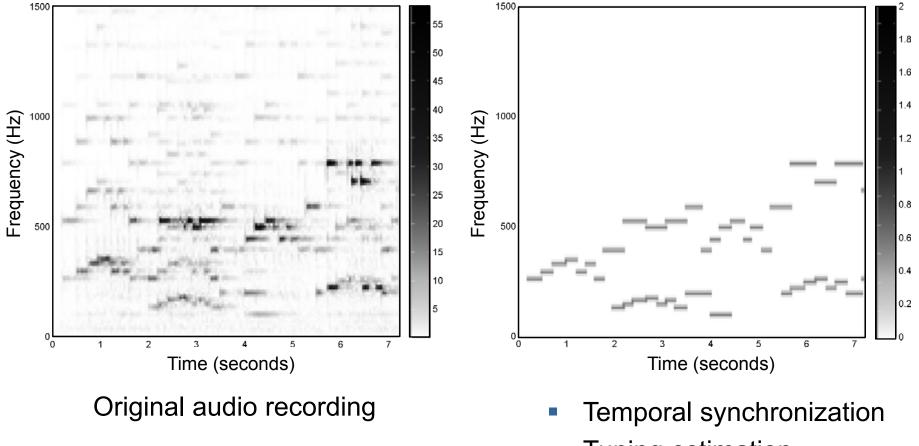




Original audio recording

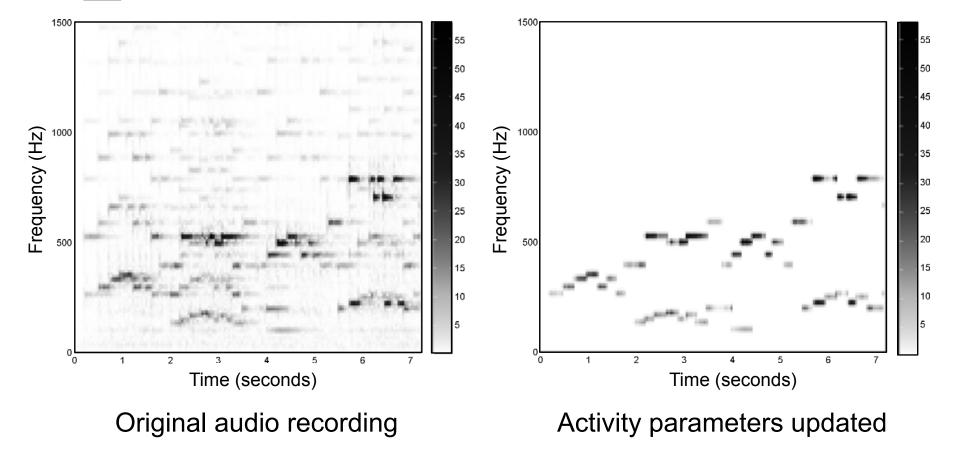




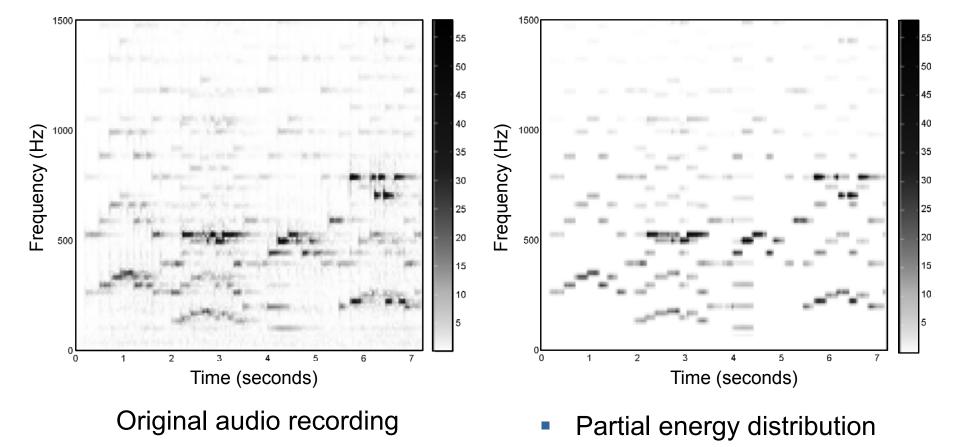


Tuning estimation

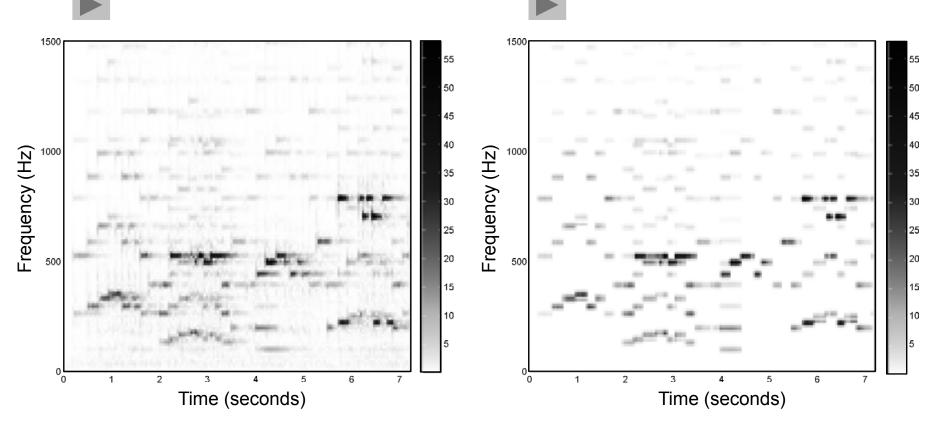








Resonance body properties

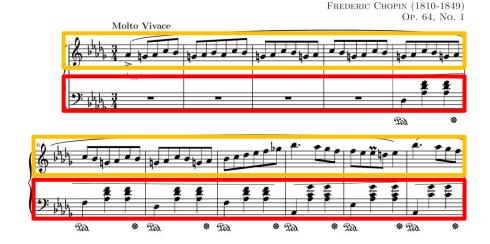


Original audio recording

Model after three iterations

Note: Each note specified by the score parameterizes a portion of the spectrogram

Experimental results for separating left and right hands for piano recordings:



Composer	Piece	Database	Results	
			L R Eq Org	
Bach	BWV 875, Prelude	SMD		
Chopin	Op. 28, No. 15	SMD		
Chopin	Op. 64, No. 1	European Archive		

Audio editing

