INTERNATIONAL AUDIO LABORATORIES ERLANGEN



Lecture Music Processing

## **Music Synchronization**

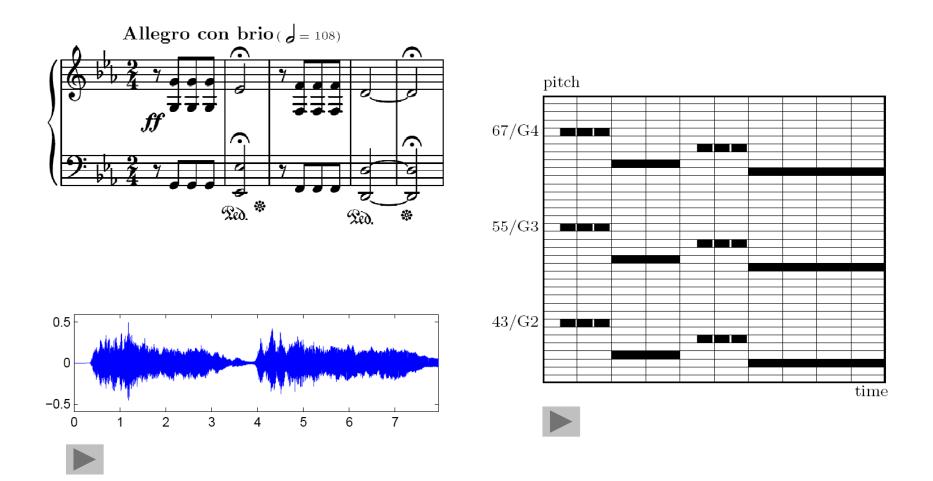
#### **Meinard Müller**

International Audio Laboratories Erlangen meinard.mueller@audiolabs-erlangen.de





## **Music Data**

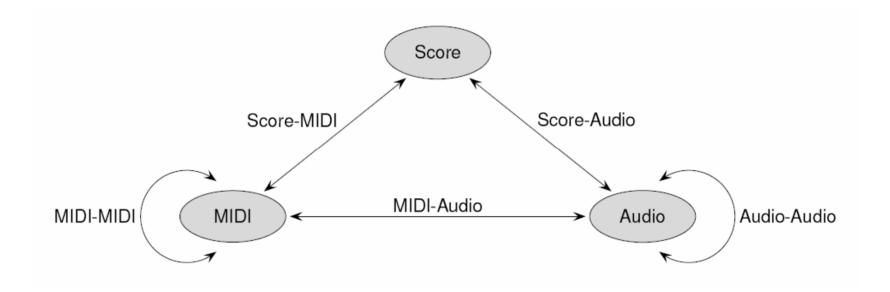


## **Music Data**

### Various interpretations – Beethoven's Fifth

Bernstein	
Karajan	
Scherbakov (piano)	
MIDI (piano)	

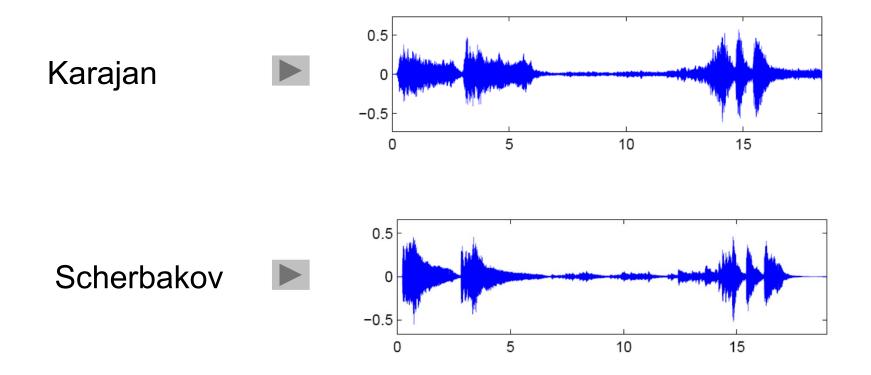
## **Music Synchronization**



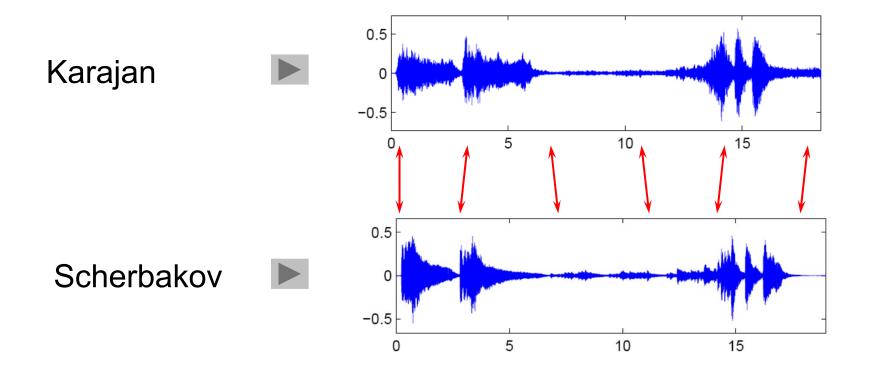
#### Schematic view of various synchronization tasks

- **Given:** Two different audio recordings of the same underlying piece of music.
- **Goal:** Find for each position in one audio recording the musically corresponding position in the other audio recording.

## Music Synchronization: Audio-Audio Beethoven's Fifth



## Music Synchronization: Audio-Audio Beethoven's Fifth



Synchronization: Karajan  $\rightarrow$  Scherbakov

#### Application: Interpretation Switcher

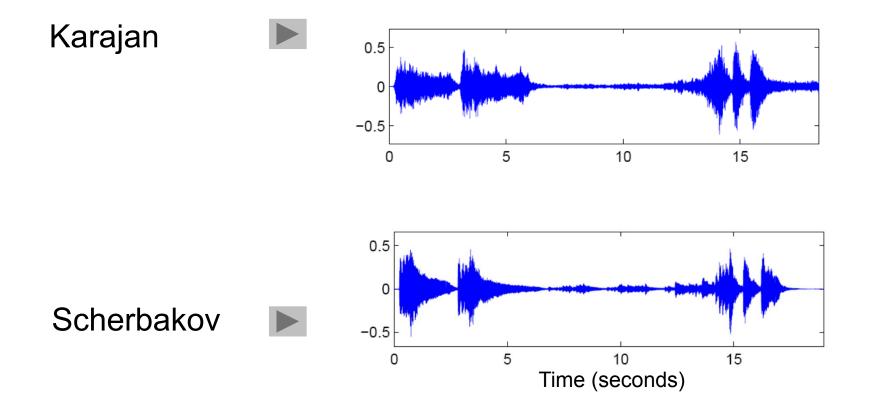


#### Two main steps:

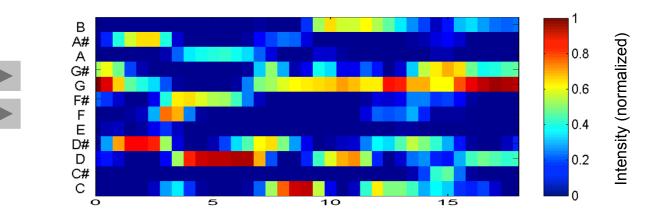
### 1.) Audio features

- Robust but discriminative
- Chroma features
- Robust to variations in instrumentation, timbre, dynamics
- Correlate to harmonic progression
- 2.) Alignment procedure
  - Deals with local and global tempo variations
  - Needs to be efficient

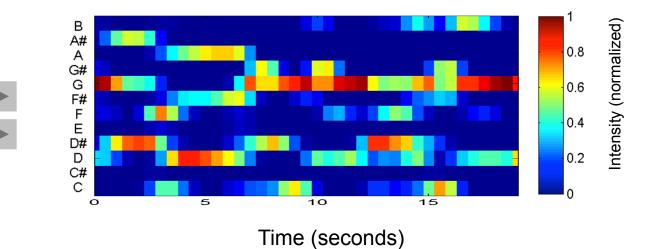
## Music Synchronization: Audio-Audio Beethoven's Fifth



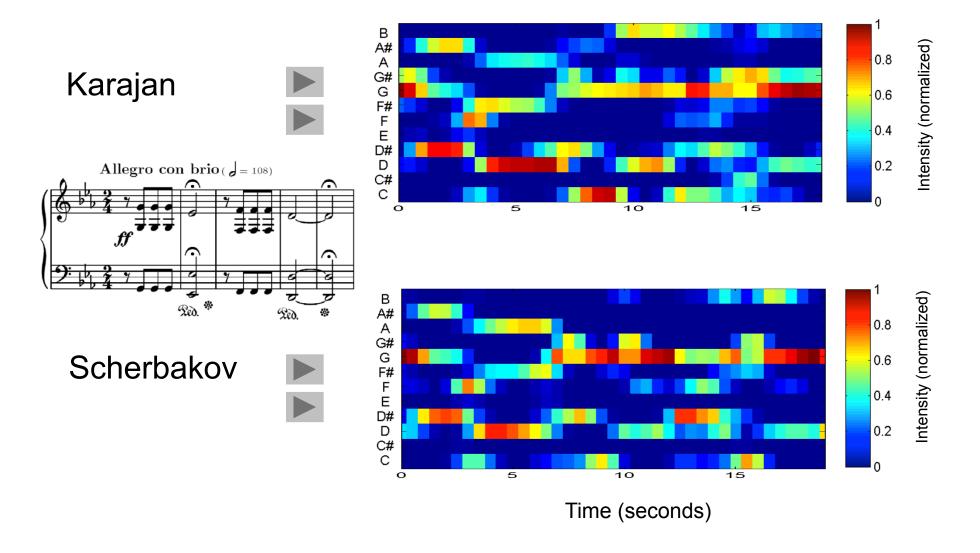
#### Beethoven's Fifth

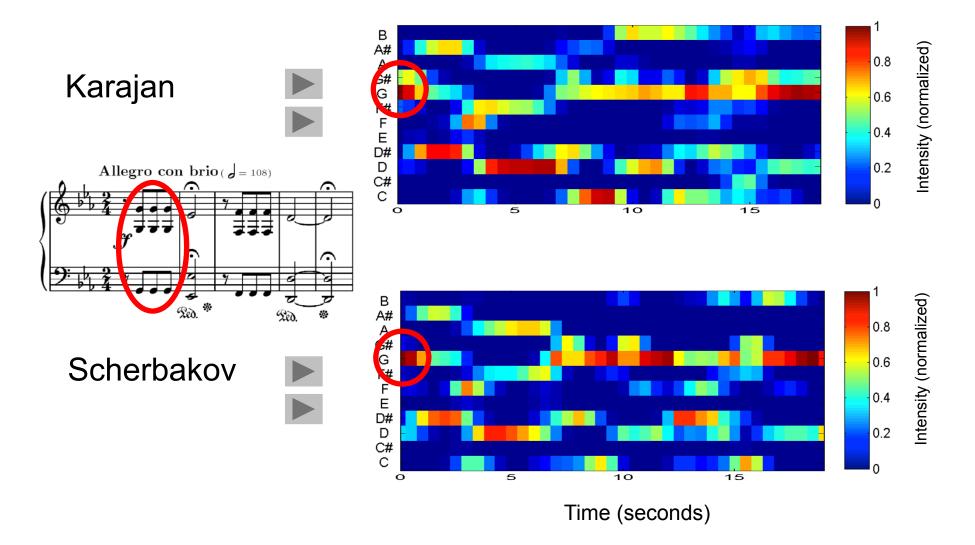


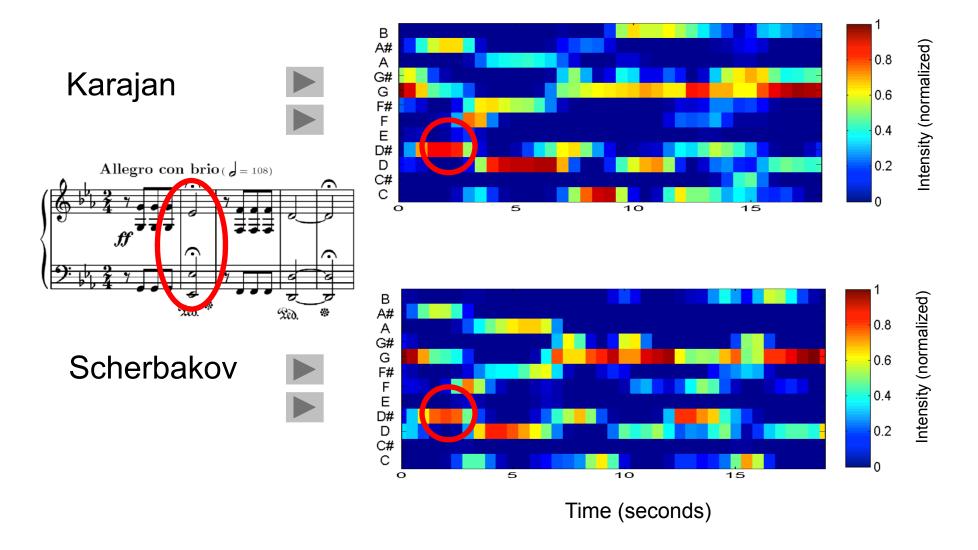
Karajan

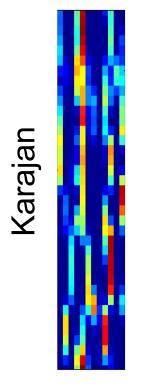


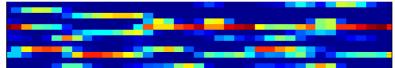
Scherbakov





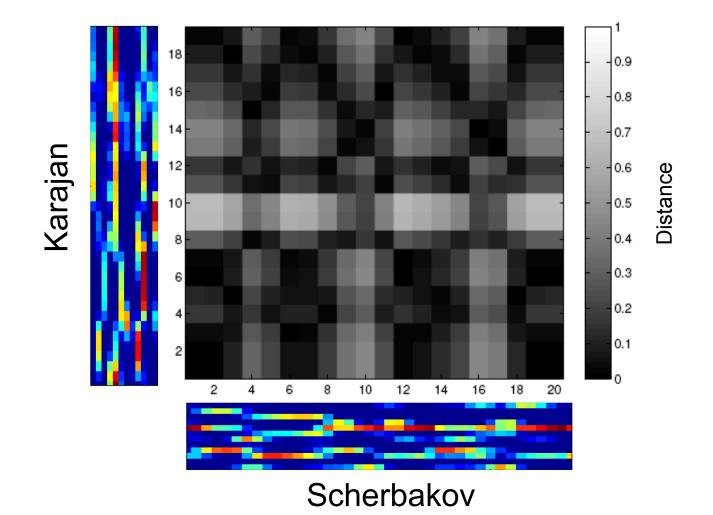




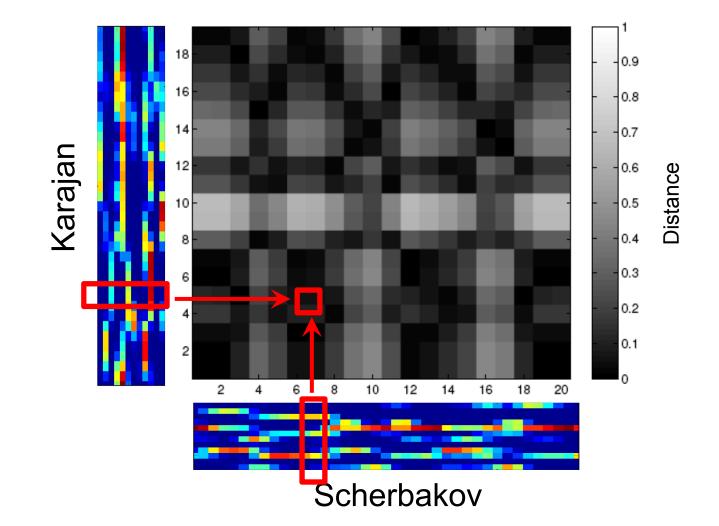


Scherbakov

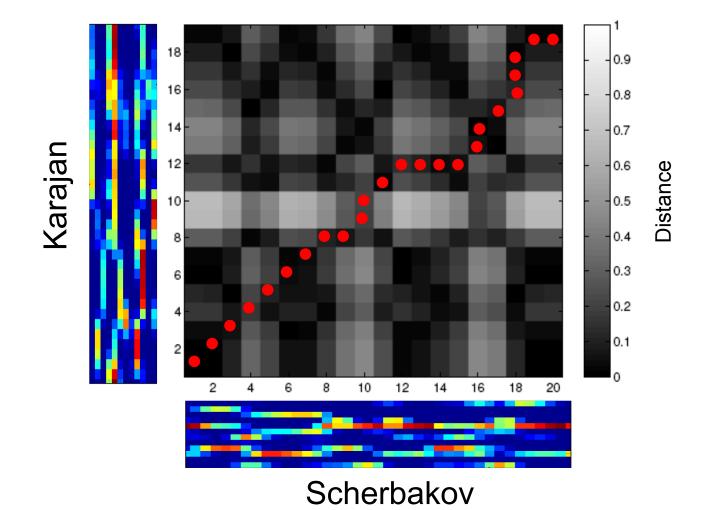
## Music Synchronization: Audio-Audio Cost matrix

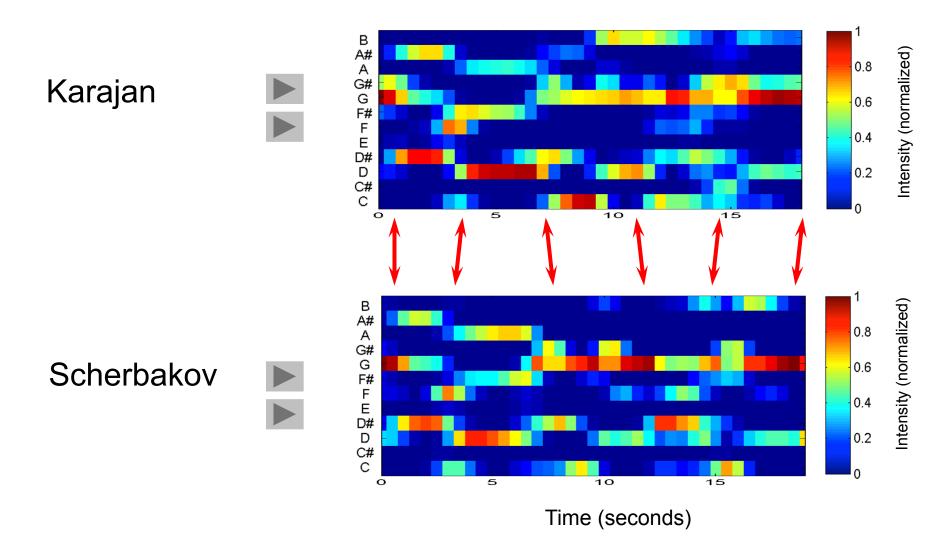


## Music Synchronization: Audio-Audio Cost matrix



## Music Synchronization: Audio-Audio Cost-minimizing alignment path

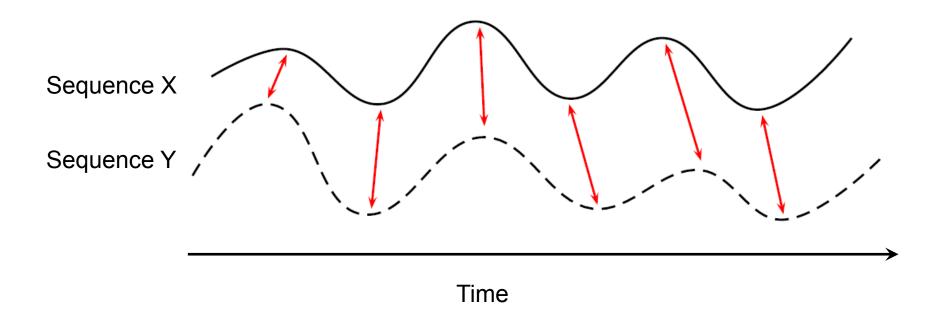




### How to compute the alignment?

- $\Rightarrow$  Cost matrices
- $\Rightarrow$  Dynamic programming
- $\Rightarrow$  Dynamic Time Warping (DTW)

- Well-known technique to find an optimal alignment between two given (time-dependent) sequences under certain restrictions.
- Intuitively, sequences are warped in a non-linear fashion to match each other.
- Originally used to compare different speech patterns in automatic speech recognition



Time alignment of two time-dependent sequences, where the aligned points are indicated by the arrows.

The objective of DTW is to compare two (time-dependent) sequences

$$X := (x_1, x_2, \dots, x_N)$$

of length  $N \in \mathbb{N}$  and

$$Y := (y_1, y_2, \ldots, y_M)$$

of length  $M \in \mathbb{N}$ . Here,

$$x_n, y_m \in \mathcal{F}$$
,  $n \in [1:N]$ ,  $m \in [1:M]$ ,

are suitable features that are elements from a given feature space denoted by  ${\mathcal F}$  .

To compare two different features  $x, y \in \mathcal{F}$ one needs a local cost measure which is defined to be a function

$$c: \mathcal{F} \times \mathcal{F} \to \mathbb{R}_{\geq 0}$$

Typically, c(x, y) is small (low cost) if x and y are similar to each other, and otherwise c(x, y) is large (high cost).

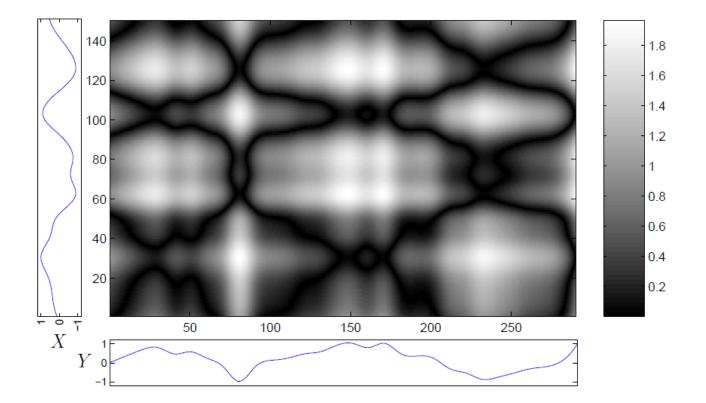
Evaluating the local cost measure for each pair of elements of the sequences X and Y, one obtains the cost matrix

$$C \in \mathbb{R}^{N \times M}$$

denfined by

$$C(n,m) := c(x_n, y_m).$$

Then the goal is to find an alignment between X and Y having minimal overall cost. Intuitively, such an optimal alignment runs along a "valley" of low cost within the cost matrix C.



Cost matrix of the two real-valued sequences X and Y using the Manhattan distance (absolute value of the difference) as local cost measure c.

The next definition formalizes the notion of an alignment.

A warping path is a sequence  $p = (p_1, \ldots, p_L)$  with  $p_{\ell} = (n_{\ell}, m_{\ell}) \in [1:N] \times [1:M]$ 

for  $\ell \in [1:L]$  satisfying the following three conditions:

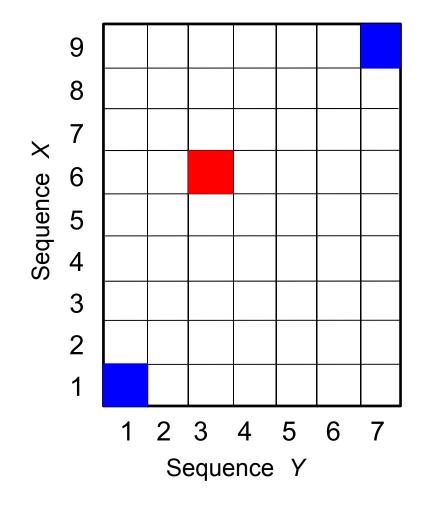
- Boundary condition:  $p_1 = (1, 1)$  and  $p_L = (N, M)$

Monotonicity condition:  $n_1 \leq n_2 \leq \ldots \leq n_L$  and  $m_1 < m_2 < \ldots < m_L$ 

Step size condition:

 $p_{\ell+1} - p_{\ell} \in \{(1,0), (0,1), (1,1)\}$ for  $\ell \in [1:L-1]$ 

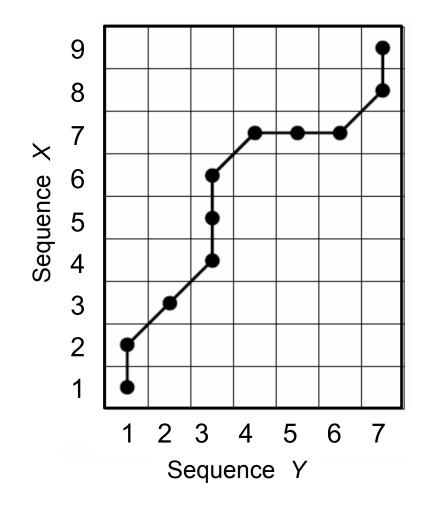
## Dynamic Time Warping Warping path



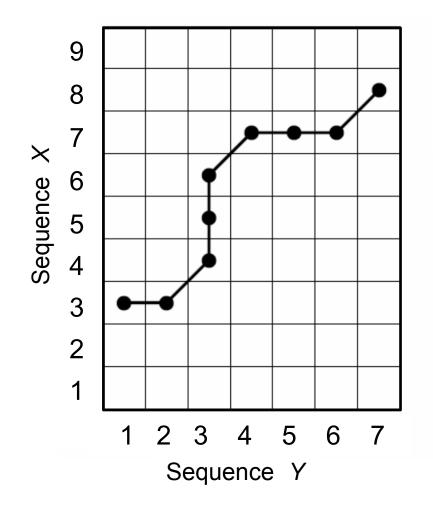
Each matrix entry (cell) corresponds to a pair of indices.

Cell = (6,3)

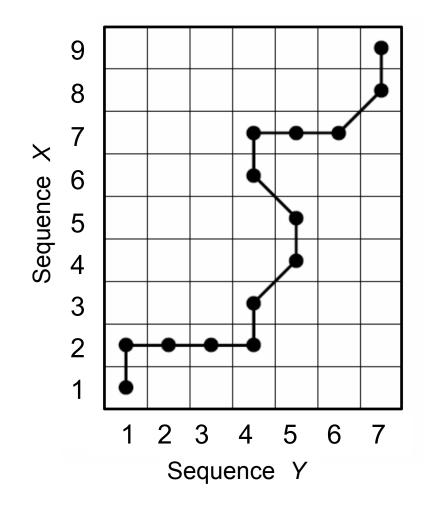
Boundary cells:  $p_1 = (1,1)$  $p_L = (N,M) = (9,7)$ 

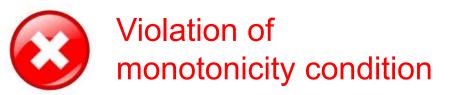


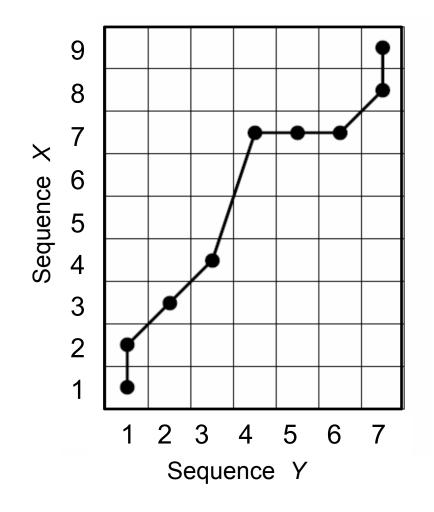














The total cost  $c_p(X, Y)$  of a warping path p between Xand Y with respect to the local cost measure c is defined as L

$$c_p(X,Y) := \sum_{\ell=1}^{2} c(x_{n_\ell}, y_{m_\ell})$$

Furthermore, an optimal warping path between X and Y is a warping path  $p^*$  having minimal total cost among all possible warping paths. The DTW distance DTW(X, Y) between X and Y is then defined as the total cost o  $p^*$ 

$$DTW(X,Y) := c_{p^*}(X,Y)$$
  
= min{c<sub>p</sub>(X,Y) | p is a warping path}

- The warping path  $p^*$  is not unique (in general).
- DTW does (in general) not definne a metric since it may not satisfy the triangle inequality.
- There exist exponentially many warping paths.
- How can  $p^*$  be computed efficiently?

Notation: 
$$X(1:n) := (x_1, ..., x_n), \quad 1 \le n \le N$$
  
 $Y(1:m) := (y_1, ..., y_m), \quad 1 \le m \le M$   
 $D(n,m) := DTW(X(1:n), Y(1:m))$ 

The matrix D is called the accumulated cost matrix.

The entry D(n,m) specifies the cost of an optimal warping path that aligns X(1:n) with Y(1:m).

#### Lemma:

(i) 
$$D(N,M) = DTW(X,Y)$$
  
(ii)  $D(1,1) = C(1,1)$   
(iii)  $D(n,1) = \sum_{k=1}^{n} C(k,1)$   
 $D(1,m) = \sum_{k=1}^{m} C(1,k)$   
(iv)  $D(n,m) = \min \begin{pmatrix} D(n-1,m-1) \\ D(n-1,m) \\ D(n,m-1) \end{pmatrix} + C(n,m)$   
for  $n > 1, m > 1$ 

**Proof**: (i) - (iii) are clear by definition

**Proof** of *(iv)*: Induction via n, m:

Let n > 1, m > 1 and  $q = (q_1, \ldots, p_{L-1}, p_L)$  be an optimal warping path for X(1:n) and Y(1:m). Then  $q_L = (n, m)$  (boundary condition).

Let  $q_{L-1} = (a, b)$ . The step size condition implies

$$(a,b) \in \{(n-1,m-1), (n-1,m), (n,m-1)\}$$

The warping path  $(q_1, \ldots, q_{L-1})$  must be optimal for X(1:a), Y(1:b). Thus,

$$D(n,m) = c_{(q_1,\dots,q_{L-1})}(X(1:a),Y(1:b)) + C(n,m)$$

Accumulated cost matrix

Given the two feature sequences X and Y, the matrix D is computed recursively.

- Initialize D using (ii) and (iii) of the lemma.
- Compute D(n, m) for n > 1, m > 1 using *(iv)*.
- DTW(X, Y) = D(N, M) using (i).

#### Note:

- Complexity *O(NM)*.
- Dynamic programming: "overlapping-subproblem property"

#### Optimal warping path

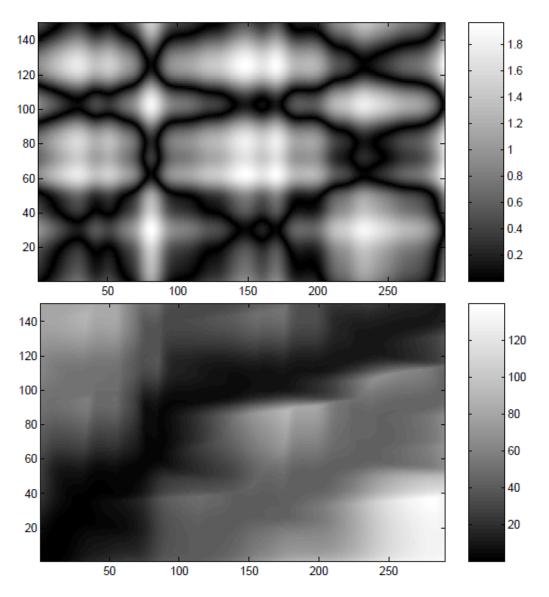
Given to the algorithm is the accumulated cost matrix D. The optimal path  $p^* = (p_1, \ldots, p_L)$  is computed in reverse order of the indices starting with  $p_L = (N, M)$ . Suppose  $p_\ell = (n, m)$  has been computed. In case (n, m) = (1, 1), one must have  $\ell = 1$  and we are done. Otherwise,

$$p_{\ell-1} := \begin{cases} (1, m-1), & \text{if } n = 1\\ (n-1, 1), & \text{if } m = 1\\ \arg\min\{D(n-1, m-1), \\ D(n-1, m), D(n, m-1)\}, & \text{otherwise}, \end{cases}$$

where we take the lexicographically smallest pair in case "argmin" is not unique.

Cost matrix C

Accumulated cost martrix D

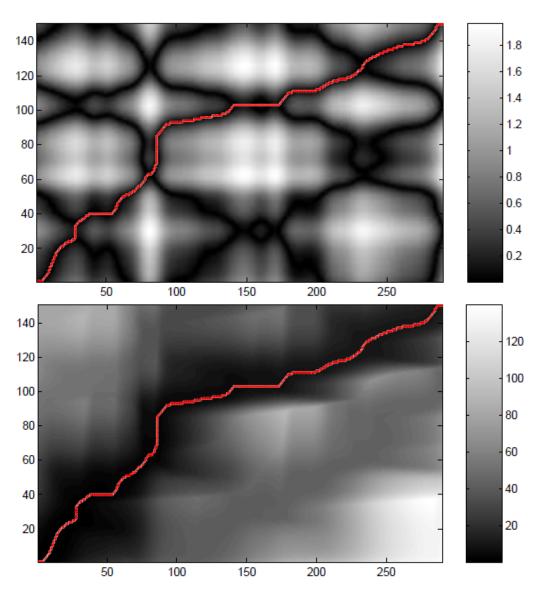


Cost matrix C

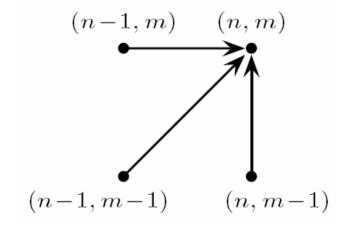
**Optimal warping path** 

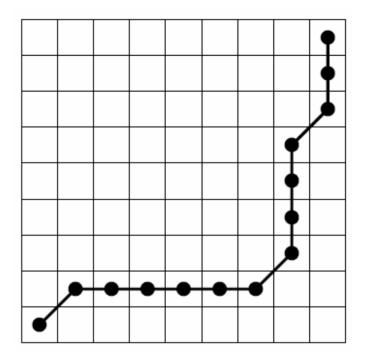
Accumulated cost martrix D

Optimal warping path

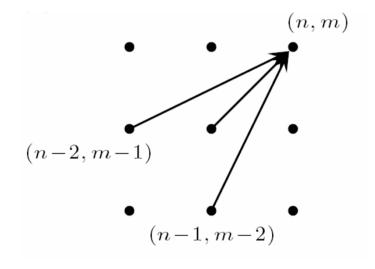


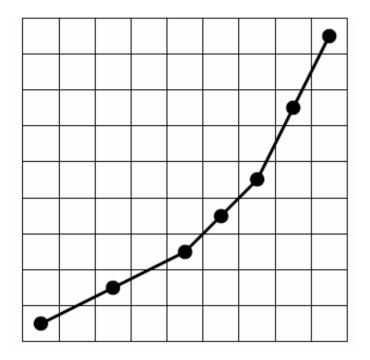
# Dynamic Time Warping Variation of step size condition



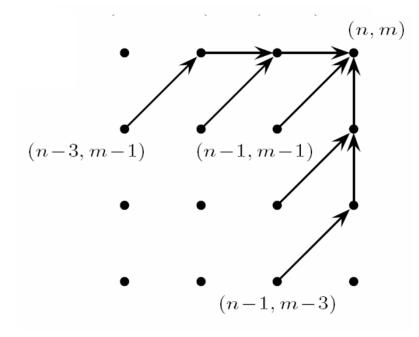


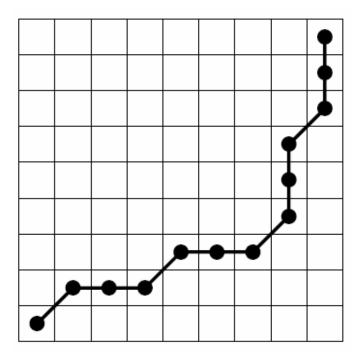
# Dynamic Time Warping Variation of step size condition





# Dynamic Time Warping Variation of step size condition

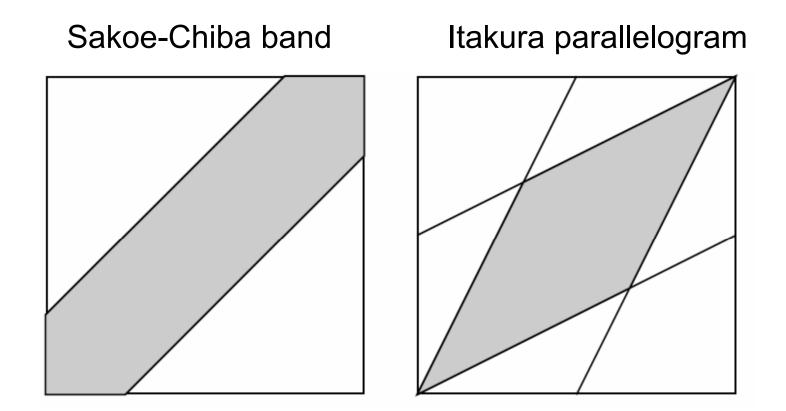




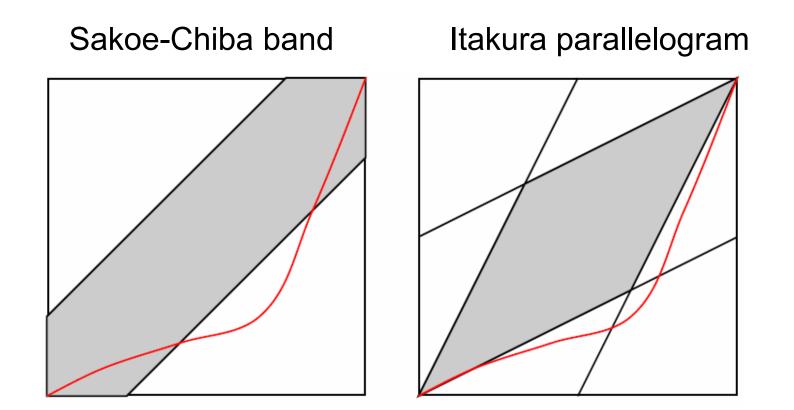
- Computation via dynamic programming
- Memory requirements and running time: O(NM)
- Problem: Infeasible for large *N* and *M*
- Example: Feature resolution 10 Hz, pieces 15 min

 $\Rightarrow N, M \sim 10,000$  $\Rightarrow N \cdot M \sim 100,000,000$ 

Dynamic Time Warping Strategy: Global constraints

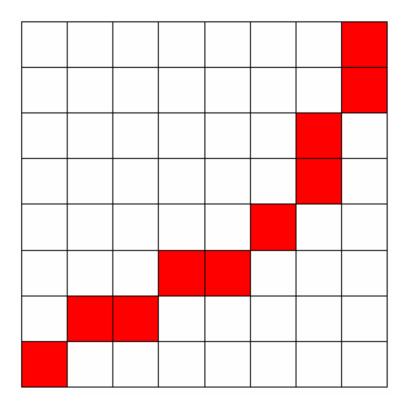


Dynamic Time Warping Strategy: Global constraints



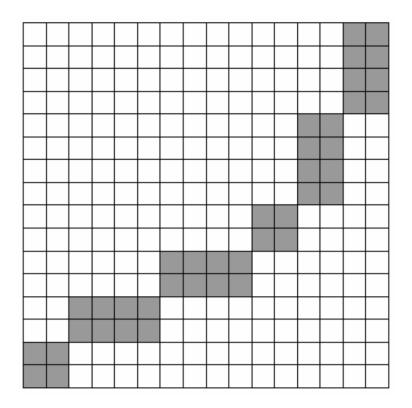
Problem: Optimal warping path not in constraint region

#### Strategy: Multiscale approach



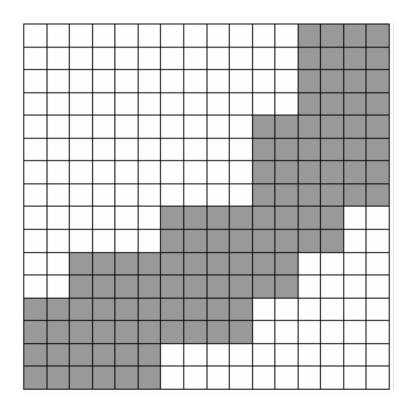
#### Compute optimal warping path on coarse level

#### Strategy: Multiscale approach



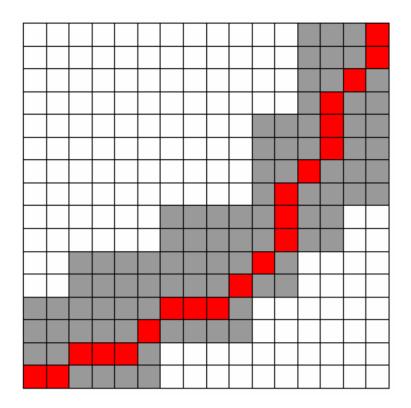
Project on fine level

#### Strategy: Multiscale approach



Specify constraint region

#### Strategy: Multiscale approach



Compute constrained optimal warping path

Dynamic Time Warping Strategy: Multiscale approach

- Suitable features?
- Suitable resolution levels?
- Size of constraint regions?

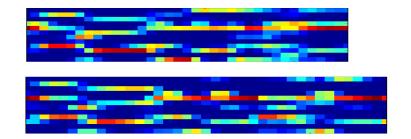
Good trade-off between efficiency and robustness? Suitable parameters depend very much on application!

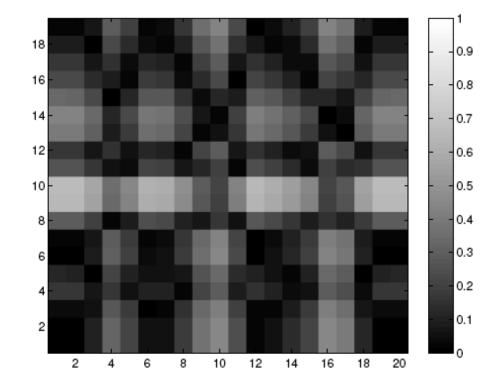
#### Music Synchronization: Audio-Audio

 Transform audio recordings into chroma vector sequences

 $\stackrel{\longrightarrow}{\longrightarrow} X := (x_1, x_2, \dots, x_N)$  $\stackrel{\longrightarrow}{\longrightarrow} Y := (y_1, y_2, \dots, y_M)$ 

• Compute cost matrix  $C(n,m) := c(x_n, y_m)$ with respect to local cost measure c



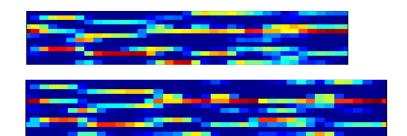


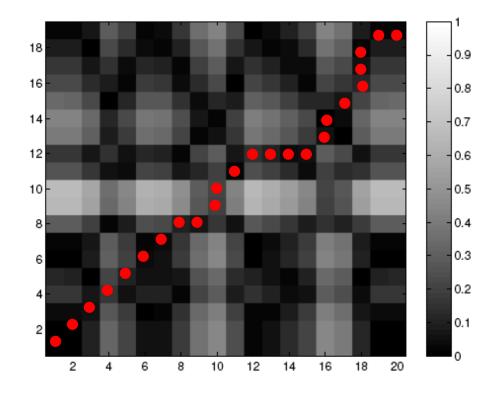
#### Music Synchronization: Audio-Audio

 Transform audio recordings into chroma vector sequences

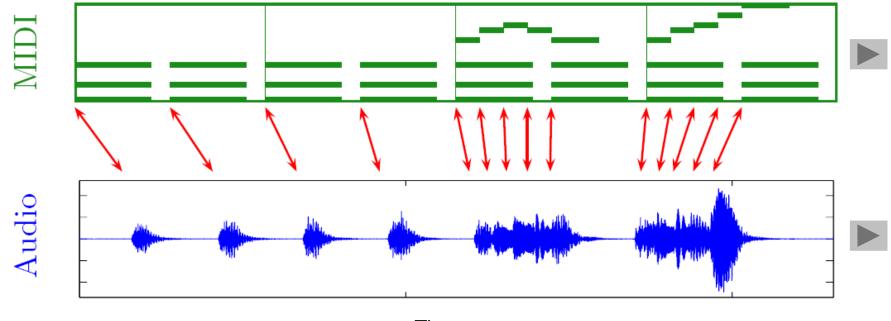
 $\stackrel{\longrightarrow}{\longrightarrow} X := (x_1, x_2, \dots, x_N) \\ \stackrel{\longrightarrow}{\longrightarrow} Y := (y_1, y_2, \dots, y_M)$ 

- Compute cost matrix  $C(n,m) := c(x_n, y_m)$ with respect to local cost measure c
- Compute cost-minimizing warping path from C





## Music Synchronization: MIDI-Audio



Time

Music Synchronization: MIDI-Audio

MIDI = meta data

Automated annotation

Audio recording

Sonification of annotations



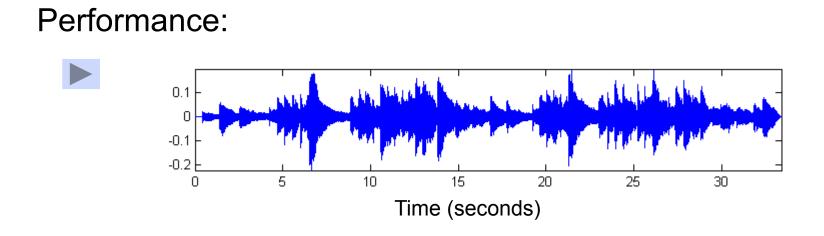
Music Synchronization: MIDI-Audio

MIDI = reference (score)

**Tempo information** 

Audio recording

Schumann: Träumerei

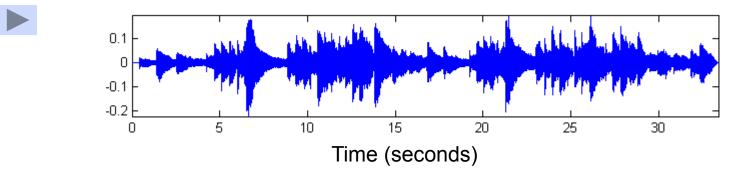


Schumann: Träumerei

Score (reference):



Performance:



Schumann: Träumerei

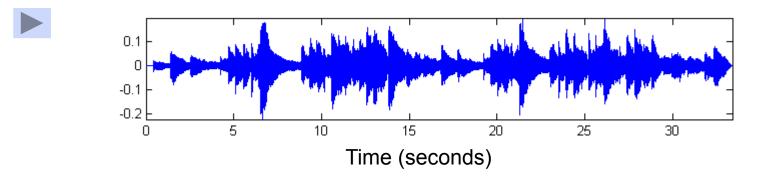
Score (reference):





#### Strategy: Compute score-audio synchronization and derive tempo curve

Performance:

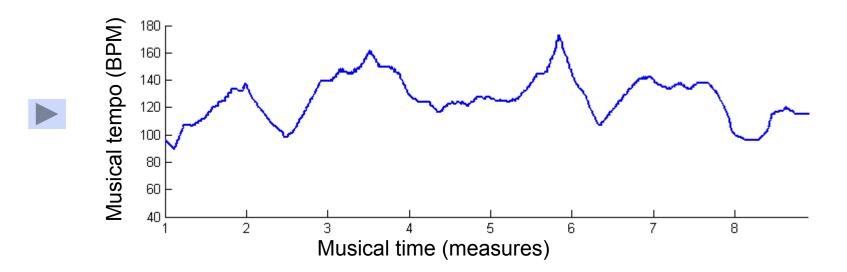


Schumann: Träumerei

Score (reference):



Tempo curve:



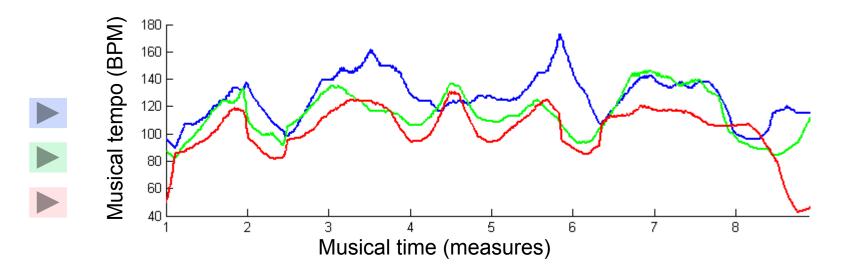
Schumann: Träumerei

Score (reference):





Tempo curves:

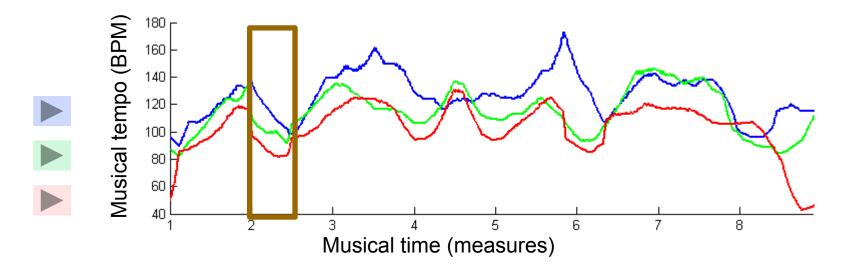


Schumann: Träumerei

Score (reference):



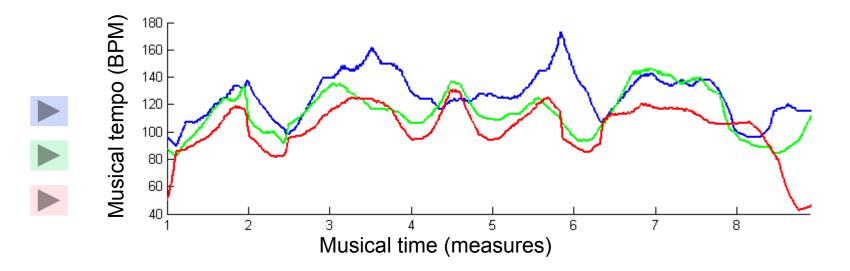
Tempo curves:



Schumann: Träumerei

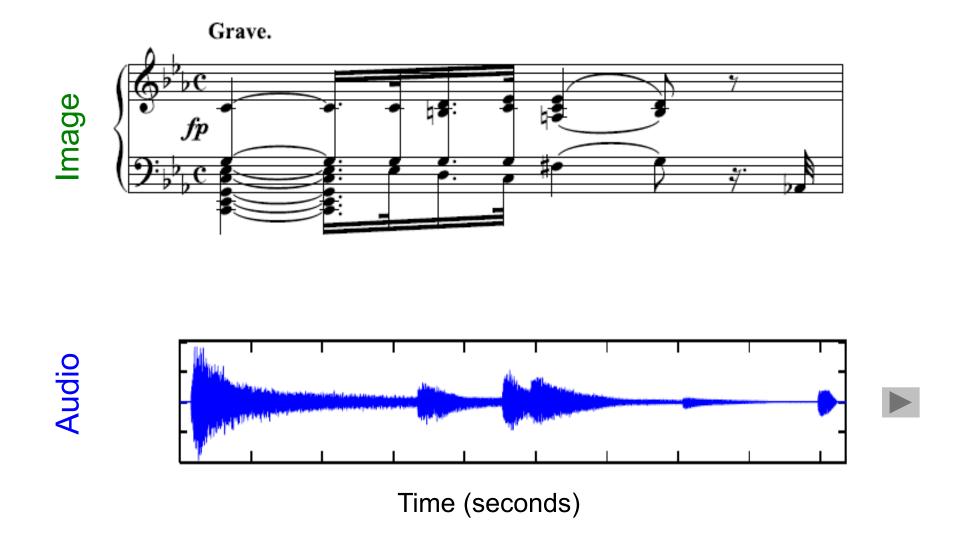
#### What can be done if no reference is available?

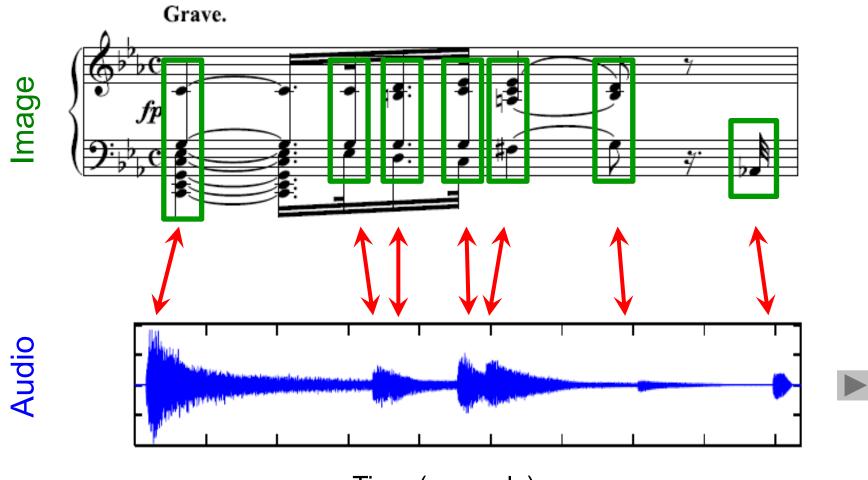
Tempo curves:



# Music Synchronization: MIDI-Audio Applications

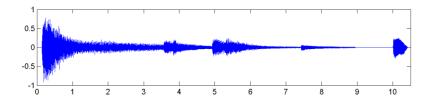
- Automated audio annotation
- Accurate audio access after MIDI-based retrieval
- Automated tracking of MIDI note parameters during audio playback
- Performance Analysis





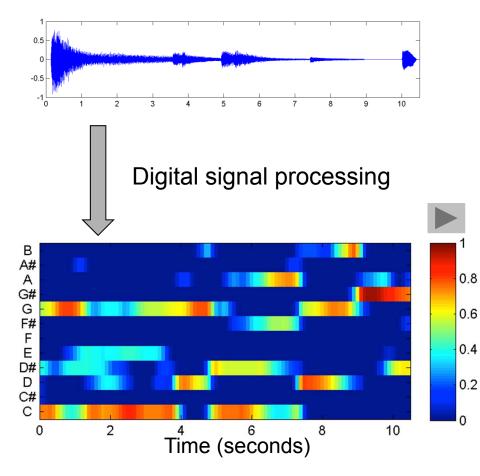
Time (seconds)

Convert into common mid-level feature representation





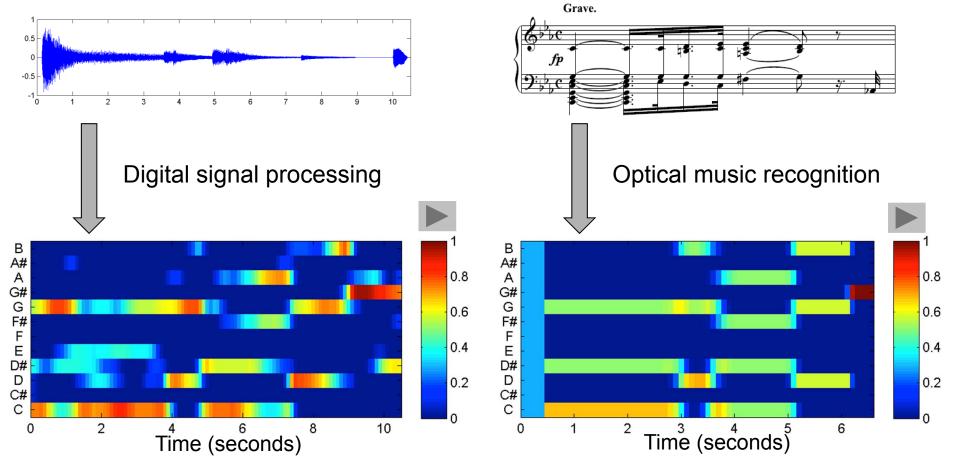
Convert into common mid-level feature representation



Audio chroma representation



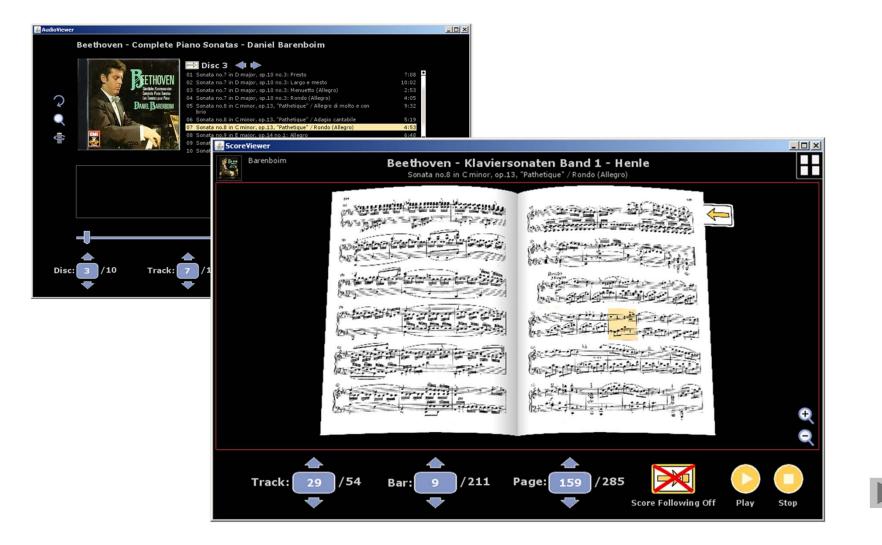
Convert into common mid-level feature representation



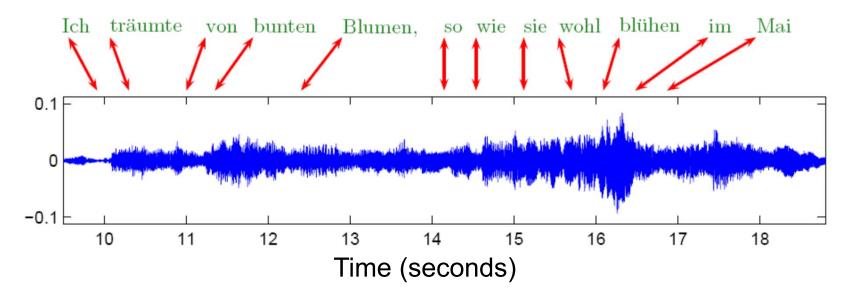
Audio chroma representation

Image chroma representation

#### **Application: Score Viewer**



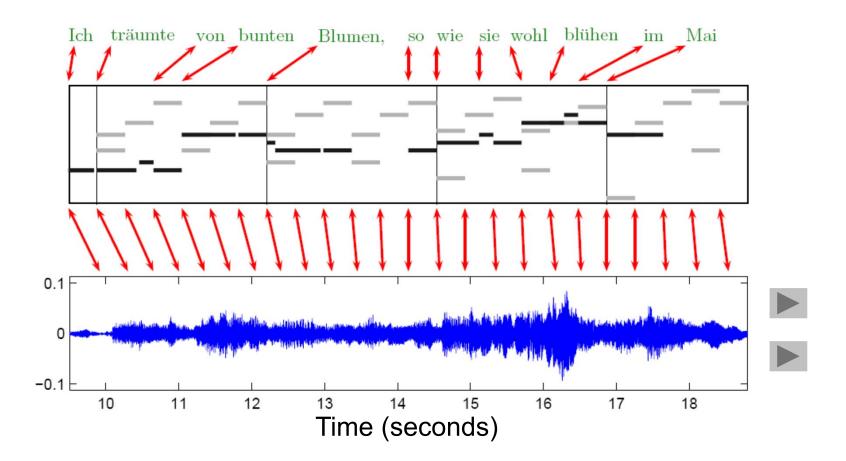
### Music Synchronization: Lyrics-Audio



**Difficult task!** 

### Music Synchronization: Lyrics-Audio

#### Lyrics-Audio $\rightarrow$ Lyrics-MIDI + MIDI-Audio



## Music Synchronization: Lyrics-Audio

#### Application: SyncPlayer/LyricsSeeker



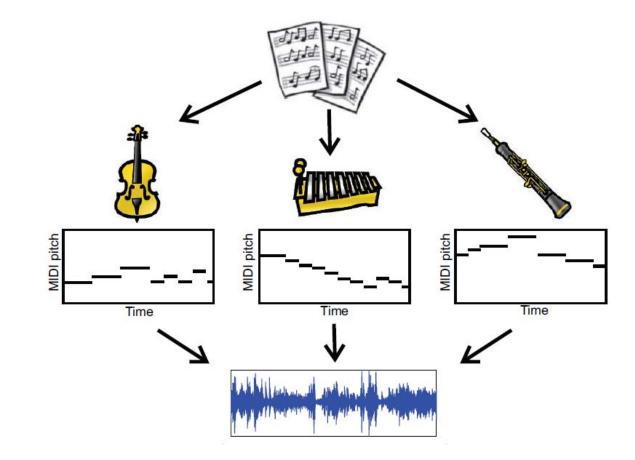
## **Source Separation**

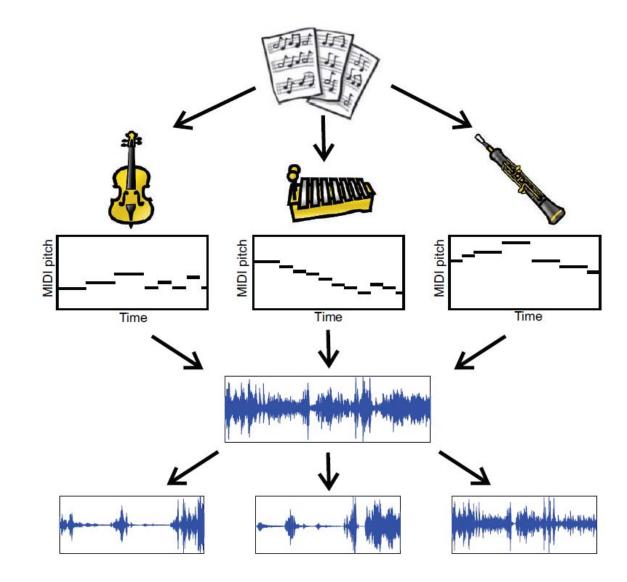
- Decomposition of audio stream into different sound sources
- Central task in digital signal processing
- "Cocktail party effect"
- Sources are often assumed to be statistically independent
- This is often not the case in music

Strategy: Exploit additional information (e.g. musical score) to support the seperation process

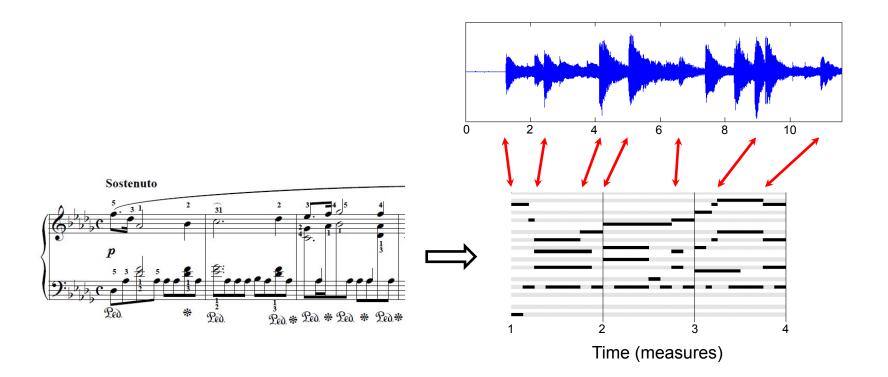


WHI Marken all	Land day the mathematic
MA MANANA	With Miles A Marthan Marth

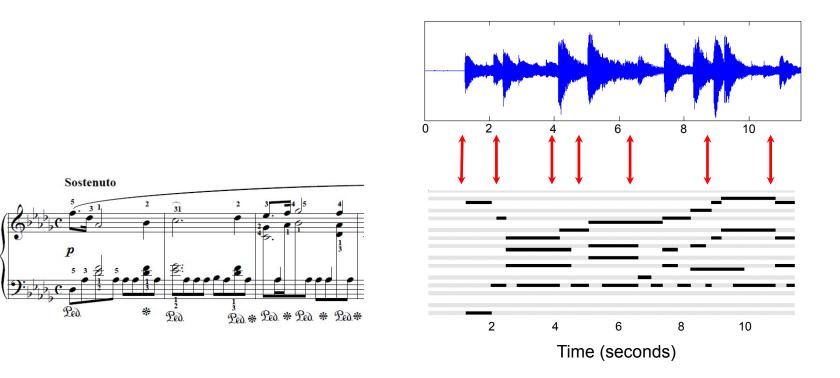




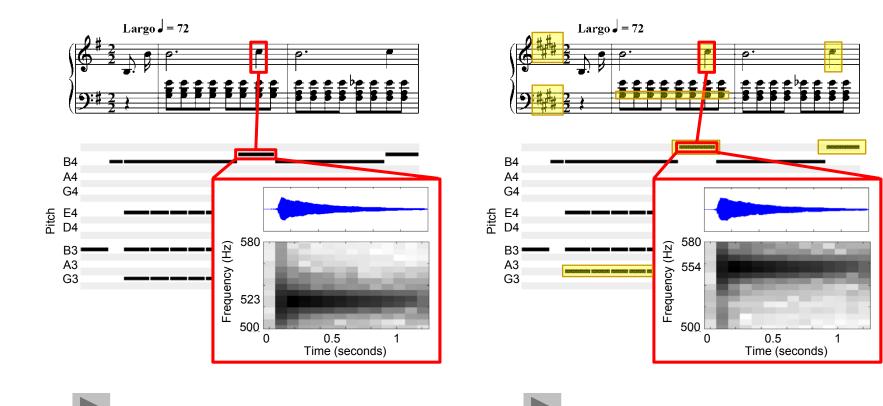
First step: Use music synchronization techniques to generate an audio-synchronous piano roll representation from the score.



First step: Use music synchronization techniques to generate an audio-synchronous piano roll representation from the score.



#### Application: Audio editing



Application: Instrument equalization

